

THESIS

METHODOLOGY FOR CALCULATING SHEAR STRESS IN A MEANDERING  
CHANNEL

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## ABSTRACT

### METHODOLOGY FOR CALCULATING SHEAR STRESS IN A MEANDERING CHANNEL

Shear stress in meandering channels is the key parameter to predict bank erosion and bend migration. A representative study reach of the Rio Grande River in central New Mexico has been modeled in the Hydraulics Laboratory at CSU. To determine the shear stress distribution in a meandering channel, the large scale (1:12) physical modeling study was conducted in the following phases: 1) model construction 2) data collection 3) data analysis, and 4) conclusion and technical recommendations. Data of flow depth, flow velocity in three velocity components ( $V_x$ ,  $V_y$  and  $V_z$ ) and bed shear stress using a Preston tube were collected in the laboratory.

According to the laboratory data analysis, shear stress from a Preston tube is the most appropriate shear stress calculation method. In case of the Preston tube, data collection was performed directly on the surface of the channel. Other shear stress calculation methods were based on ADV (Acoustic Doppler Velocity) data that were not collected directly on the bed surface. Therefore, the shear stress determined from ADV measurements was underestimated. Additionally,  $K_b$  (the ratio of maximum shear stress to average shear stress) plots were generated. Finally, the envelope

equation for  $K_b$  from the Preston tube measurements was selected as the most appropriate equation to design meandering channels.

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## List of Symbols

|              |   |                                                                                                                               |
|--------------|---|-------------------------------------------------------------------------------------------------------------------------------|
| $A$          | = | cross sectional flow area ( $L^2$ )                                                                                           |
| $\alpha$     | = | shear stress by Preston tube ( $M/L^2$ )                                                                                      |
| $b$          | = | the intercept of the regression line of Reynolds Shear Stress (Dimensionless)                                                 |
| $\beta$      | = | shear stress from linear regression of flow velocity profile ( $M/L^2$ )                                                      |
| $\beta_1$    | = | shear stress from the Rozovskii method ( $M/L^2$ )                                                                            |
| $\beta_2$    | = | shear stress from Reynolds shear stress extrapolation ( $M/L^2$ )                                                             |
| COV-XY       | = | the covariance of two variables ( $V_x$ and $V_y$ ) (Dimensionless)                                                           |
| COV-YX       | = | the covariance of two variables ( $V_x$ and $V_y$ ) (Dimensionless)                                                           |
| COV-XZ       | = | the covariance of two variables ( $V_x$ and $V_z$ ) (Dimensionless)                                                           |
| COV-ZX       | = | the covariance of two variables ( $V_x$ and $V_z$ ) (Dimensionless)                                                           |
| COV-ZY       | = | the covariance of two variables ( $V_z$ and $V_y$ ) (Dimensionless)                                                           |
| COV-YZ       | = | the covariance of two variables ( $V_z$ and $V_y$ ) (Dimensionless)                                                           |
| $D$          | = | horizontal distance of piezo between a and Piezo g (L)                                                                        |
| $D$          | = | internal diameter of pipe (L)                                                                                                 |
| $d$          | = | the outer diameter of pitot tube (L)                                                                                          |
| $d_1$        | = | 3 times of the difference of height of Piezo a and d (L)                                                                      |
| $d_2$        | = | Channel bottom width (L)                                                                                                      |
| $d_3$        | = | 3 times of the difference of height of Piezo g and d (L)                                                                      |
| $\delta$     | = | the percentage difference of shear stress between Preston tube and linear regression of flow velocity profile (Dimensionless) |
| $\delta_1$   | = | the percentage difference between Preston tube and Rozovskii Method (Dimensionless)                                           |
| $\delta_2$   | = | the percentage difference between Preston tube and Reynolds Shear Stress Extrapolation (Dimensionless)                        |
| $\partial p$ | = | the differential pressure ( $M/L^2$ )                                                                                         |
| $\partial r$ | = | the differential radius of curvature (L)                                                                                      |
| $g$          | = | the acceleration of gravity ( $L/T^2$ )                                                                                       |
| $\gamma$     | = | specific gravity of water ( $M/L^3$ )                                                                                         |
| $H$          | = | the flow depth (L)                                                                                                            |
| $h$          | = | Difference of water surface elevation between piezo a and g (L)                                                               |
| $k_s$        | = | the grain roughness. (Dimensionless)                                                                                          |
| $\kappa$     | = | the constant of Von Karman (Dimensionless)                                                                                    |
| $K_b$        | = | the ratio of maximum shear stress to averaged shear stress (Dimensionless)                                                    |
| $L$          | = | the length of test section (L)                                                                                                |
| $L_c$        | = | the Channel Length (L)                                                                                                        |
| $L_v$        | = | Straight Line Valley Length of a channel (L)                                                                                  |
| $n$          | = | the number of samples that collected velocity data (Dimensionless)                                                            |
| $P$          | = | the dynamic pressure ( $M/L^2$ )                                                                                              |
| $p_o$        | = | the static pressure ( $M/L^2$ )                                                                                               |

|              |   |                                                                                                            |
|--------------|---|------------------------------------------------------------------------------------------------------------|
| $p_t$        | = | the impact pressure ( $M/L^2$ )                                                                            |
| $\Delta p$   | = | the dynamic pressure (L)                                                                                   |
| $R$          | = | hydraulic Radius (L)                                                                                       |
| $R_c$        | = | radius of curvature of meandering channel (L)                                                              |
| $r$          | = | the radius of curvature of the channel bend (L)                                                            |
| $r_{ce}$     | = | the center radius of curvature in bend (L)                                                                 |
| $r_i$        | = | the inner radius of curvature in bend (L)                                                                  |
| $r_o$        | = | the outer radius of curvature in bend (L)                                                                  |
| $\rho$       | = | the mass density of water ( $M/L^3$ )                                                                      |
| $S$          | = | the lope of the Regression Equation of Velocity Profile                                                    |
| $S_o$        | = | the bed slope of channel (L/L)                                                                             |
| $S_r$        | = | the water surface elevation (L/L)                                                                          |
| $T_w$        | = | top width of channel (L)                                                                                   |
| $\tau_{bed}$ | = | the turbulent shear stress in longitudinal direction that applies on the bed of the channel ( $M/L^1T^2$ ) |
| $\tau_o$     | = | bed shear stress ( $ML^{-2}$ )                                                                             |
| $\tau_r$     | = | the radial shear stress ( $ML^{-1}T^{-2}$ )                                                                |
| $\tau_{xy}$  | = | The turbulent shear stress that applies in y axis and caused by $V_x$ ( $M/L^1T^2$ )                       |
| $\tau_{yx}$  | = | The turbulent shear stress that applies in x axis and caused by $V_y$ ( $M/L^1T^2$ )                       |
| $\tau_{zx}$  | = | The turbulent shear stress that applies in x axis caused by $V_z$ ( $M/L^1T^2$ )                           |
| $\tau_{xz}$  | = | The turbulent shear stress that applies in z axis and caused by $V_x$ ( $M/L^1T^2$ )                       |
| $\tau_{yz}$  | = | The turbulent shear stress that applies in z axis and caused by $V_y$ ( $M/L^1T^2$ )                       |
| $\tau_{zy}$  | = | The turbulent shear stress that applies in y axis and caused by $V_z$ ( $M/L^1T^2$ )                       |
| $\tau_{xx}$  | = | The normal force that applies in x axis and caused by $V_x$ ( $M/L^1T^2$ )                                 |
| $\tau_{yy}$  | = | The normal force that applies in y axis and caused by $V_y$ ( $M/L^1T^2$ )                                 |
| $\tau_{zz}$  | = | The normal force that applies in z axis and caused by $V_z$ ( $M/L^1T^2$ )                                 |
| $\bar{U}$    | = | The vertical averaged streamwise velocity ( $LT^{-1}$ )                                                    |
| $U^*$        | = | The velocity scaling parameter for log law, identical with $u_*$ for uniform 2D flow ( $L/T$ )             |
| $u$          | = | Flow velocity ( $L/T$ )                                                                                    |
| $u_*$        | = | Shear velocity ( $L/T$ )                                                                                   |
| $\nu$        | = | the kinematic viscosity of water ( $L^2/T$ )                                                               |
| $V_x$        | = | The flow velocity along x-axis ( $L/T$ )                                                                   |
| $V_y$        | = | The flow velocity along y-axis ( $L/T$ )                                                                   |
| $V_z$        | = | The flow velocity along z-axis ( $L/T$ )                                                                   |
| $v_\theta$   | = | the flow velocity along the bend of the channel ( $L/T$ )                                                  |
| $v_1$        | = | Flow velocity value that locates in the lowest data collection point ( $L/T$ )                             |
| $v_2$        | = | Flow velocity value that locates just above of the location of $v_1$ ( $L/T$ )                             |

$v_n$  = Flow velocity value that locates in the highest point (L/T)  
 $x$  = the Preston differential pressure (L)  
 $y$  = the distance normal to the plane of the channel bottom (L)  
 $z$  = the vertical distance the bottom of the channel (L)  
 $z_{Bed}$  = Bed elevation of the Channel (L)  
 $\Delta Z$  = Differential flow depth (L)

# **1 Introduction**

## **1.1 Background**

Natural channels never stop changing their geomorphic characteristics. Natural alluvial streams are similar to living creatures because they generate water flow, develop point bars, alter bed profile, scour the bed, erode the bank, and cause other phenomena in the stream system. The geomorphic changes in a natural system lead to a wide array of research worldwide, because methods of predicting channel change are limited. Bank erosion due to meandering of the channel is a critical issue in modern river engineering. In the United States, the severity of the problem was recognized when Congress enacted the Streambank Erosion Control Evaluation and Demonstration Act of 1974 and authorized research in the field (Odgaard 1986). The increased demand for bank erosion research resulted in many theoretical and experimental studies to predict geomorphic changes in natural channels. Julien (2002) describes the magnitude and orientation of applied shear stress as one of the main factors of bank erosion. Julien (2002) also describes the damping of shear stress by erosion control.

## **1.2 Project Background**

The 29-mile-long study reach of Rio Grande River was located in central New Mexico. The study reach was a straight braided system with a shifting sand bed and shallow banks (Heintz 2002). The high supply of sediment caused channelization of the river. Cochiti dam was constructed by the U.S Army Corps of Engineers for the

purposes of flood and sediment transport control for the Albuquerque area in 1973 (Schmidt, 2005). Subsequently, the channel changed from an aggrading to degrading system. As a result, the planform geometry of the reach has changed from a straight braided to active meandering system (Heintz 2002). Channel meandering resulted in bank erosion and lateral migration. Bank erosion and lateral channel migration occurred to satisfy quasi-equilibrium conditions of the stream system. Fish habitat, vegetation, and infrastructure around the stream and farming lands were threatened due to the bank erosion.

Understanding shear stress distribution in the study reach is necessary because shear stress is the key parameter to predict bank erosion and lateral channel migration. Shear stress distribution was investigated through physical modeling conducted by Colorado State University (CSU). For testing purposes, a 1:12 Froude scale model was constructed and tested in the Hydromachinery Laboratory that is located at the Engineering Research Center (ERC) in CSU. The purpose of the physical modeling was to simulate conditions in the reach and to predict the shear stress distribution at four target flow rates: 8, 12, 16 and 20 cubic feet per second (cfs). Laboratory tests were performed in baseline test conditions without installing hydraulic structures in the main channel.

### 1.3 Research Objectives

The focus of this study was shear stress distribution analysis in meandering channels via the following methods: 1) Preston tube; 2) linear regression of velocity profile; 3) Rozovskii Method; and 4) Reynolds shear stress extrapolation.

The objectives of the study were to:

- a) Understand in detail the shear stress distribution mechanism for meandering channels by performing a physical model study;
- b) Calculate shear stress by using four different methods;
- c) Compare the different shear stress values;
- d) Recommend the most appropriate shear stress calculation method for the establishment of a design guide for channels in the field.

The scope of the research was defined to satisfy the objectives:

- a) A comprehensive literature review of previous studies about the shear stress calculation methods in meandering channel;
- b) Analysis of the collected data to calculate shear stress distribution in meandering channel;
- c) Compare and discuss the different shear stress calculation methods;
- d) Recommend the most appropriate shear stress analysis method and direction of future research.

## 2 Literature Review

### 2.1 Introduction

Flow in a meandering channel results in geomorphic changes. A picture of a typical meandering channel is presented in Figure 2.1. Flow in meandering channels results in geomorphic changes, such as bank erosion. Implementation of bank protection to prevent erosion is a significant economic expense. Therefore, a development of a tool for bank implementation is important. This tool would be used to predict shear stress, which is the most important aspect of bank erosion. Since the beginning of the 20<sup>th</sup> century, many researchers have developed methods for the analysis of flow in bends. The literature review provides an explanation of the basic concepts of fluvial geomorphology, Preston tube method, Rozovskii's shear calculation, linear regression of flow velocity profile, and Reynolds shear stress about flow in a bend.



Figure 2.1 Typical Meandering Channel (from Watson et al. (2005))

## 2.2 Open Channel Flow in Meandering Bends

To study flow characteristics in a meandering alluvial channel, a basic understanding of a meandering channel is needed. This section covers the background of meandering channel geometry, flow patterns in bends, erosion patterns and channel stability.

### 2.2.1 Meandering Channel Geometry

Sinuosity is used to describe a meandering channel. When sinuosity is greater than 1.5, the channel is classified as meandering (Knighton 1998). Equation 2.1 describes the method used for calculating channel sinuosity:

$$\text{Sinuosity} = \frac{L_c}{L_v} \quad \text{Equation 2.1}$$

Where,  $L_c$  = the channel length; and

$L_v$  = the straight line valley length.

There are two methods available to analyze meander geometry (Knighton 1998). The first method focused on the individual bend statistics: meander wavelength ( $L$ ) and radius of curvature ( $r_c$ ), which are averaged over a series of bends. The second method is a series approach method that spans sequences of bends and treats the stream trace as a spatial series of flow direction (arc angle  $\theta$ ) or differential change of flow direction ( $\Delta\theta$ ) along the reach (Knighton 1998). For meandering channels, Knighton (1998) states that the second method provides more flexibility for flow characteristics analysis and theoretical model development. Figure 2.2 presents the geometry of meandering channel.

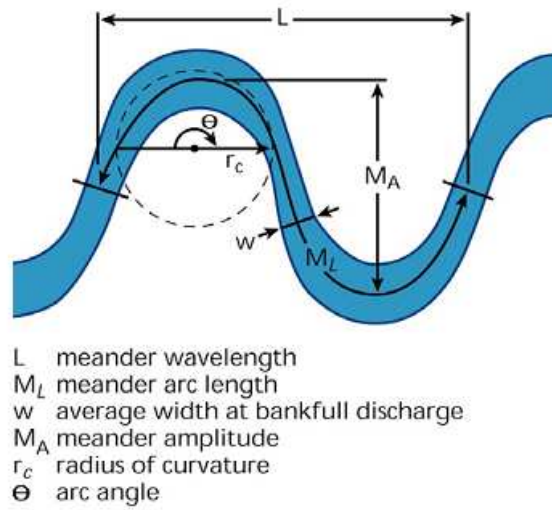


Figure 2.2 Geometry of Meandering Channel (from Watson et al. (2005))

A sine-generated curve is used to develop a simple model of meandering channel, as described by equation 2.2. A pictorial representation of the sine-generated curve is provided in Figure 2.3.

$$\theta = \omega \sin kx \quad \text{Equation 2.2}$$

Where,  $\theta$  = channel direction;

$x$  = flow distance along the reach;

$\omega$  = the maximum angle between a channel segment and the mean downvalley axis; and

$k$  = the ratio of  $2\pi$  to the meander wavelength.

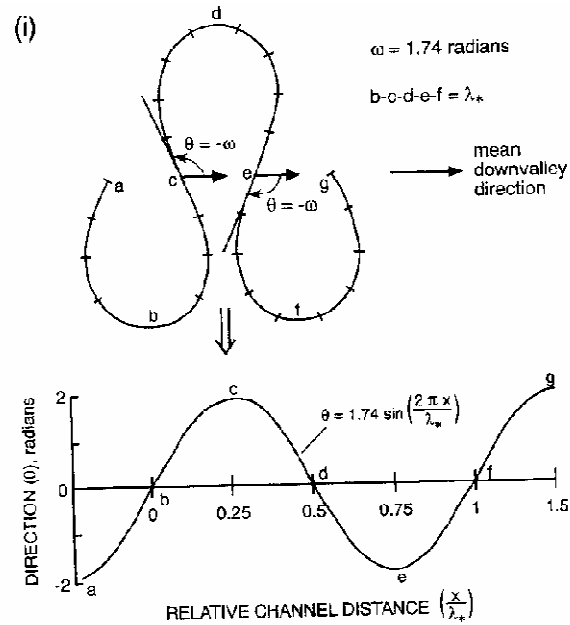


Figure 2.3 Description of Sine-Generated Curve Function (from Knighton (1998))

## 2.2.2 Flow Patterns in Meandering Channels

The description of flow patterns in a meandering channel has three components; stream morphology, transverse velocity distribution in bends, and superelevation of the water surface against the outside of the bank. This section explains the three main components of flow patterns in meandering channels.

### 2.2.2.1 Stream Morphology

A geomorphic sketch of a straight and meandering channel is presented in Figure 2.4. Pool-riffle sequences are the characteristics of cobble, gravel and mixed load rivers of moderate gradient (smaller than 5%) (Sear 1996). Topographic high points are defined as riffles and low points are defined as pools (Watson, et al. (2005)). The grain sizes found in riffles are larger than pools. Keller (1971) explained that the reason for the difference in grain size is caused by the sorting

process. In addition, Keller (1971) explains that fine sediments are removed from riffles during low flows due to flow velocity and shear stress. These sediments are then deposited in pools. Normally, the outer side of the bank is deeper than the inside bank, forming a point bar at the inside bank. In addition, the following features are also observed in natural streams: point bars, middle bars, alternate bars and braiding. Figure 2.5 shows a typical meandering stream with point bars.

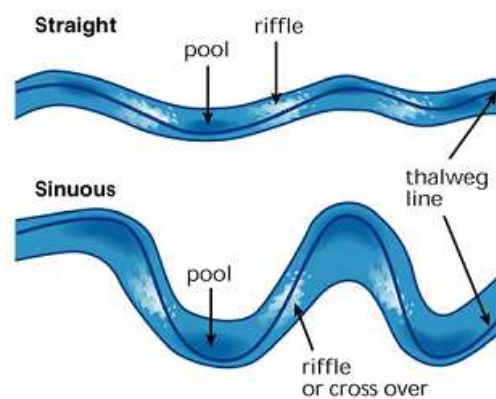


Figure 2.4 Schematic Description of Straight Channel and Meandering Channel (from Federal Interagency Stream Restoration Working Group (FISHRWG) (1998)).



Figure 2.5 A typical meandering stream with point bars (from Watson et al. (2005))

Point bars form at the inside bank of a bend as seen in Figure 2.5. The factors which influence the formation of point bars are flow characteristics, degree of sinuosity, and sediment transportation. Reduction of sediment transport capacity at the inside of the bank, transverse flow velocity distribution and secondary currents in bends result in the formation of point bars (Watson et al. (2005)). A pictorial representation of a middle bar is shown in Figure 2.6. A middle bar is a depositional feature located within the channel, but not connected to the banks.



Figure 2.6 Typical Middle Bar (from Watson et al. (2005))

Alternate bars are regularly-spaced depositional features that are located in the opposite sides of a straight or slightly sinuous stream (Watson et al. (2005)). Figure 2.7 presents the typical shape of alternate bars. Alternate bars are good indicator of the initiation of a meander or braided planform (Watson et al. (2005)). Figure 2.8 shows a braided river, which is composed of a straight channel with multi-threads. In the case of braid bars, the mobility is very high.



Figure 2.7 Typical Alternate Bars (from Watson et al. (2005))



Figure 2.8 Typical Braid Bars (from Watson et al. (2005))

### 2.2.2.2 Transverse Velocity Distribution in Bends

Imbalance in radial pressure around the bend causes the transverse velocity distribution in a meandering channel (FHWA (Federal Highway Administration) 2001). Figure 2.9 represents a typical cross section within a bend and the velocity distribution. The radial forces that act on the shaded control volume are the centrifugal force that was presented in Equation 2.3 (FHWA 2001):

$$F_c = \frac{mv^2}{r} \quad \text{Equation 2.3}$$

Where,  $F_c$  = the centrifugal force ( $MLT^{-2}$ );

$r$  = the value of radius of curvature (L);

$m$  = the mass of the moving object (M); and

$v$  = the moving velocity of the object ( $LT^{-1}$ ).

In addition, superelevation of the water surface,  $dz$ , results in the differential hydrostatic force  $\gamma dz$ . Therefore, the centrifugal force is greater near the surface where the flow velocity is greater and less at the bed where the flow velocity is small (FHWA 2001). The differential hydrostatic force is constant throughout the depth of the control volume. In addition, Figure 2.9 (b) explains that the combination of centrifugal force and hydrostatic force causes a secondary flow in the bend (FHWA 2001).

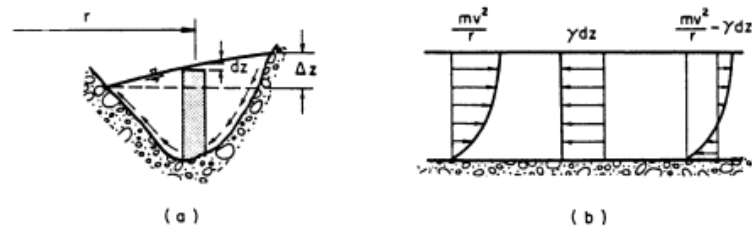


Figure 2.9 Schematic Descriptions of Flow in Meandering Channel (from FHWA (2001))

### 2.2.2.3 Superelevation against the Outside of the Bank

Due to the centrifugal force of flow in the bend, there is a superelevation of the water surface in the bend (FHWA 2001). The water surface elevation at the outer bank is higher than at the inside of the bank. The differential pressure in the radial direction results from the radial acceleration and can be expressed by Equation 2.4. A sketch of the flow around a bend is provided in Figure 2.10.

$$\frac{1}{\rho} \times \frac{\partial p}{\partial r} = \frac{v_{\theta}^2}{r} \quad \text{Equation 2.4}$$

Where,  $\rho$  = the mass density of water ( $M/L^3$ );

$\partial p$  = the differential pressure ( $M/L^2$ );

$\partial r$  = the differential radius of curvature (L); and

$v_{\theta}$  = the flow velocity along the bend of a channel (L/T).

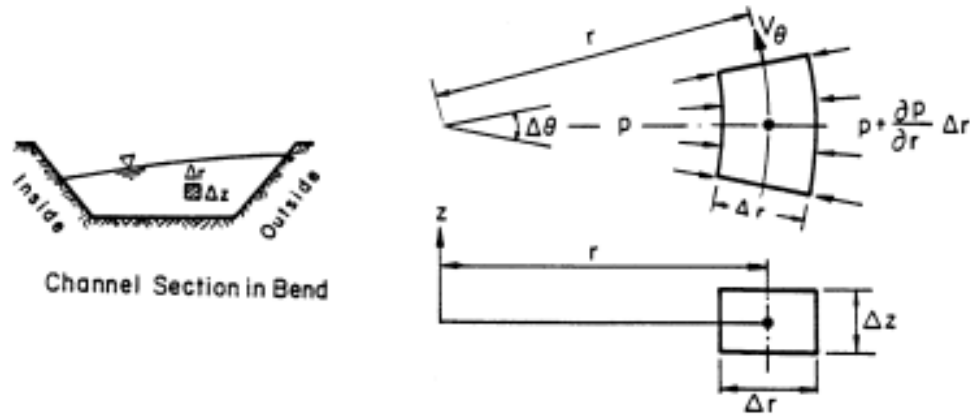


Figure 2.10 Sketch of the flow around bend (from FHWA (2001))

For the calculation of the superelevation, two assumptions should be made;

- a) The magnitudes of radial and vertical velocities are smaller than tangential velocities.
- b) Distribution of pressure in the bend is hydrostatic.

If the two assumptions are satisfied, it is possible to calculate the superelevation by using Equation 2.5.

$$\Delta Z = \frac{V_{\max}^2}{2g} \left( 2 - \left( \frac{r_i}{r_{ce}} \right)^2 - \left( \frac{r_{ce}}{r_o} \right)^2 \right) \quad \text{Equation 2.5}$$

Where,  $\Delta Z$  = height of superelevation (L);

$V_{\max}^2$  = maximum flow velocity ( $L^2/T^2$ );

$g$  = acceleration of the gravity ( $L/T^2$ );

$r_i$  = the inner radius of curvature in bend (L);

$r_{ce}$  = center radius of curvature in bend (L); and

$r_o$  = outer radius of curvature in bend (L).

### 2.2.3 Erosion Patterns in Meandering Rivers

Figure 2.11 shows the geomorphic change of a straight channel into a meandering channel. There are four stages to change a straight channel into a meandering channel (after Keller, 1972):

- a) Alternating bars dominant. (Stage 1)
- b) Development of incipient pools and riffles (Stage 2)
- c) Development of well-developed pools and riffles with a mean spacing of 5 to 7 channel widths. (Stage 3)

- d) Development of meandering channel with riffles at inflection points and pools at bend apices where bank erosion is concentrated. (Stage 4)

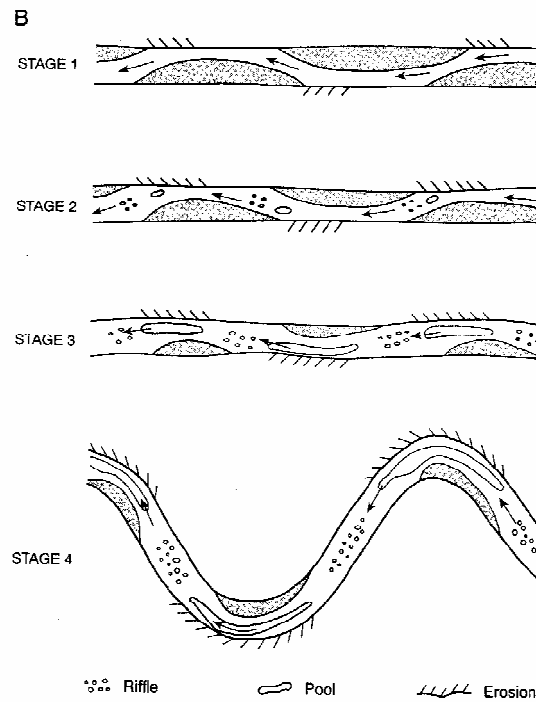


Figure 2.11 Geomorphic Change of Straight Channel into Meandering Channel (from Knighton, (1998))

In addition, Knighton (1998) explained that the relationship between flow and geomorphic form has a link with the radius of the curvature versus width relationship, which can alter flow pattern in meandering channel. Bagnold (1960) claimed that if the ratio of radius of curvature and channel width is smaller than 2, water filaments begin to separate from the inner bank. Hickin and Nanson (1975) suggested that there is a corresponding reduction in the rate of erosion at the concave bank. Hickin and Nanson (1986) plotted the relationship of relative migration rate to bend curvature for 18 rivers (Figure 2.12)

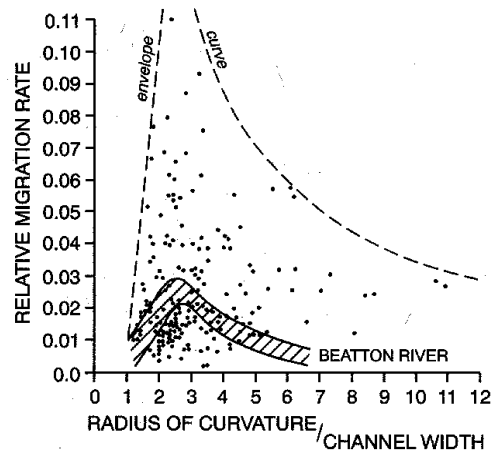


Figure 2.12 The relationship of relative migration rate to bend curvature for 18 rivers (from Knighton (1998))

It is hard to predict the planform of the channel, but the U.S Federal Highway Administration (2001) suggested the modes of meander loop development will aid in planform prediction. Figure 2.13 presents the seven modes of the meander loop development. These modes are: A) Extension B) Translation C) Rotation D) Conversion to a compound loop E) Neck cutoff by closure F) Diagonal cutoff by chute G) Neck cutoff by chute (FHWA (2001)).

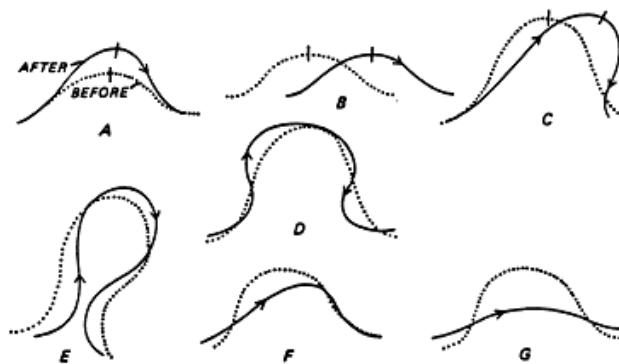


Figure 2.13 Seven Modes of Meander Loop Development (from FHWA (2001))

## 2.2.4 Channel Stability

It is possible to classify the stream system as stable or unstable. The criterion of the classification depends on whether the stream has adjusted or is still adjusting to the flow and sediment regimes (FHWA 2001). A graded stream is defined as a stream that is not necessarily static or fixed and may exhibit temporary morphological changes in response to the impacts of extreme events. The main attitude of a graded stream is that fluvial processes operating under formative flows tend to restore stream morphology to the graded condition (FHWA 2001). This type of stability is described as dynamic equilibrium. To explain the concept of dynamic equilibrium, the concept of Lane's balance (1955) is commonly used. The schematic sketch of Lane's balance is provided in Figure 2.14. Lane's balance shows the change of the following four variables:  $Q$ ,  $S$ ,  $Q_s$  and  $D_{50}$ . If one or more of these variables change, the river will responded by causing a change in the other variables to restore equilibrium.

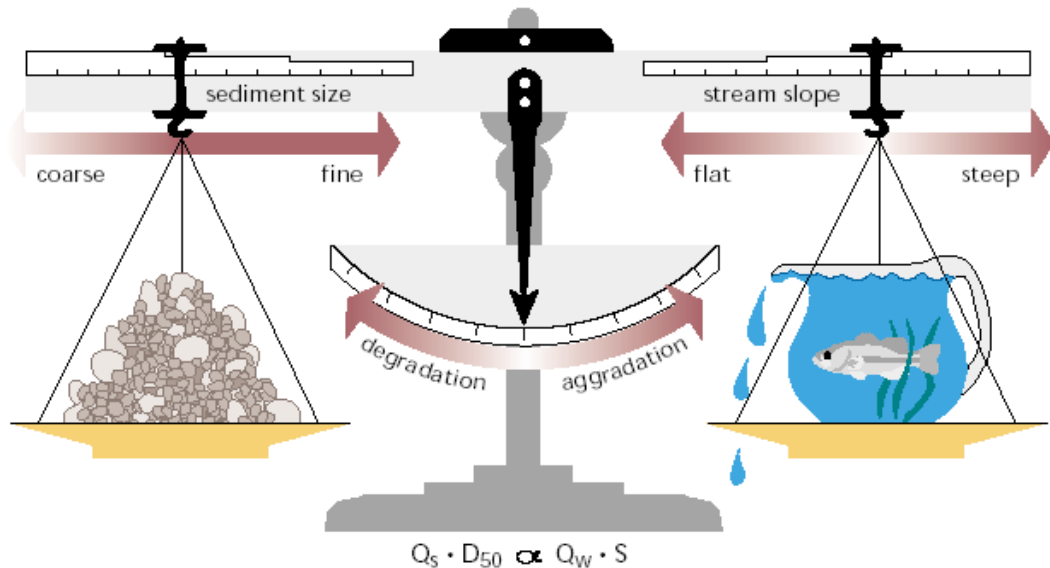


Figure 2.14 Lane's Balance (from Rosgen (1996))

The following equation describes Lane's balance;

$$QS \sim Q_s D_{50} \quad \textbf{Equation 2.6}$$

Where,  $Q$  = water flow rate ( $L^3/T$ );

$S$  = slope ( $L/L$ );

$Q_s$  = sediment flow rate ( $M/T$ ); and

$D_{50}$  = median size of bed material ( $L$ ).

## **2.3 Shear Stress Calculation Methods**

Calculation methods of shear stress in meandering channels have been suggested by many researchers. In this section, the techniques for calculating shear stress using the concept of Reynolds shear stress, Rozovskii method, linear regression of flow velocity profile method and Preston tube method will be introduced.

### **2.3.1 Preston Tube**

Preston tube method computes shear stress by locating a Preston tube directly on the bed of the channel at the point of measurement. After data collection, calibration was performed to convert data from an electronic signal into bed shear stress.

#### **2.3.1.1 Preston (1954)**

Preston (1954) performed a laboratory study to determine turbulent skin friction by using pitot tubes. The purpose of the laboratory study was to calculate skin friction that applies on the surface. Before Preston (1954), Stephens and Haslam (1938) suggested the method to determine local skin friction by reading local static pressure. The relationship between local skin friction and local static pressure is presented in Equation 2.7.

$$\frac{(P - p_o) \times d^2}{\rho \nu^2} = F \left( \frac{\tau_o d^2}{\rho \nu^2} \right) \quad \text{Equation 2.7}$$

Where,  $F$  = representative linear function;

$P$  = dynamic pressure (slug×ft/s<sup>2</sup>);

$p_o$  = static pressure (slug×ft/s<sup>2</sup>);

$d$  = pitot tube diameter taken as a representative length (ft);

$\rho$  = mass density of water (slug/ft<sup>3</sup>);

$\nu$  = kinematic viscosity of water (ft<sup>2</sup>/s); and

$\tau_o$  = boundary shear stress (slug×ft/s<sup>2</sup>).

For circular pipe, Preston (1954) explained shear stress,  $\tau_o$  can be calculated from Equation 2.8.

$$\tau_o = (p_1 - p_2) \frac{D}{4L} \quad \text{Equation 2.8}$$

Where,  $\tau_o$  = boundary shear stress (slug×ft/s<sup>2</sup>);

$p_1$  = pressure at the beginning of length,  $L$  (slug×ft/s<sup>2</sup>);

$p_2$  = pressure at the end of length,  $L$  (slug×ft/s<sup>2</sup>);

$D$  = internal diameter of pipe (ft); and

$L$  = the length of test section (ft).

The instrument for data collection is presented in Figure 2.15. For the data collection, four different pitot tubes were used. The dimensions of the pitot tubes are presented in Table 2.1.

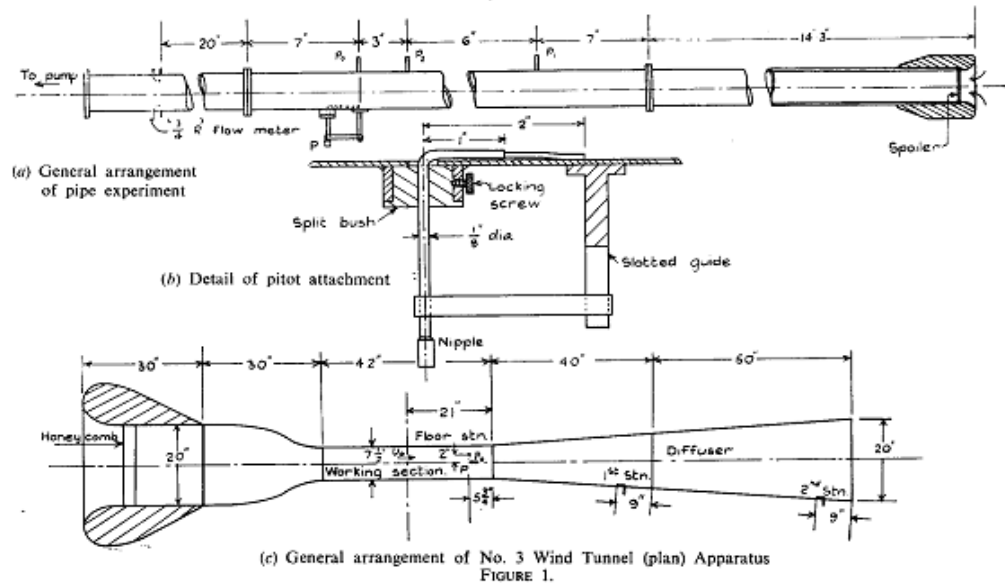


Figure 2.15 Sketch of Data Collection Facility of Preston (from Preston (1954))

Table 2.1 Dimension of the Pitot Tubes (from Preston (1954))

| Pitot Tube Number                      | 1       | 2      | 3      | 4      |
|----------------------------------------|---------|--------|--------|--------|
| External Diameter (in)                 | 0.02915 | 0.0544 | 0.0907 | 0.1214 |
| Ratio:<br>(Internal/External) Diameter | 0.602   | 0.603  | 0.599  | 0.598  |

The result of experiments in the laboratory was presented in Figure 2.16. Preston (1954) also presents two different equations by expressing the relationship between  $\log_{10} \frac{\tau_o d^2}{4\rho v^2}$  and  $\frac{(p - p_o)d^2}{4\rho v^2}$  in the non-dimensional form. For the condition of  $\log \frac{(p_t - p_o)^2}{4\rho v^2} > 5$ , the equation is expressed in Equation 2.9 and the expression of the relationship under the condition of viscous flow was presented in Equation 2.10.

$$\log_{10} \frac{\tau_o d^2}{4\rho v^2} = 2.604 + \frac{7}{8} \times \log_{10} \frac{(p - p_o) d^2}{4\rho v^2} \quad \text{Equation 2.9}$$

$$\log_{10} \frac{\tau_o d^2}{4\rho v^2} = \frac{1}{2} \left( \log_{10} 2 + \log_{10} \frac{(p - p_o)^2}{4\rho v^2} \right) \quad \text{Equation 2.10}$$

Where,  $P$  = dynamic pressure (slug×ft/s<sup>2</sup>);

$p_o$  = static pressure (slug×ft/s<sup>2</sup>);

$d$  = pitot tube diameter taken as a representative length (ft);

$\rho$  = mass density of water (slug/ft<sup>3</sup>);

$\nu$  = kinematic viscosity of water (ft<sup>2</sup>/s); and

$\tau_o$  = boundary shear stress (slug×ft/s<sup>2</sup>).

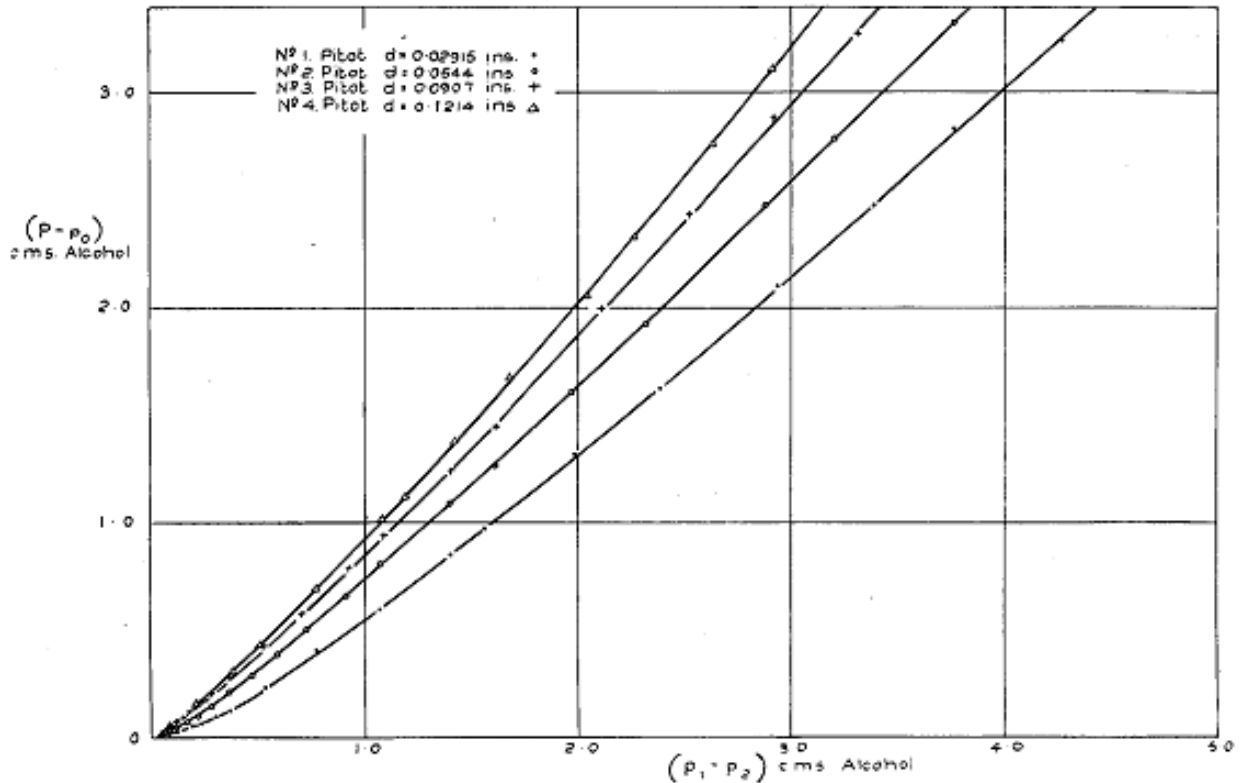


Figure 2.16 Actual Observations of round pitot on wall of circular pipe (from Preston (1954))

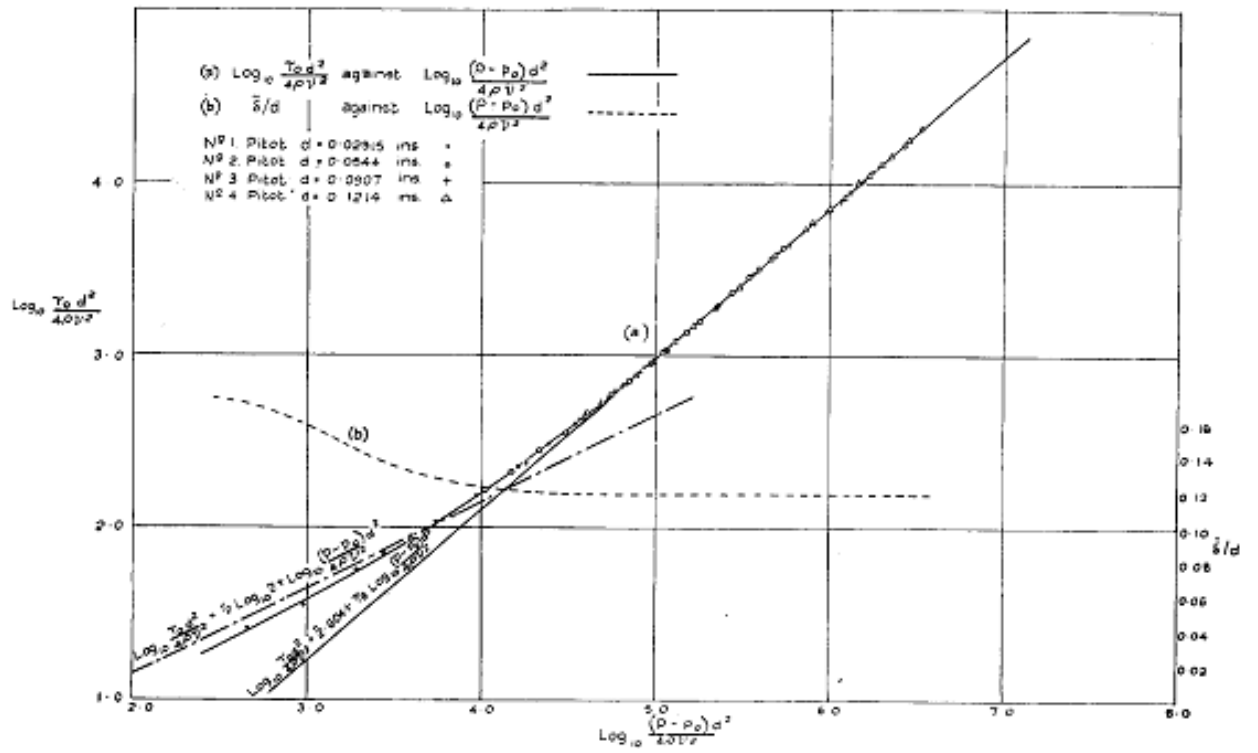


Figure 2.17 The Plot of Non-Dimensional Results of Experimentations of Preston (1954)

### 2.3.1.2 Ippen and Drinker (1962)

Ippen and Drinker (1962) performed laboratory experiments to correlate the impacts of shear stress on meandering channel bank erosion by using a Preston tube. Two flumes were constructed for data collection. The geometry of each flume was trapezoidal. Table 2.2 presents the geometric information of the two flumes. Figure 2.18 provides a sketch of the flumes in the laboratory.

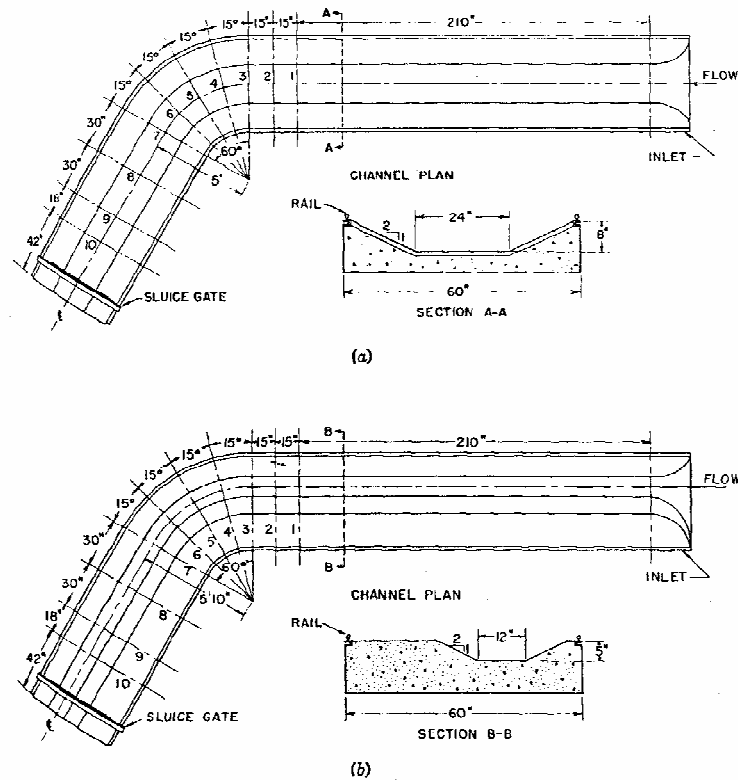


Figure 2.18 Sketches of Laboratory Flume (from Ippen and Drinker (1962))

Table 2.2 Geometric Information of Flume (from Ippen and Drinker (1962))

|               | Shape of Cross Section | Side Slope (Horizontal :Vertical) | Rotation Angle (Degrees) | Bottom Width (inch) | Radius of curvature (inch) |
|---------------|------------------------|-----------------------------------|--------------------------|---------------------|----------------------------|
| Larger Flume  | Trapezoidal            | 2:1                               | 60                       | 24                  | 60                         |
| Smaller Flume | Trapezoidal            | 2:1                               | 60                       | 12                  | 70                         |

For flow depth adjustment at the curve entrance, a sluice gate was installed at the exit section to control downstream flow depth. At the beginning of the experiment, the Manning's roughness coefficient was assumed as 0.009. As the experiment progressed, calculation of the roughness coefficient was conducted and the result was 0.010. To measure boundary shear stress, Ippen and Drinker (1962) selected the Preston method (1954) presented in Equation 2.11. This method computes shear stress on a smooth boundary by the pressure differential between static and dynamic pitot tubes resting on the bed surface. Ippen and Drinker (1962) calibrated the pressure head recorded in shear stress measurements in pounds per square feet by using Equation 2.11.

$$\log \frac{\tau_o d^2}{4\rho v^2} = -1.396 + 0.875 \times \log \frac{(p_t - p_o)^2}{4\rho v^2} \quad \text{Equation 2.11}$$

Where,  $\tau_o$  = local boundary shear stress (psf);

$d$  = the outer diameter of pitot tube;

$\rho$  = the mass density of water (slug/ft<sup>3</sup>);

$v$  = the kinematic viscosity of water (ft<sup>2</sup>/sec);

$p_t$  = the impact pressure (psf); and

$p_o$  = the static pressure (psf).

After experimental investigation of flow in meandering channels by using a Preston tube, Ippen and Drinker (1962) drew the following conclusions;

- a) The maximum value of shear stress that resulted from the curved flow is not possible to predict by theoretically or using empirical coefficient of head loss in curved flow at present.
- b) During the laboratory experiments, in the case of large curvatures, a high value of shear was observed near the inside bank in the curve and near the outside bank below the curve exit.
- c) The laboratory test proved that boundary shear stress distribution is an important parameter to understand erosion and deposition processes in meandering channel.

### 2.3.1.3 Heintz (2002)

Heintz (2002) carried out Preston tube calibration to measure shear stress in a curved channel constructed at the Engineering Research Center located at Colorado State University. A pressure transducer was used for the collection of pressure data in a trapezoidal meandering channel. Figure 2.27 presents the Preston tube and pressure transducer that were used in the calibration. Equation 2.12 was obtained after Preston tube calibration.

$$\tau = 0.02788 \times \gamma \times \Delta p \quad \text{Equation 2.12}$$

Where,  $\tau$  = the shear stress (psf);

$\gamma$  = the specific gravity of water (lb/ft<sup>3</sup>); and

$\Delta p$  = the dynamic pressure ft of H<sub>2</sub>O.

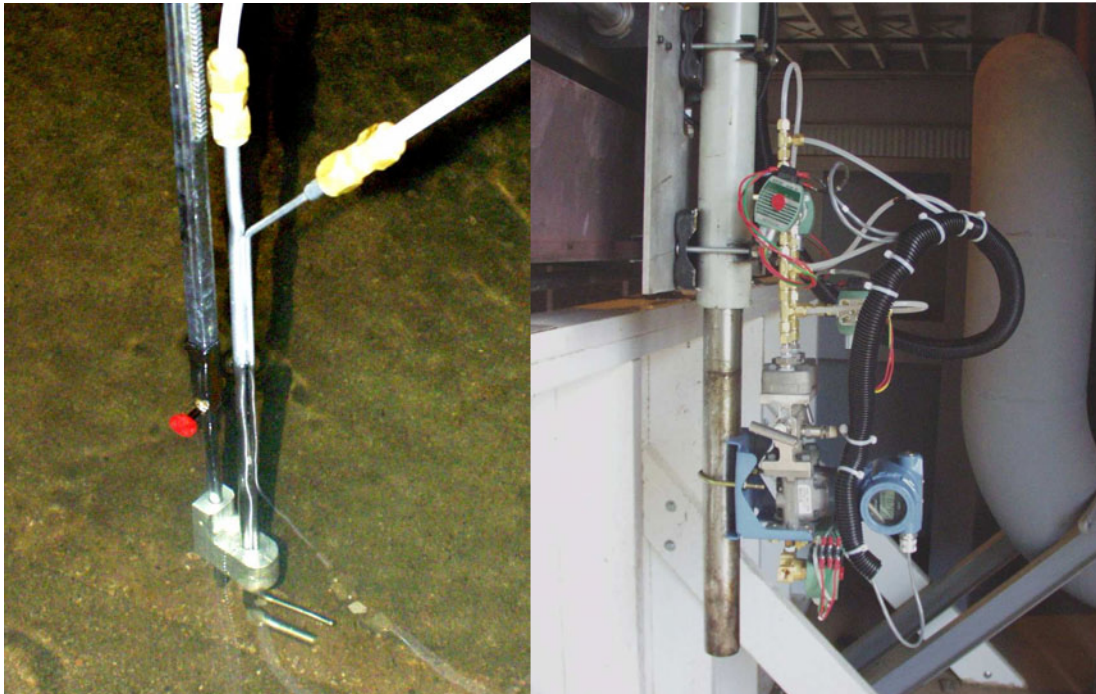


Figure 2.19 Preston Tube for Shear Stress Measurement (at left) and Pressure Transducer (at right) (from Heintz 2002)

#### 2.3.1.4 Sclafani (2008)

Sclafani (2008) carried out another Preston tube calibration in the Engineering Research Center in Colorado State University. Sclafani (2008) explained that the purpose of the second Preston tube calibration was to overcome the limitation of the meandering channel geometry and to develop uniform flow completely in the flume. The Preston tube was installed and calibrated in a 60-foot long, 4-foot wide, 2.5-foot tall flume (Sclafani (2008)).

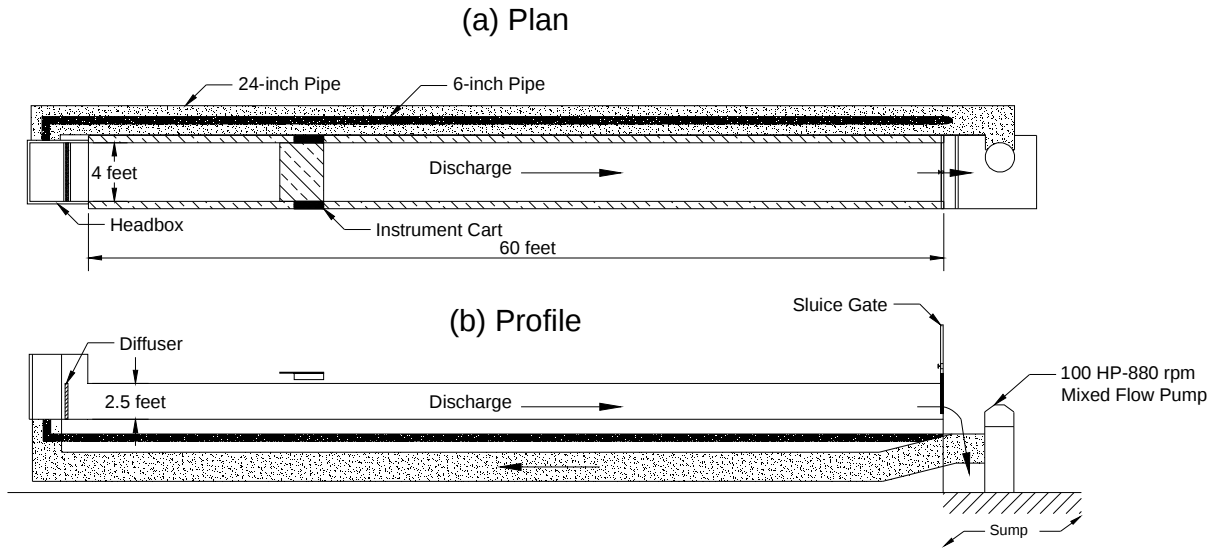


Figure 2.20 Schematic Sketch of the Flume (Sclafani (2008))

After the second Preston tube calibration, Sclafani (2008) obtained a close relationship between differential pressure and bed shear stress presented in Equation 2.13.

$$\tau = 0.1644 \times dp \quad \text{Equation 2.13}$$

Where,  $\tau$  = the shear stress (psf); and

$dp$  = the differential pressure (in).

### 2.3.2 Linear Regression of Flow Velocity Profile

Linear regression of flow velocity profile method for shear stress calculation is based on the relationship between the logarithmic profile of flow depth and flow velocity. In this section, relevant studies of the method will be presented.

#### 2.3.2.1 Clauser (1956)

Shear velocity can be calculated using Equation 2.14. If Equation 2.14 is rearranged, it is possible to obtain shear stress.

$$u_* = \sqrt{\frac{\tau_o}{\rho}} \quad \text{Equation 2.14}$$

Where,  $u_*$  = the shear velocity. ( $LT^{-1}$ )

$\tau_o$  = the bed shear stress. ( $ML^{-2}$ )

$\rho$  = the mass density of water. ( $ML^{-3}$ )

According to Clauser (1956), shear velocity can be obtained by taking linear regression between mean point velocity,  $u$  and natural log of  $\left[ \left( y + \frac{y + 0.2d_{50}}{d_{50}} \right) \right] + B$

$$u = \alpha \times \ln \left[ \left( y + \frac{y + 0.2d_{50}}{d_{50}} \right) \right] + B \quad \text{Equation 2.15}$$

Where,  $\alpha$  and  $B$  = the slope and intercept of the linear regression respectively (Dimensionless);

$y$  = the distance normal to the plane of the channel bottom (L); and

$d_{50}$  = the grain size for 50 % of the material weight is finer. (L)

Also, Afzalimehr and Anctil (2000) explained combination of law of the wall with Equation 2.15 generates Equation 2.16 to estimate shear velocity. The result of this combination is presented in Equation 2.16.

$$\frac{u}{u_*} = \frac{1}{\kappa} \times \ln \left[ \left( \frac{y + 0.2 \times d_{50}}{k_s} \right) \right] + B \quad \textbf{Equation 2.16}$$

Where,  $u$  = the mean point velocity in the longitudinal direction (L/T);

$u_*$  = the shear velocity. (LT<sup>-1</sup>);

$\kappa$  = von Karman coefficient;

$y$  = the distance normal to the plane of the channel bottom (L);

$k_s$  = the grain roughness. (Dimensionless); and

$B$  = the intercept of the Equation 2.16.

### 2.3.2.2 Schlichting (1987)

Schlichting (1987) suggested a bed shear stress calculation method by applying a linear regression between the logarithmic profile of flow depth and flow velocity. The shear stress calculation method is explained in Equation 2.17 through Equation 2.19.

$$V = \frac{u_*}{\kappa} \ln \left( \frac{z}{z_o} \right) \quad \text{Equation 2.17}$$

$$V = \frac{u_*}{\kappa} \ln z + C \quad \text{Equation 2.18}$$

$$\text{Where, } C \text{ is the constant: } -\frac{u_*}{\kappa} \ln(z_o) \quad \text{Equation 2.19}$$

$\frac{u_*}{\kappa}$  is the slope of linear regression equation.

As a result, the shear stress can be computed by Equation 2.20;

$$\tau = \rho \times (\kappa \times S)^2 \quad \text{Equation 2.20}$$

Where,  $S$  = the slope of the Equation 2.19;

$\kappa$  = von Karman coefficient. It was assumed that the value of 0.4; and

$z$  = the vertical distance the bottom of the channel (L).

### 2.3.2.3 Smart (1999)

Smart (1999) published a theory of turbulent velocity profiles and boundary shear by analyzing field data. Smart (1999) collected velocity data at six rivers in New Zealand by using an ADV (Acoustic Doppler Velocity) meter. Three rivers have medium flow condition; Waiho, North Ashburton, and Rangitata rivers. The other three rivers have floods condition; Waitaki, Hurunui, and Rangitata rivers. Smart (1999) obtained the flow resistance equation presented in Equation 2.21

$$\frac{\bar{U}}{U^*} = 2.5 \times \left[ \ln \left( M \frac{gH}{U^{*2}} \right) - 1 \right] \quad \text{Equation 2.21}$$

To determine the M value in Equation 2.21, the relationship between shear velocity head and hydraulic roughness was plotted in Figure 2.21.

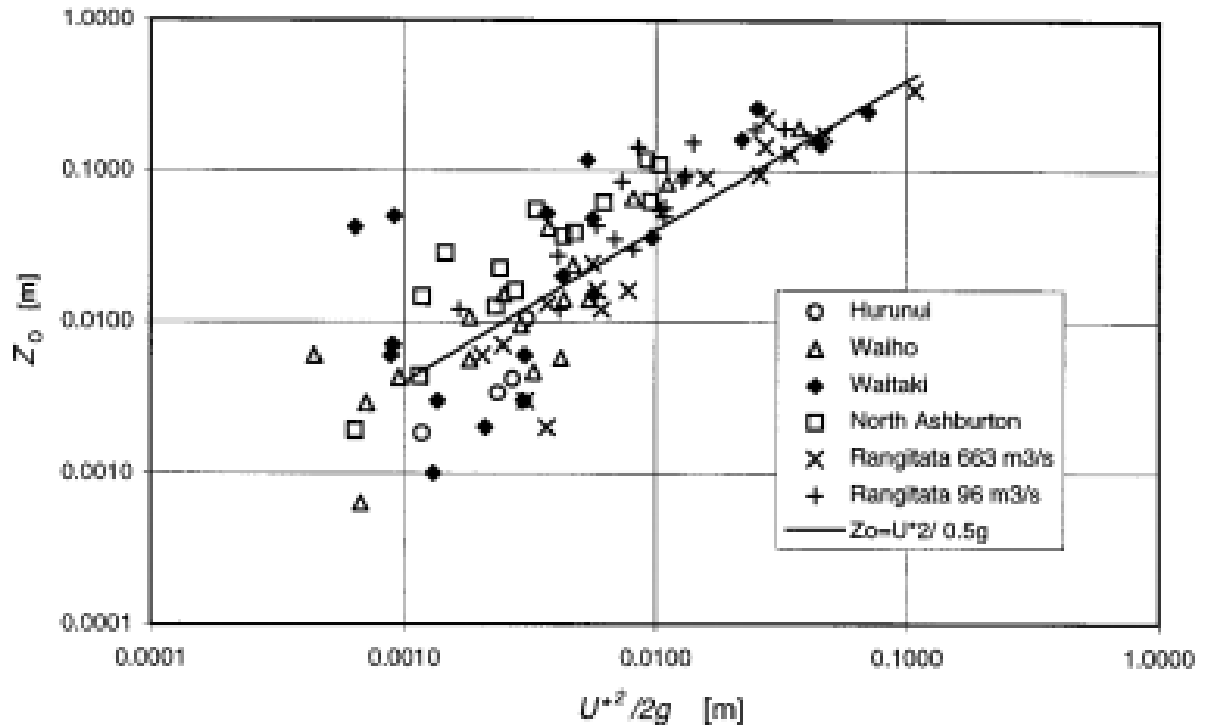


Figure 2.21 Relationship between Log Profile Parameters and Shear Velocity Head (from Smart 1999)

Where,  $\bar{U}$  = the vertical averaged streamwise velocity ( $LT^{-1}$ );

$U^*$  = the velocity scaling parameter for log law, identical with  $u_*$  for uniform 2D flow. ( $LT^{-1}$ ); and

$M$  = the coefficient that relates shear velocity head to hydraulic roughness. (Dimensionless)

Smart (1999) concluded that the collected field data indicate that the grain roughness is proportional to the log profile parameter,  $U^*$  under the condition of mobile bed channels. In addition, Smart (1999) claimed that bed shear stress,  $\tau_o$  is linearly proportional to the grain roughness in case of uniform flow conditions.

### 2.3.3 Rozovskii's Method (1961)

The method presented by Rozovskii is for the radial shear stress computation by using equations that were derived from Cartesian coordinates. Rozovskii published a paper titled 'Flow of Water in Bends of Open Channels' in 1957 which was translated into English in 1961 at Academy of Science of the Ukrainian SSR Institute of Hydrology and Hydraulic Engineering. Rozovskii introduced the equations for analyzing the flow characteristics in a meandering channel. In addition, Rozovskii (1961) provided a comparison and discussion of other researchers' studies since the introduction of the radial shear stress calculation method in meandering channel. Rozovskii's radial shear stress equation in meandering channel is provided in Equation 2.22;

$$\tau_r = [\rho g S_r h] - \left[ \rho \times \int_0^h \frac{v_\theta^2}{R} dz \right] \quad \text{Equation 2.22}$$

Where,  $\tau_r$  = the radial shear stress ( $\text{ML}^{-1}\text{T}^{-2}$ );

$\rho$  = the mass density of the fluid ( $\text{ML}^{-3}$ );

$g$  = the acceleration of gravity ( $\text{LT}^{-2}$ );

$S_r$  = the water surface elevation ( $\text{L/L}$ );

$h$  = the flow depth ( $\text{L}$ );

$v_\theta$  = the flow velocity along the bend of the channel ( $\text{LT}^{-1}$ ); and

$r$  = the radius of curvature of the channel bend ( $\text{L}$ ).

Before Rozovskii (1961) suggested the method for radial shear stress computation, several researchers conducted laboratory tests to figure out the flow characteristics in meandering channels. Table 2.3 presents the summary of the laboratory tests.

Table 2.3 Summary of Experiment Results of Flow in Bend (from Rozovskii, 1961)

| Author                         | Year of Experiments | Rotation Angle (Degrees) | Channel Width (cm) | Radius of Curvature (cm) | Flow Depth (cm) | Mean Flow Velocity (cm/sec) | h/b         | h/r          | Channel Form                                     | Subject Of Measurement                                                |
|--------------------------------|---------------------|--------------------------|--------------------|--------------------------|-----------------|-----------------------------|-------------|--------------|--------------------------------------------------|-----------------------------------------------------------------------|
| Milovich                       | 1914                | 180                      | 24                 | 28                       | 0.45-13.8       | 0.66-5                      | -           | -            | Rectangular                                      | Trajectories of Bottom Particles with the aid of coloring Material    |
| Daneliya                       | 1936                | 180                      | 40                 | 60                       | 12              | 18                          | 0.3         | 0.2          | Rectangular                                      | Distribution of longitudinal and transverse velocity components       |
| Kozhevnikov                    | 1940-1941           | 180                      | 80                 | 160                      | 2-10            | 22-50                       | 0.025-0.125 | 0.0125-0.067 | Rectangular<br>Triangular<br>Parabolic           | Trajectories of Bottom and surface floats, topography of free surface |
| Mockmore                       | 1943                | 2×180                    | 45                 | 52.5                     | 9-12            | 15-25                       | 0.2-0.27    | 0.17-0.23    | Rectangular                                      | Longitudinal Velocity components topography of free surface           |
| Shuckry                        | 1949-1950           | 45-180                   | 30                 | 15-90                    | 18-36           | 90-78                       | 0.6-1.2     | 0.4-1.2      | Rectangular                                      | Distribution of Velocities, topography of free surface                |
| A.I Fidman                     | 1949                | 3×117                    | 100                | 225                      | 11.5-16         | 8.7-3.6                     | 0.12-0.16   | 0.051-0.071  | Rectangular                                      | Topography of free surface                                            |
| M.I Terasvatsyan               | 1950                | 180                      | 38.4               | 58                       | -15             | 30-40                       | 0.39        | 0.26         | Rectangular                                      | Distribution of Velocities, with aid of ball nozzle                   |
| Same                           | 1950                | 67                       | 38.4               | 209                      | -11             | -                           | 0.29        | 0.048        | Rectangular                                      | Distribution of Velocities, with aid of ball nozzle                   |
| A.K Ananyan                    | 1953                | 2×180                    | 50                 | 250                      | 15-18           | 26-33                       | 0.3-0.36    | 0.06-0.72    | Rectangular                                      | Distribution of Velocities, with aid of ball nozzle                   |
| N.I Makkareev<br>B.E Romanenko | 1940                | 180                      | 25                 | 50                       | 3-12            | 20-72                       | 0.1-0.5     | -            | Rectangular of sinusoidal configuration in plane | Velocity Distributions                                                |

### 2.3.3.1 Laboratory Study for Validation of Theory

For the validation of the theory of Rozovskii, a physical model was constructed by the Hydraulic Laboratory of the Institute of Hydrology at the USSR Academy of Sciences. The rotation angle was 90 degrees, radius of curvature was 16.4 ft, the maximum flow depth was 0.459 ft and bed slope was 0.001 ft/ft. A hydrometric tube was used for the velocity measurement. To obtain the velocity profile, flow velocity measurements were carried out. The depth increment was 0.0656 ft. In the case of the bend section that starts at cross section 14, a nozzle ball was used for the velocity measurement. Figure 2.22 shows the test results for flow velocity distribution.

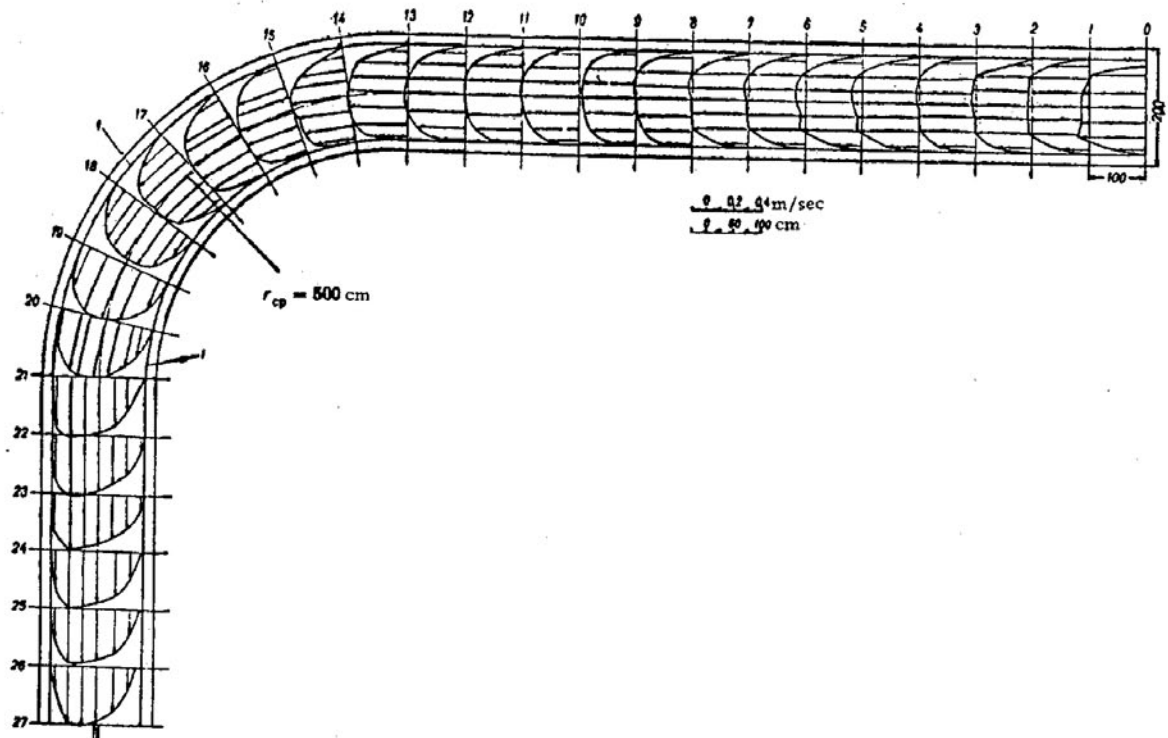


Figure 2.22 Velocity Distribution from the Test result by the Experiment of Polygonal Section (from Rozovskii, 1961)

### 2.3.3.2 Field Observation for Validation of Theory

Field observations were also performed by the Hydraulic Laboratory of the Institute of Hydrology USSR Academy of Sciences in 1951~1952. The locations of the field observation were the Snov River and Desna River. The rotation angle of the study reach of Desna River is  $180^\circ$  and radius of curvature is 400 m. Figure 2.23 shows the study reach of the river. During the field observation, field surveying was performed to determine the water surface elevation and flow depth. According to the surveying results, the general cross section is rectangular. The flow depth was especially deep at cross section 4 the location of contraction of the channel width to 110 m. For measuring the flow velocity, a rotary flow meter with an elongated vane was used.

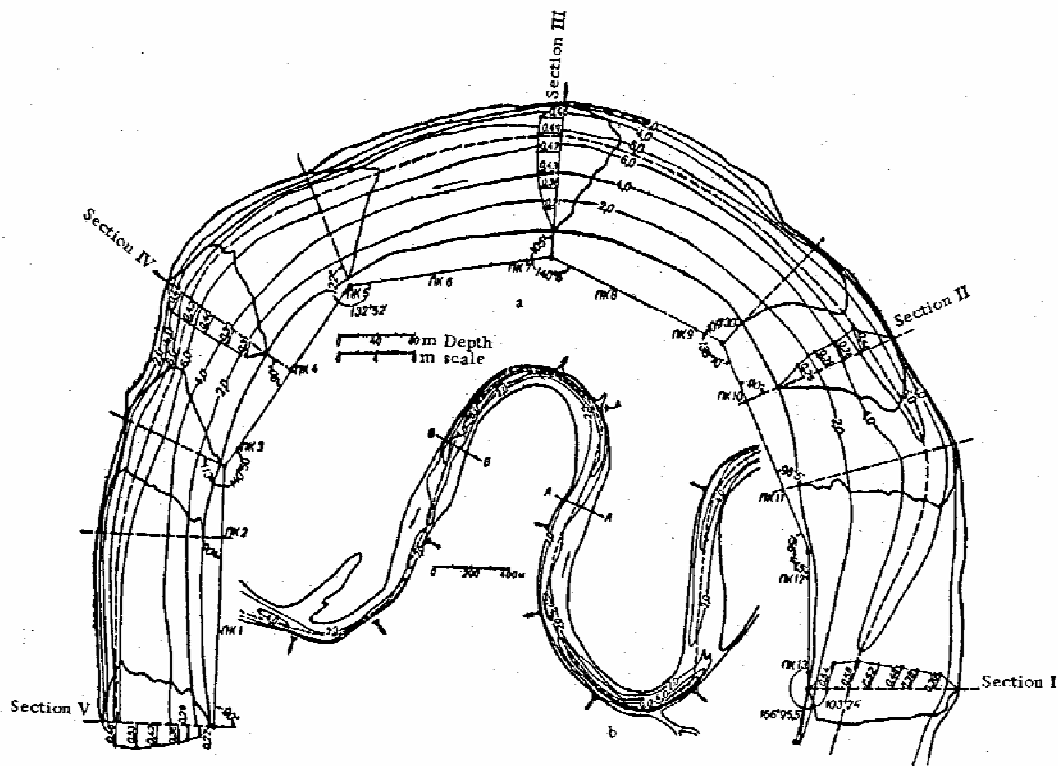


Figure 2.23 Description of Study Reach, Desna River (from Rozovskii, 1961)

Another field observation was performed at the Snov River by Hydraulic Laboratory of the Institute of Hydrology USSR Academy of Sciences. The geometry of the Snov River explained below. Figure 2.18 also shows the plan view and velocity distribution of the Snov River.

- 1) The averaged channel width was 82.02 ft.
- 2) The radius of curvature was 279 ft.
- 3) Maximum flow velocity was 2.624 ft/sec.
- 4) Discharge of Snov River was about 2119 ft<sup>3</sup>/sec.
- 5) Bed Slope was 0.000382 ft/ft.

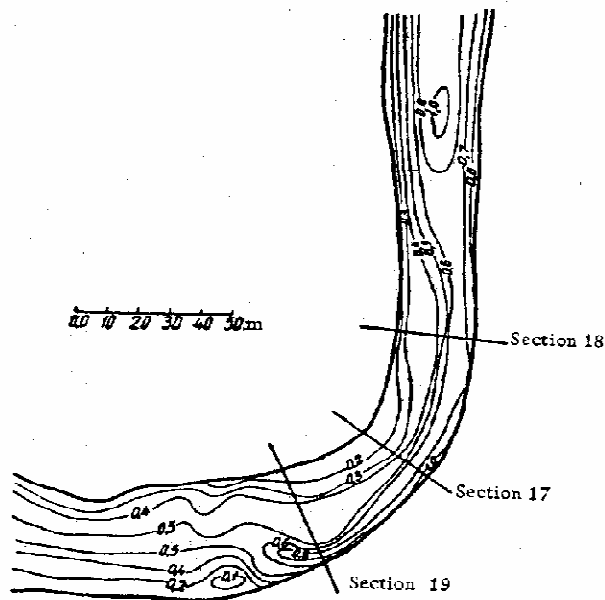


Figure 2.24 Plan View of Snov River (from Rozovskii, 1961)

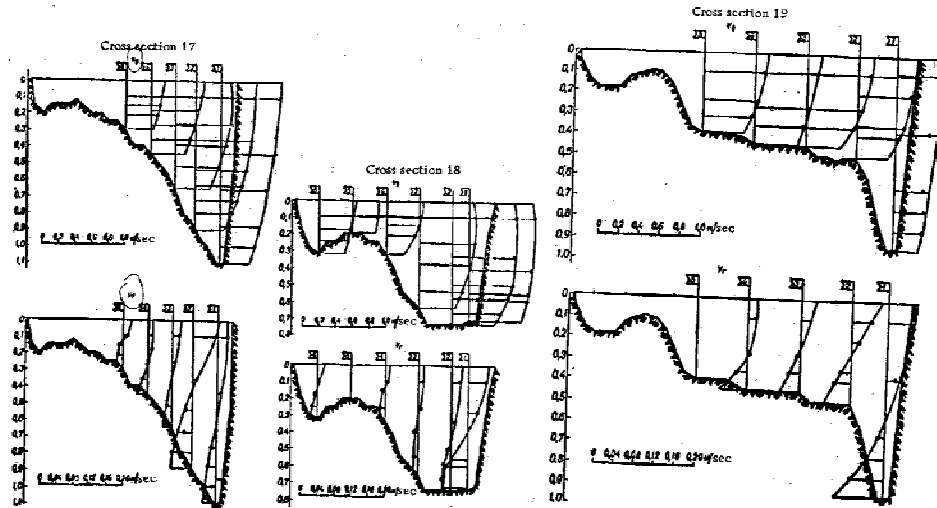


Figure 2.25 Distribution of Flow Velocity of Snov River (from Rozovskii, 1961)

According to the results of the laboratory study and field observations, Rozovskii (1961) concluded that there was good agreement between field observation and the desired theoretical equation. Following Rozovskii's research, several people such as Odgaard (1986) conducted mathematical modeling to determine flow characteristics for a meandering channel.

### 2.3.4 Reynolds Shear Stress

Julien (1998) explained the Cartesian element of fluid composed with two different forces; internal and external forces. Internal forces apply at the center of the mass (Julien 1998). In case of external forces, stress can be classified as two other components; normal and tangential stress. The study focuses on the calculation of the tangential stress that corresponds with Reynolds shear stress comprised of six different components;  $\tau_{xy} = \tau_{yx}$ ,  $\tau_{xz} = \tau_{zx}$  and  $\tau_{yz} = \tau_{zy}$ . A schematic sketch of surface stresses is presented in Figure 2.26.

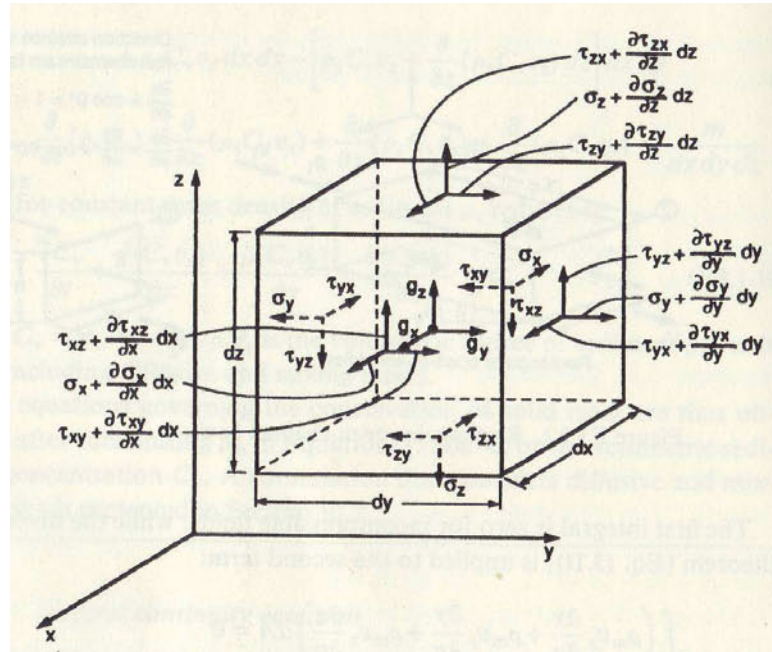


Figure 2.26 Schematic Sketch of Surface Stresses (from Julien 1998)

#### 2.3.4.1 Wahl (2000)

To calculate six components of Reynolds shear stress, an ADV (Acoustic Doppler Velocity) meter was used in this study. The representative flow data from ADV are COV (Covariance) because they are directly used to obtain Reynolds shear

stress. As shown in Figure 2.27, flow velocity is not always identical with the averaged flow velocity due to the turbulence in the flow. The basic concept of covariance in this study is the correlation of two components of flow velocity out of three flow velocity components;  $V_x$ ,  $V_y$  and  $V_z$ .

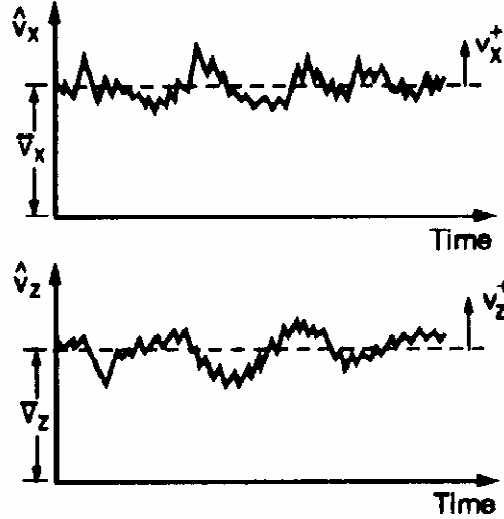


Figure 2.27 The Description of Turbulence in Flow (from Julien 1998)

Equation 2.23 through Equation 2.28 that was cited from Wahl (1996) show the calculation method of Reynolds shear stress using ADV data.

$$\tau_{xy} = \tau_{yx} = -\rho \times (COV - XY) \quad \text{Equation 2.23}$$

Where,  $\tau_{xy}$  = the turbulent shear stress that applies along the y axis and caused by flow velocity fluctuation in the direction of x-axis (ML-1T-2).

$\rho$  = the mass density of water (ML<sup>-3</sup>).

COV-XY is the covariance of two variables ( $V_x$  and  $V_y$ ). It can be computed by using Equation 2.24.

$$\text{COV-XY} = \frac{\sum V_x V_y}{n-1} - \frac{\sum V_x \sum V_y}{n(n-1)} \quad \text{Equation 2.24}$$

Where,  $V_x$  = the flow velocity along x-axis ( $LT^{-1}$ );

$V_y$  = the flow velocity along y-axis ( $LT^{-1}$ );

$n$  = the number of samples that collected velocity data (Dimensionless).

$\tau_{zx}$  is the turbulent shear stress that applies along the x axis and caused by flow velocity fluctuation in the direction of z-axis ( $ML^{-1}T^{-2}$ ).

$$\tau_{zx} = \tau_{xz} = -\rho \times (COV - XZ) \quad \text{Equation 2.25}$$

Where,  $\rho$  = the mass density of water ( $ML^{-3}$ ).

COV-XZ is the covariance of two variables ( $V_x$  and  $V_z$ ). Covariance of two variables ( $V_x$  and  $V_z$ ) is computed by Equation 2.26.

$$\text{COV-ZX} = \frac{\sum V_z V_x}{n-1} - \frac{\sum V_z \sum V_x}{n(n-1)} \quad \text{Equation 2.26}$$

Where,  $V_x$  = the flow velocity along x-axis ( $LT^{-1}$ ).

$V_z$  = the flow velocity along z-axis ( $LT^{-1}$ ).

$n$  = the number of samples that collected velocity data (Dimensionless).

$\tau_{zy}$  is the turbulent shear stress that applies along the y axis and caused by flow velocity fluctuation in the direction of z-axis ( $ML^{-1}T^{-2}$ ).

$$\tau_{yz} = \tau_{zy} = -\rho \times (COV - YZ) \quad \text{Equation 2.27}$$

Where,  $\rho$  = the mass density of water ( $ML^{-3}$ ).

COV-YZ is the covariance of two variables ( $V_z$  and  $V_y$ ). It can be obtained using Equation 2.28.

$$\text{COV-YZ} = \frac{\sum V_y V_z}{n-1} - \frac{\sum V_y \sum V_z}{n(n-1)} \quad \text{Equation 2.28}$$

Where,  $V_y$  = the flow velocity along y-axis ( $LT^{-1}$ ).

$V_z$  = the flow velocity along z-axis ( $LT^{-1}$ ).

$n$  = the number of samples that collected velocity data (Dimensionless).

#### 2.3.4.2 Baird (2004)

Baird (2004) suggested linear extrapolation of Reynolds shear stress profile to obtain bed shear stress using ADV data. An example of Reynolds shear stress profile is presented in Figure 2.17. Due to the existence of roughness sublayer, Reynolds shear stress decreases to the near bed area just after a maximum value of Reynolds shear stress (Raupach (1991); Nikora and Gohring (2000)). As a result, Montes (1998) suggested linear extrapolation of the linear portion of Reynolds shear stress profile as a method of bed shear stress calculation. Actually, Baird (2004) stated “Reynolds shear stress can be calculated by extrapolating the slope of the linear portion of the shear stress profile to the bed”. In addition, Montes (1998) explained that finding the point of interception with x axis is zero in Figure 2.28 is a good method of estimation of bed shear stress.

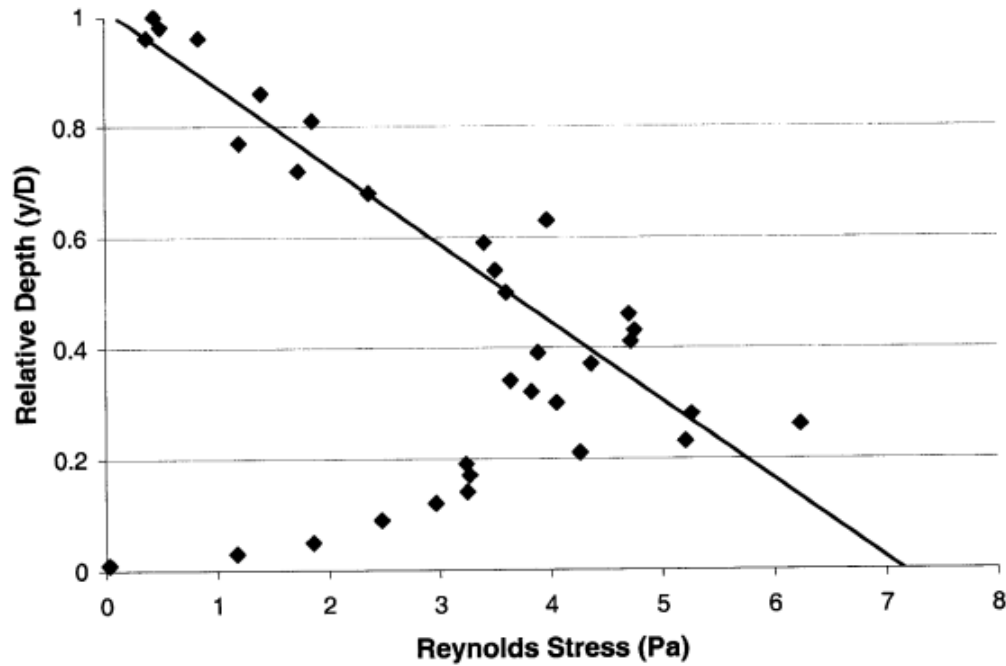


Figure 2.28 Reynolds Shear stress Profile (from Baird (2004))

Baird (2004) rearranged Equation 2.29 (cited from Muste and Patel, 1997; Montes, 1998) into Equation 2.30 to obtain the linear regression equation from the linear portion of the Reynolds Shear stress profile that was presented in Figure 2.28.

$$\frac{\tau}{\rho} = -u'v' = u_*^2 \left( 1 - \frac{y}{D} \right) \quad \text{Equation 2.29}$$

Where,  $\tau$  = the shear stress ( $\text{ML}^{-1}\text{T}^{-2}$ );

$\rho$  = the mass density of water ( $\text{ML}^{-3}$ );

$u'$  = the instantaneous velocity fluctuations about the mean in the longitudinal direction ( $\text{LT}^{-1}$ ); and

$v'$  = the instantaneous velocity fluctuations about the mean in the vertical direction ( $\text{LT}^{-1}$ ).

$$\frac{y}{D} = m \times (\tau) + b \quad \text{Equation 2.30}$$

Where,  $\frac{y}{D}$  = relative depth (Dimensionless);

$\tau$  = the shear stress that equals to  $-\rho \bar{u'v'}$  at depth  $\frac{y}{D}$  ( $\text{ML}^{-1}\text{T}^{-2}$ );

$m$  = the regression slope of linear regression equation; and

$b$  = the intercept of the regression line.

## 2.4 Summary

Numerous researchers have performed studies to quantify shear stress distribution in meandering channels. Mathematical modeling and laboratory experiments have been implemented for the validation of theories. To understand the mechanism of shear stress distribution in meandering channels, the understanding of background of flow in a bend is necessary. At the beginning of this chapter, the basic mechanism of flow in meandering channels was introduced; the parameters to determine meandering channel geometry, stream morphology, concept of secondary flow in bend, the effect of superelevation, and Lane's balance to explain the dynamic equilibrium in a stream system. In Section 2.3.1 through Section 2.3.4, the methods of shear stress calculation were introduced for data analysis of the study. The calculation methods are; Preston tube, linear regression of velocity profile, Rozovski's method and extrapolation of Reynolds shear stress by using ADV data.

## **3 Data Analysis**

### **3.1 Introduction**

Data analysis was conducted to determine the distribution of shear stress. Measurements of flow velocity, flow depth, and boundary shear stress were performed during the data collection procedure. In accordance with the procedure presented in Section 2.3, four methods were used for the data analysis: a) Preston tube, b) Logarithmic Velocity Profile, c) Rozovskii method, and d) Reynolds shear stress. In this chapter, the shear stress calculation results and the value of differences between each shear stress calculation method are presented.

### **3.2 Shear Stress Calculation Results**

Four calculation methods were used for data analysis. Entering and exiting flow in the model will result in overestimation of shear stress. As result, shear stress data of cross sections 1 through 3 and cross section 18 were excluded from analysis. Preston tube method is the shear stress calculation using a pitot tube. Logarithmic Velocity Profile is the technique of shear stress calculation by obtaining a linear regression after plotting the relationship between flow depth and logarithmic flow velocity profile. Rozovskii's method was derived from the equation of motion in Cartesian coordinates. Reynolds shear stress is calculated from ADV data based on the covariance of two variables of flow velocity. The two variables originated from two of three flow velocity components:  $V_x$ ,  $V_y$  and  $V_z$ . In this section, the results and discussion of the data analysis for the four different shear stress calculation methods are presented.

### 3.2.1 Preston Tube

Preston tube calibration was conducted by Sclafani (2008) in a flume. Boundary shear stress in the x direction,  $\tau_x$ , was computed by converting Preston differential pressure data (inch of head) into shear stress (psf) using the Preston tube calibration that was exhibited as Equation 2.13. The shear stress distribution calculations from the Preston tube method are presented in Figure 3.1 through Figure 3.4. The range of  $\tau_x$  values by Preston tube were between 0.0075 psf and 0.072 psf. Clearly, the area with a higher value of  $\tau_x$  was located at the inner side of the downstream bend of the channel. Also, proportionality of the  $\tau_x$  value with increasing flow rate was observed except for the case of 16 cfs. With the increases of constant rate, the measured data consistently moved into a higher level of  $\tau_x$  values.

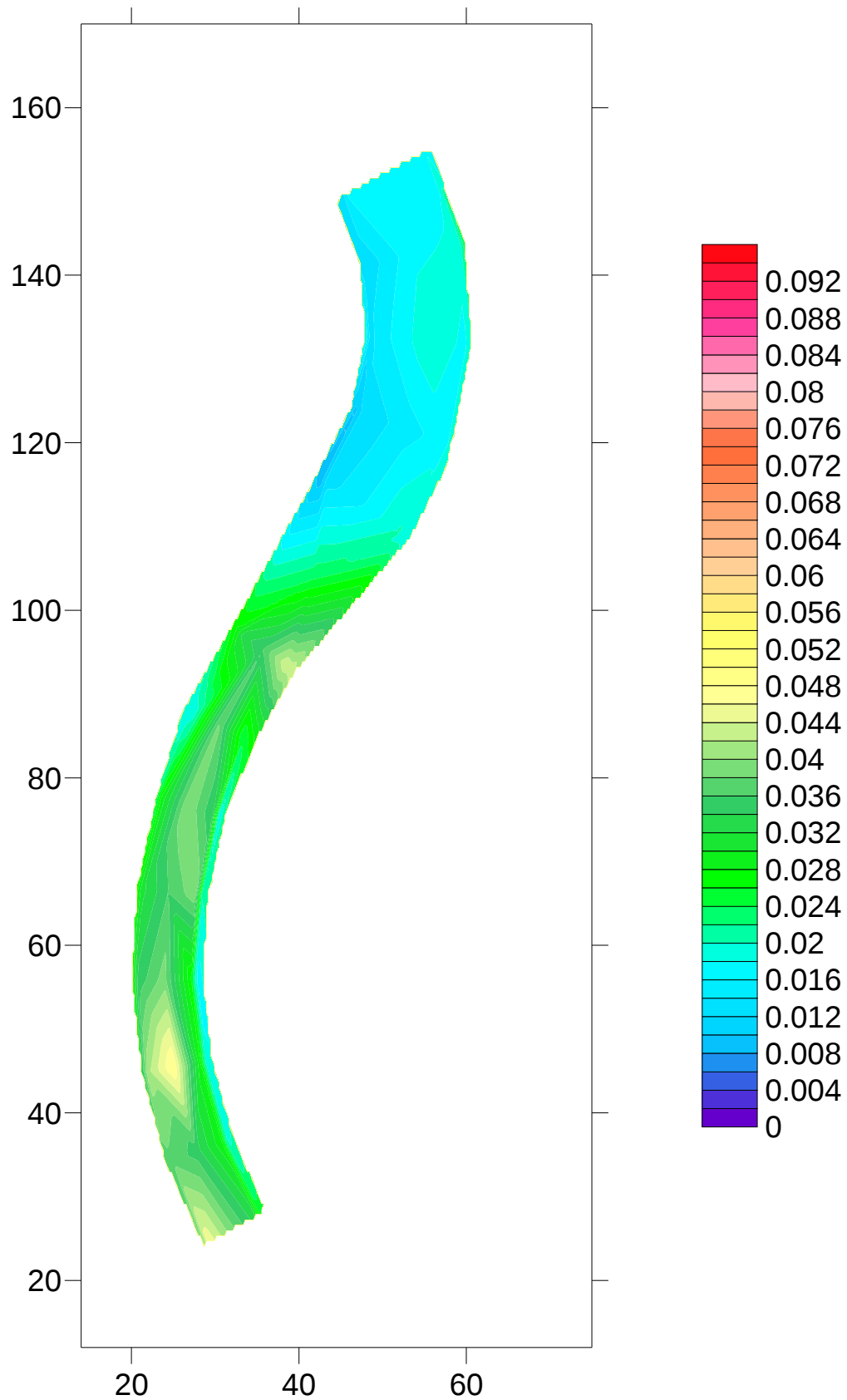


Figure 3.1 Shear Stress Distribution,  $\tau_{xy}$ , from Preston Tube for 8 cfs (psf)

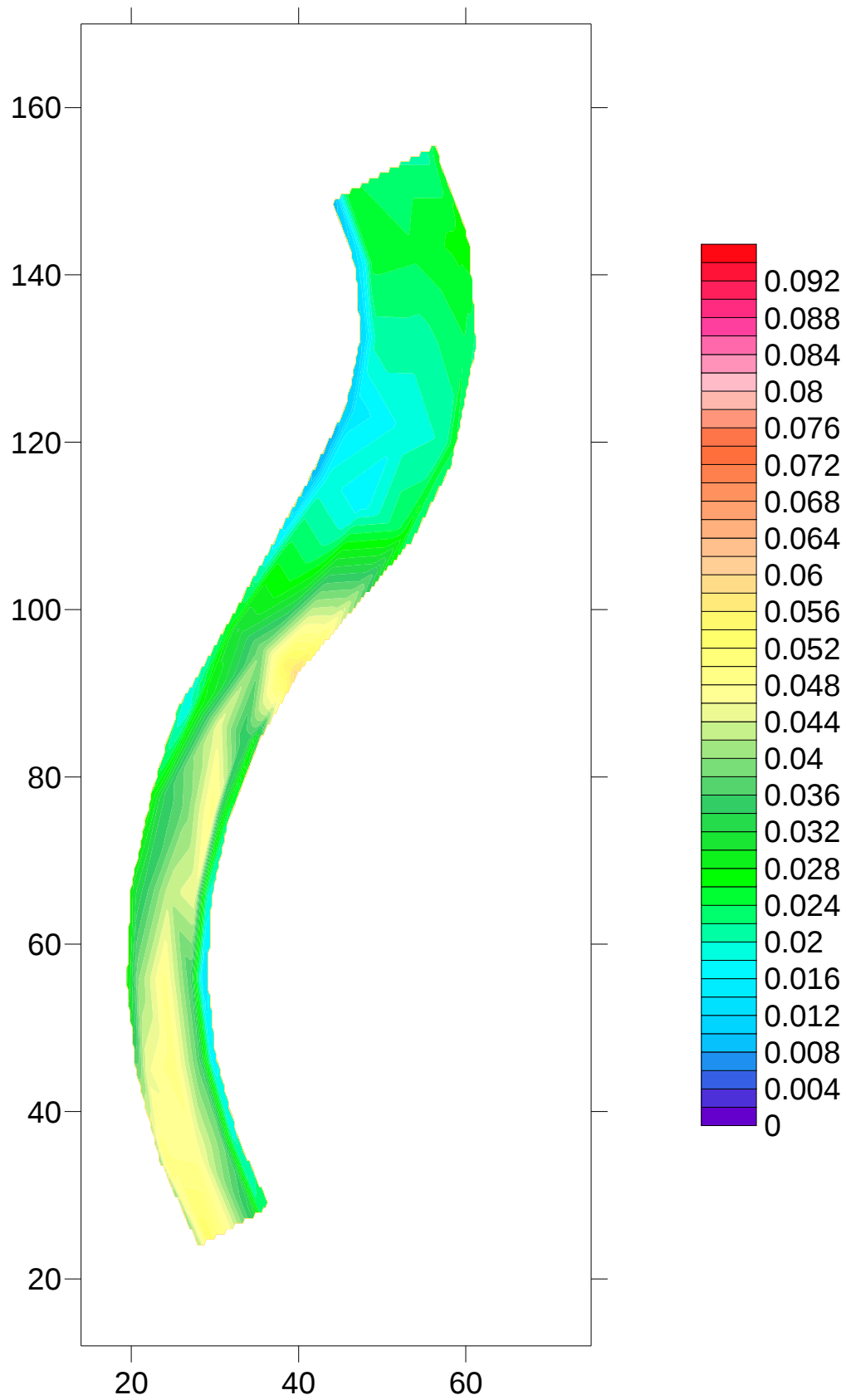


Figure 3.2 Shear Stress Distribution,  $\tau_x$ , from Preston Tube for 12 cfs (psf)

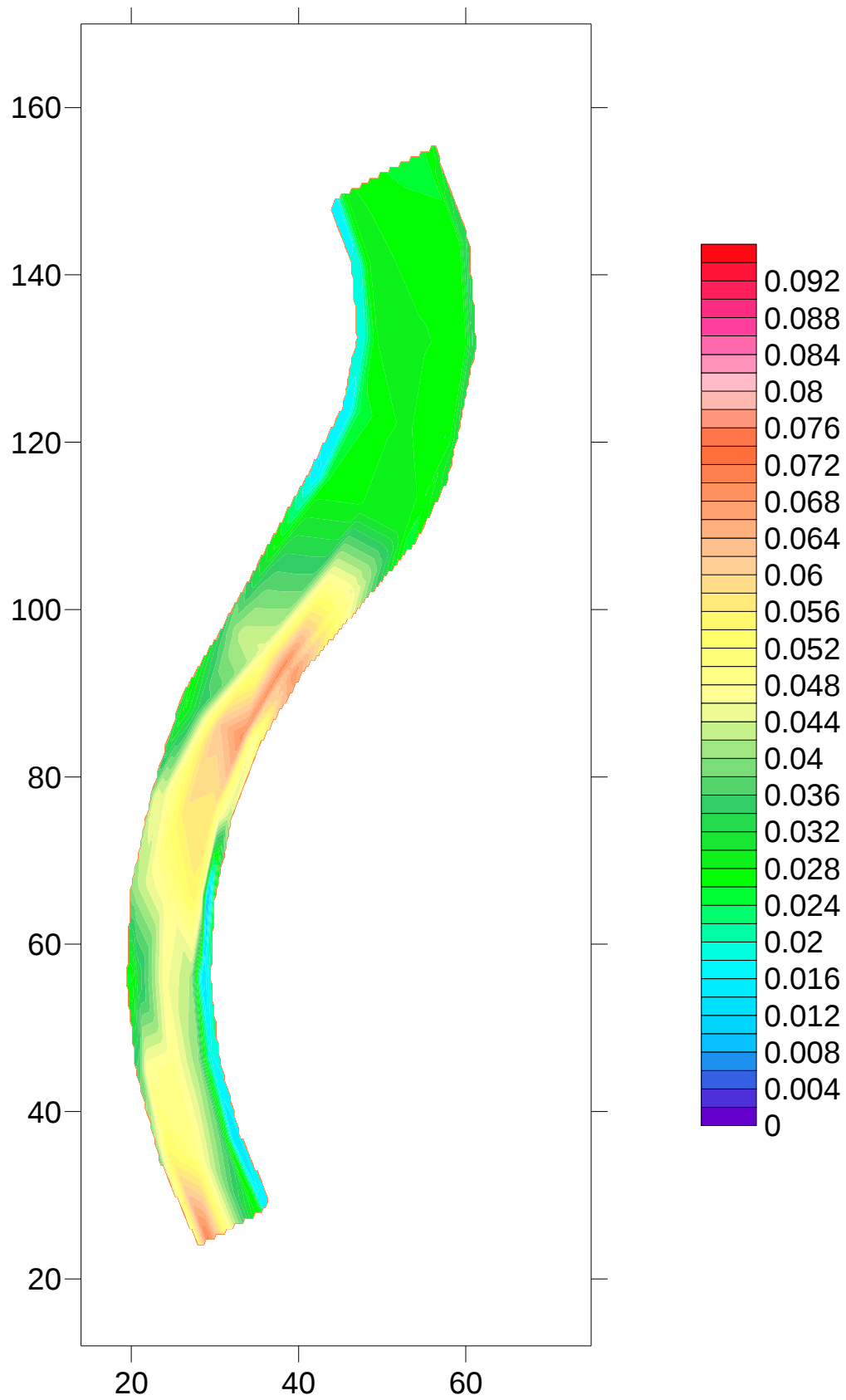


Figure 3.3 Shear Stress Distribution,  $\tau_x$ , from Preston Tube for 16 cfs (psf)

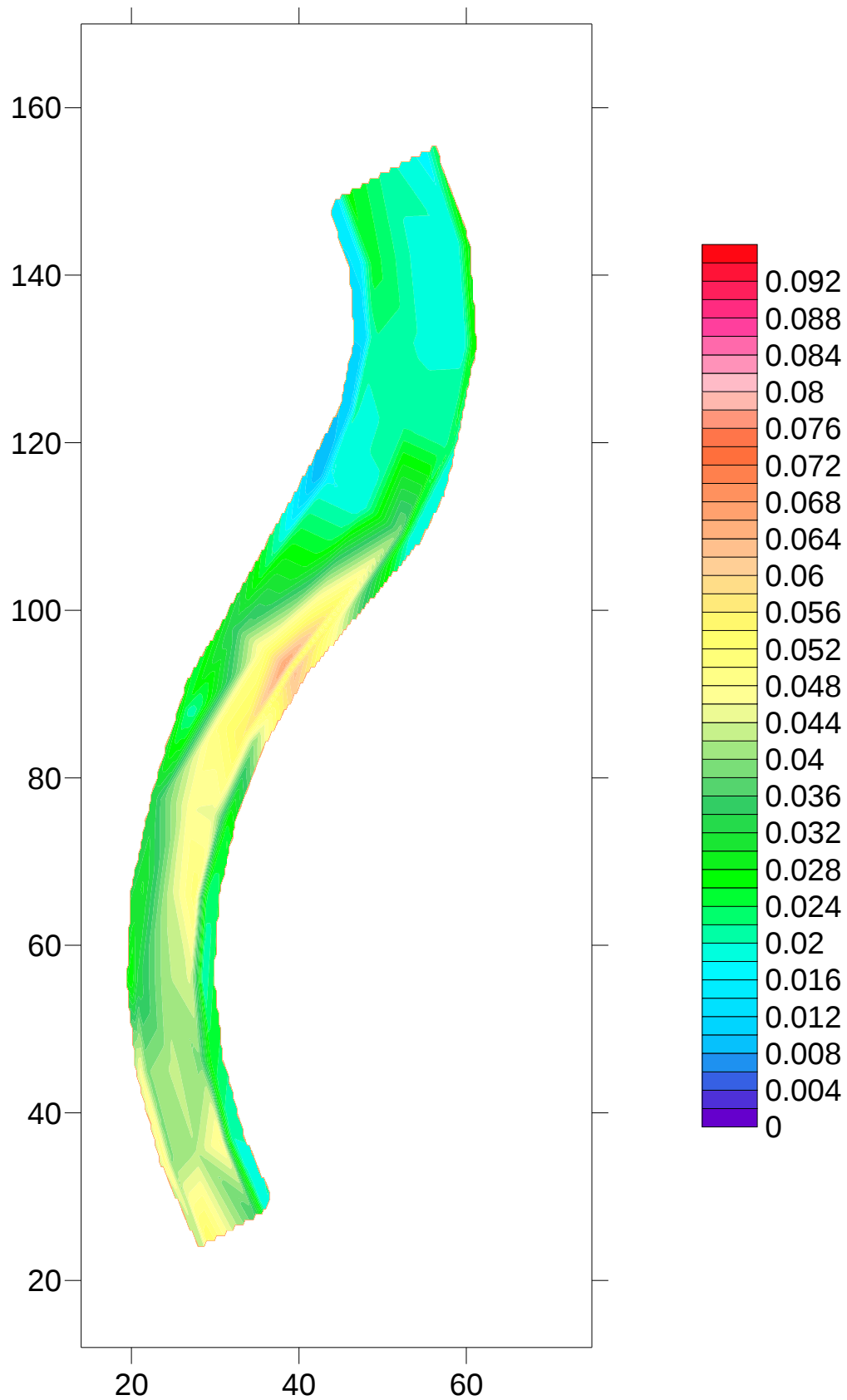


Figure 3.4 Shear Stress Distribution,  $\tau_x$ , from Preston Tube for 20 cfs (psf)

### 3.2.2 Linear Regression of Flow Velocity Profile

Equation 2.17 through Equation 2.20 describes the method of linear regression of flow velocity profile. Ideally, the  $\tau_x$  value that was obtained from this method is identical with the value of  $\tau_x$  by Preston tube. Figure 3.5 presents the distribution of turbulent shear stress,  $\tau_x$  for 20 cfs. The value of  $\tau_x$  ranged between 0 psf and 0.076 psf. Just as in the case of  $\tau_x$  by Preston tube, a higher value of  $\tau_x$  was observed at the inside of the downstream bend of the channel. Proportionality of flow rate and shear stress also was observed. In addition, lateral shear stress,  $\tau_y$  was calculated using same method to obtain  $\tau_x$ . The result is presented in Figure 3.6. The shear stress distribution for 8, 12 and 16 cfs is presented in Appendix C.

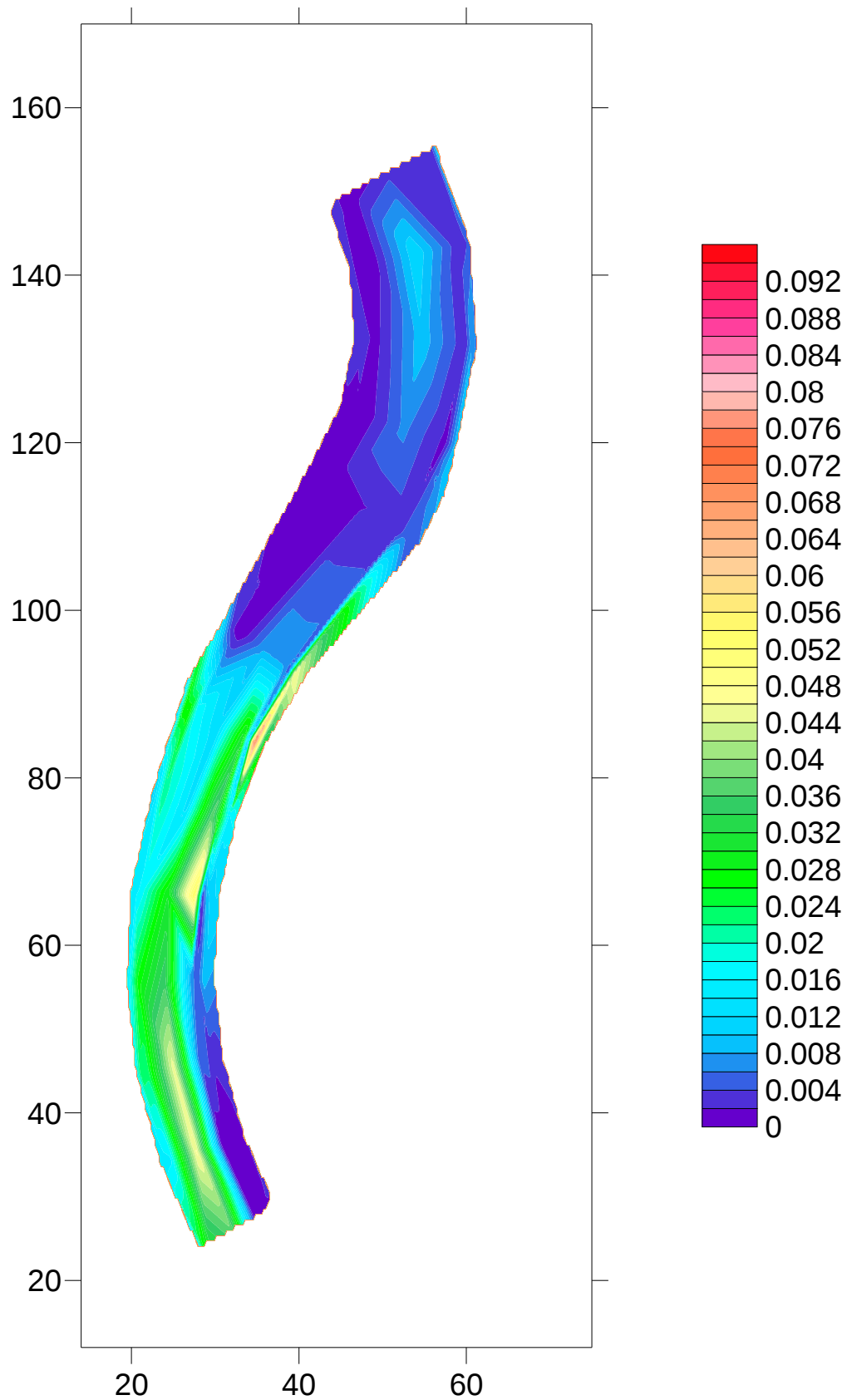


Figure 3.5 Shear Stress Distribution,  $\tau_x$ , by Linear Regression for 20 cfs (psf)

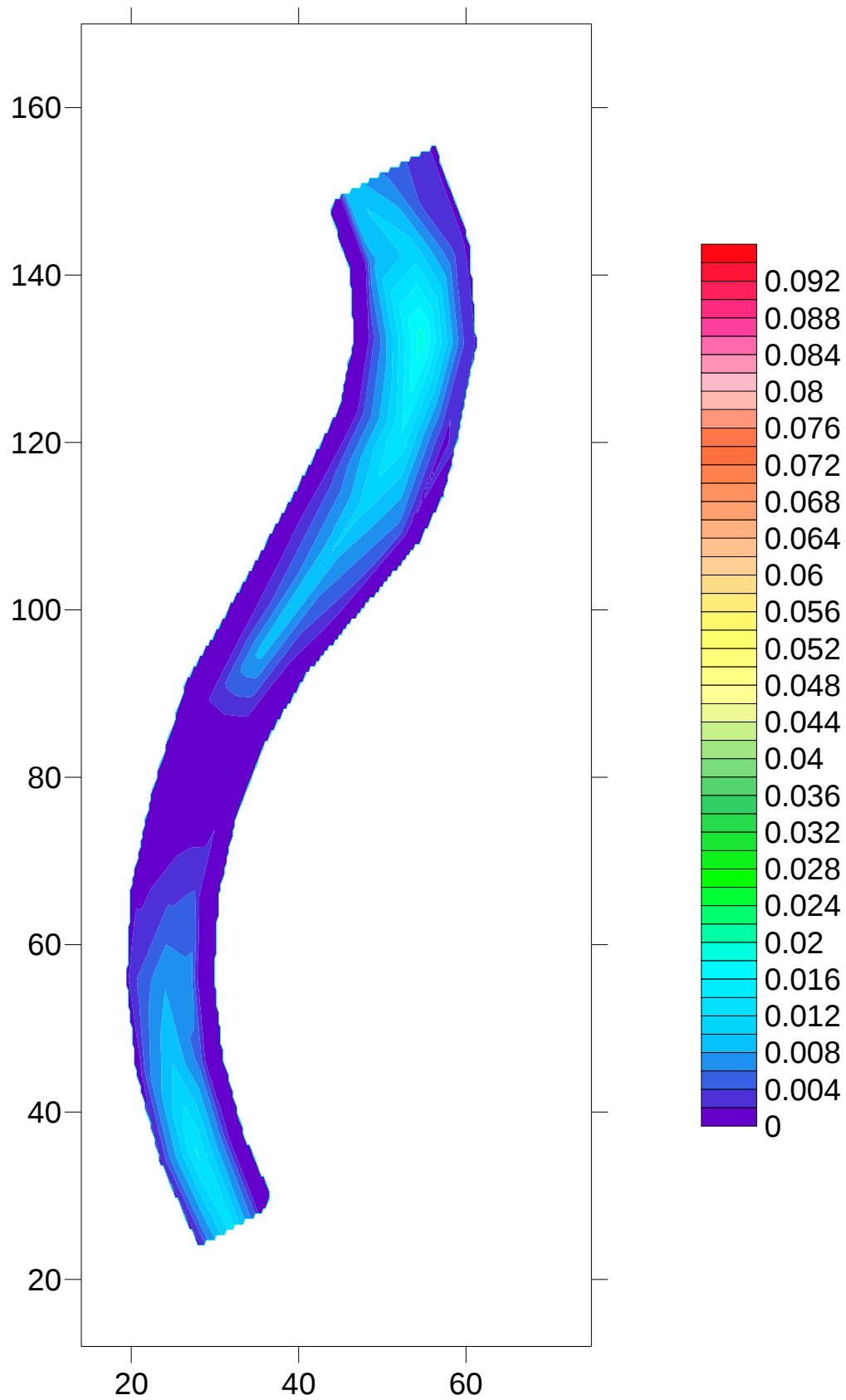


Figure 3.6 Shear Stress Distribution,  $\tau_y$ , by Linear Regression for 20 cfs (psf)

### 3.2.3 Rozovskii Method

The shear stress calculation method presented by Rozovskii (1961) computes the radial shear stress in a meandering channel,  $\tau_r$  by using Equation 2.22. A detailed calculation procedure for the water surface slope,  $S_r$ , and the second bracket in the right hand side of Equation 2.22 is presented in this section. The water surface slope can be expressed by Equation 3.1:

$$S_r = \frac{h}{D} \quad \text{Equation 3.1}$$

Where,  $S_r$  = water surface slope (L/L);

$h$  = difference of water surface elevation between piezo a and g (L);

$D$  = horizontal distance of piezo between piezo a and piezo g (L).

Equation 4.2 shows the detailed calculation method for the distance between piezometer a and piezometer g. The multiplying factor of 3 comes from the 3:1 (Horizontal: Vertical) side slope of the trapezoidal channel. Equation 3.2 is presented below;

$$D = d_1 + d_2 + d_3 \quad \text{Equation 3.2}$$

Where,  $D$  = Horizontal distance between Piezo a and Piezo g (L);

$d_1$  = 3 times of the difference of height of Piezo a and d (L);

$d_2$  = Channel bottom width (L); and  $d_3$  is 3 times of the difference of height of Piezo g and d (L).

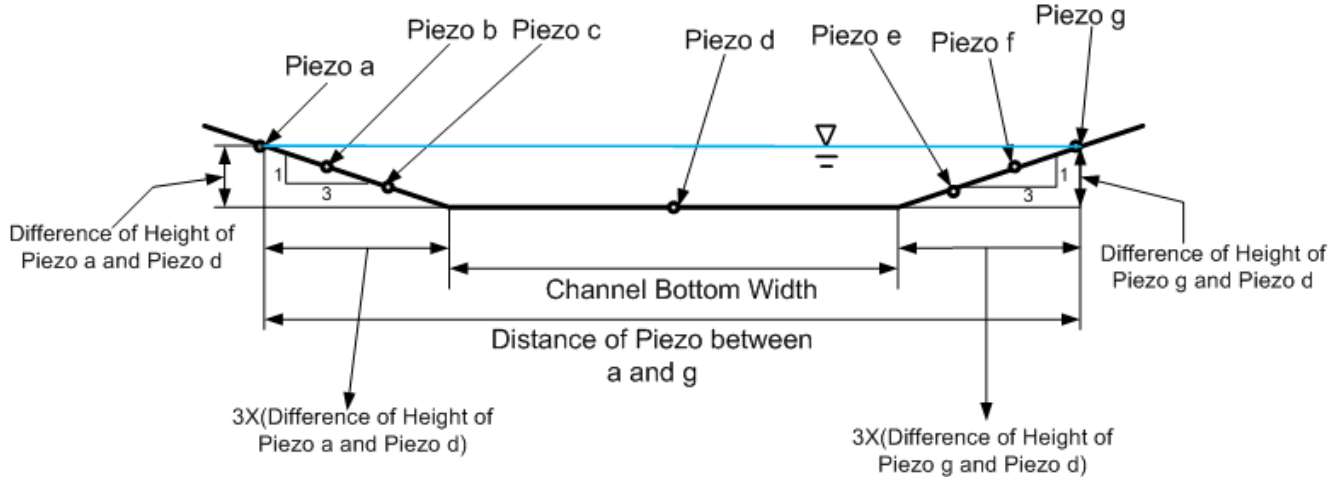


Figure 3.7 Schematic Sketch of Distance between Piezo a and Piezo g

For the calculation of the second bracket in the right-hand-side of Equation 2.22, a manual integration method was used. Figure 3.8 illustrates the idealized flow

velocity profile. The term  $\int_0^H \frac{v_{\theta}^2}{r} dz$  can be described by Equation 3.3;

$$\frac{1}{r} \left\{ \left( \frac{v_1 + v_o}{2} \right)^2 (z_1 - z_{Bed}) + \dots + \left( \frac{v_n + v_{n+1}}{2} \right)^2 \times (z_{n+1} - z_n) + v_n^2 \times (z_{WSE} - z_n) \right\} \quad \text{Equation 3.3}$$

Where,  $v_1$  = flow velocity value that locates in the lowest data collection point (L/T);

$v_2$  = flow velocity value that locates just above of the location of  $v_1$  (L/T);

$v_n$  = flow velocity value that locates in the highest point (L/T);

$z_{Bed}$  = bed elevation of the Channel; and  $\Delta Z$  is differential flow depth (L).

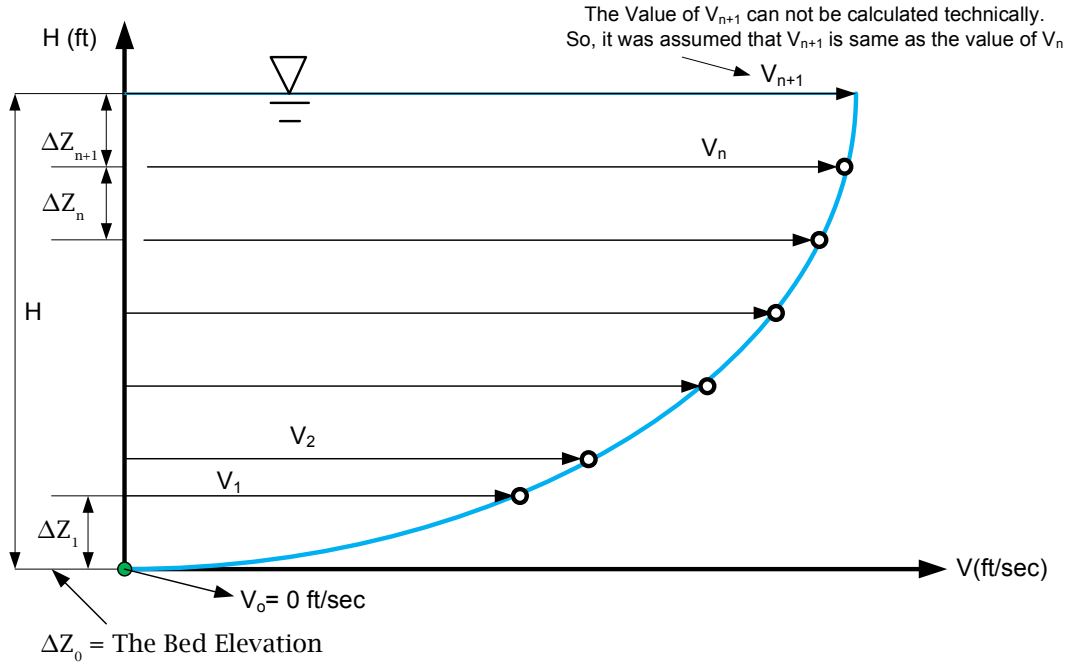


Figure 3.8 Idealized Flow Velocity Profile

The shear stress distribution from the Rozovskii method is presented in Figure 3.9 for 20 cfs. The range of the values of  $\tau_r$  were between -0.048 psf and 0.13 psf. Differently from the method of Preston tube and linear regression of flow velocity profile, shear stress by Rozovskii method did not show proportionality with increase of the flow rate. Also, negative shear stress values were observed: the point of negative shear stress has a less steep water surface slope. That means the  $S_r$  value is the dominant parameter of shear stress from the Rozovskii method. To validate the observation, the water surface slope distribution for each flow rate is presented in Figure 3.10 for 20 cfs. The plots show good agreement between the change of water surface slope and shear stress distribution from Rozovskii.

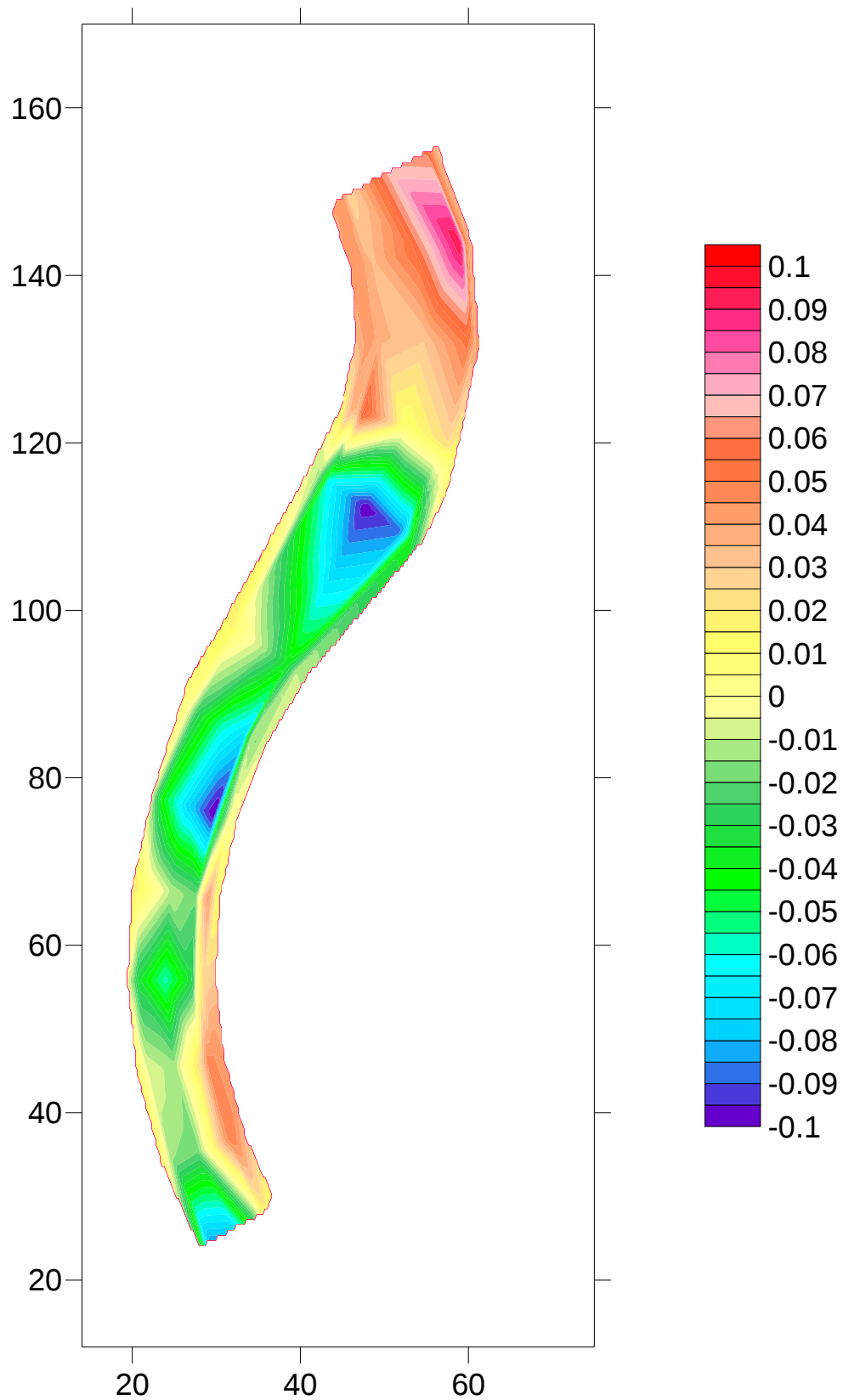


Figure 3.9 Radial Shear Stress Distribution,  $\tau_r$ , from Rozovskii (1961) for 20 cfs (psf)

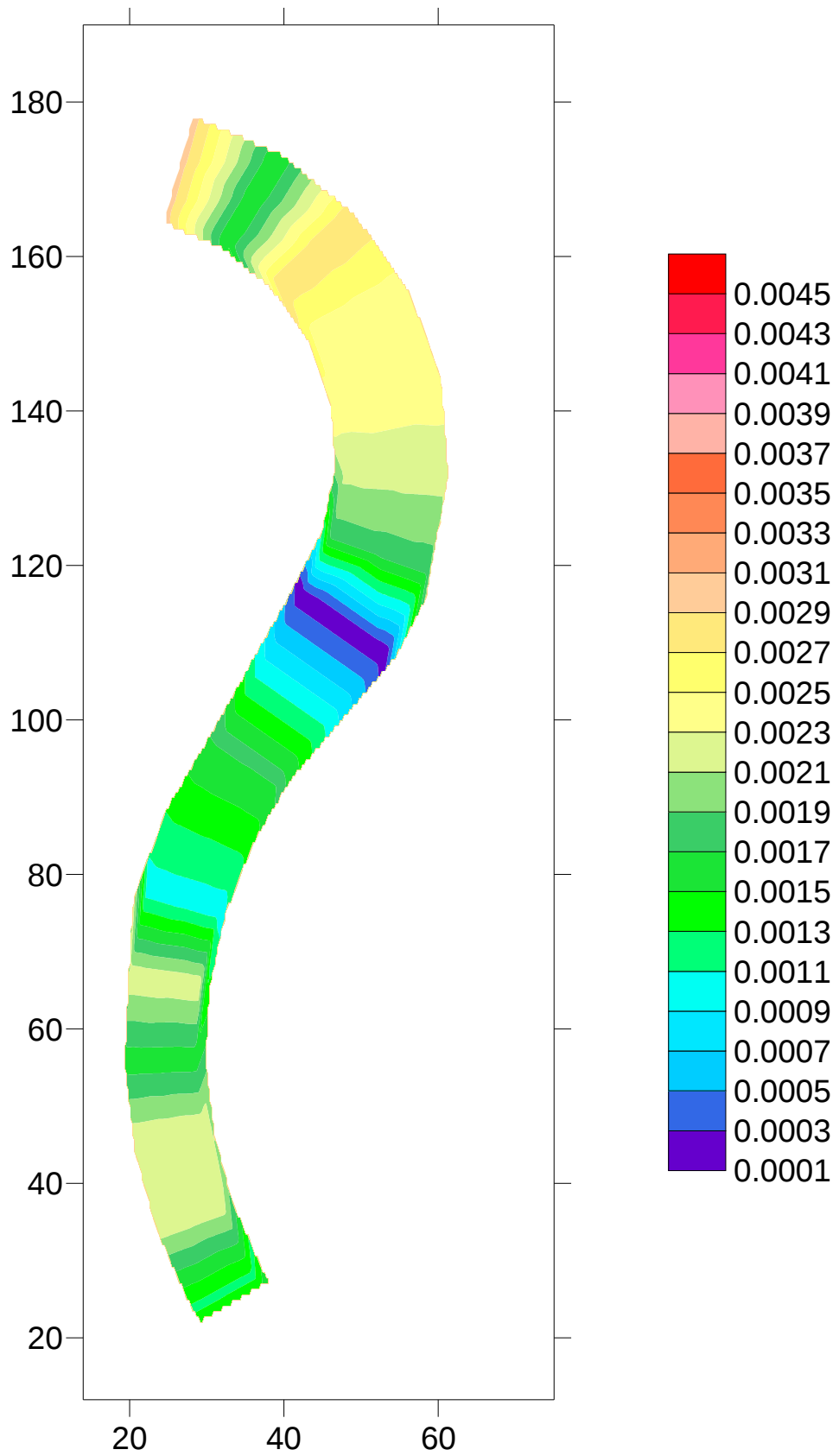


Figure 3.10 Water Surface Slope Distribution for 20 cfs

### 3.2.4 Reynolds Shear Stress

Reynolds shear stress is based on the ADV (Acoustic Doppler Velocity meter) data of each piezometer and each cross section of the model. As suggested by Montes (1998), Reynolds shear stress profile was plotted to take a linear regression of the linear portion of the Reynolds shear stress profile. The x axis of the linear regression equation is Reynolds shear stress and y axis is the relative depth. The non-linear portion of the Reynolds shear stress profile that was shown as pink dots in Figure 3.11 and Figure 3.12 was taken out for the linear regression. In addition, Wahl (2002) explained that when a data point of correlation is below 70 and the signal to noise ratio is below 15 has a high possibility of low accuracy. As a result, ADV data point covariance below 70 and signal to noise ratio below 15 were excluded from the plotting of the Reynolds shear stress profile. Montes (1998) explained the point where the linear regression equation intercepts the x axis is the bed shear stress.  $\tau_{bed}$ , shear stress in the longitudinal direction that applies on the bed of the channel can be computed from Equation 3.4. Summaries of the calculation result from Reynolds shear stress extrapolation are presented in Appendix E.

$$\tau_{bed} = \sqrt{(\tau_{zx})^2 + (\tau_{zy})^2} \quad \text{Equation 3.4}$$

Where,  $\tau_{bed}$  = the turbulent shear stress in longitudinal direction that applies on the bed of the channel ( $M/L^1T^2$ );

$\tau_{zx}$  = the turbulent shear stress that applies in x axis caused by  $V_z$  ( $M/L^1T^2$ ); and

$\tau_{zy}$  = the turbulent shear stress that applies in y axis and caused by  $V_z$  ( $M/L^1T^2$ ).

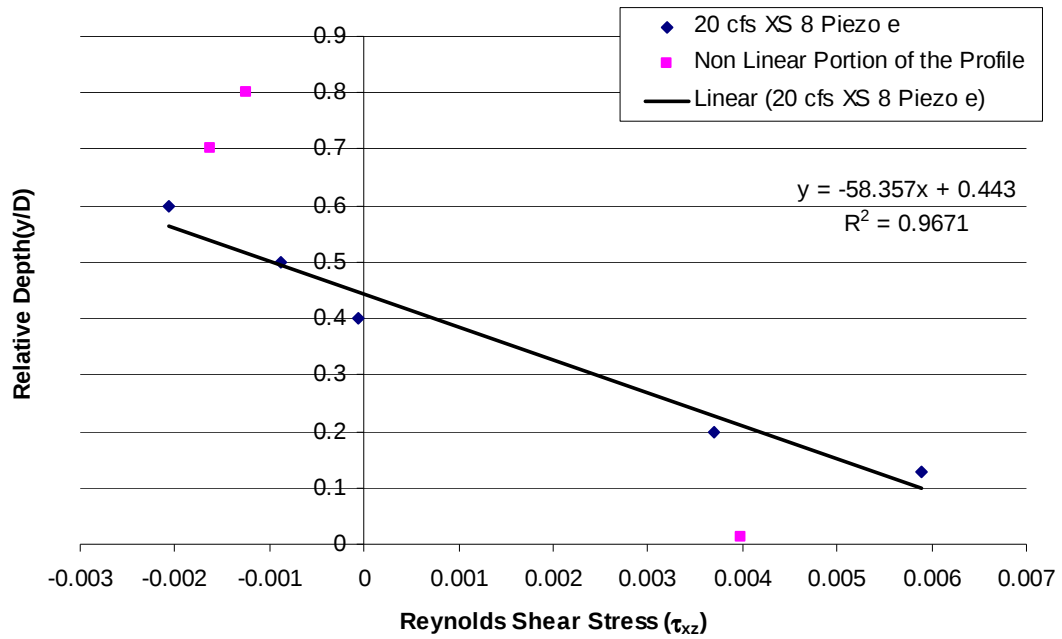


Figure 3.11 Profile of Reynolds Shear Stress of  $\tau_{xz}$  for 20 cfs Cross Section 8 Piezo e

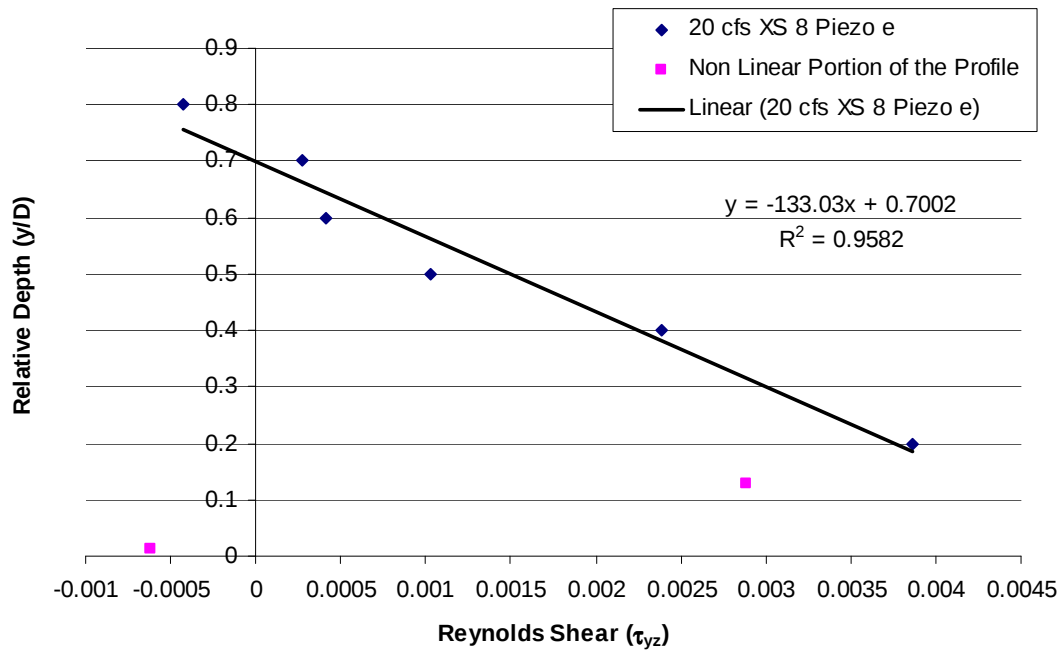


Figure 3.12 Profile of Reynolds Shear Stress of  $\tau_{zy}$  for 20 cfs Cross Section 8 Piezo e

Figure 3.13 through Figure 3.16 present the shear stress distribution for overall flow rate of 8, 12, 16 and 20 cfs. The lowest value of Reynolds shear stress is indicated by a violet color and the highest value of turbulent shear stress is indicated by a red color. The value of  $\tau_{bed}$  ranged from 0.002 psf to 0.058 psf. The location of the maximum value of  $\tau_{bed}$  was observed at the near apex of the downstream bend.

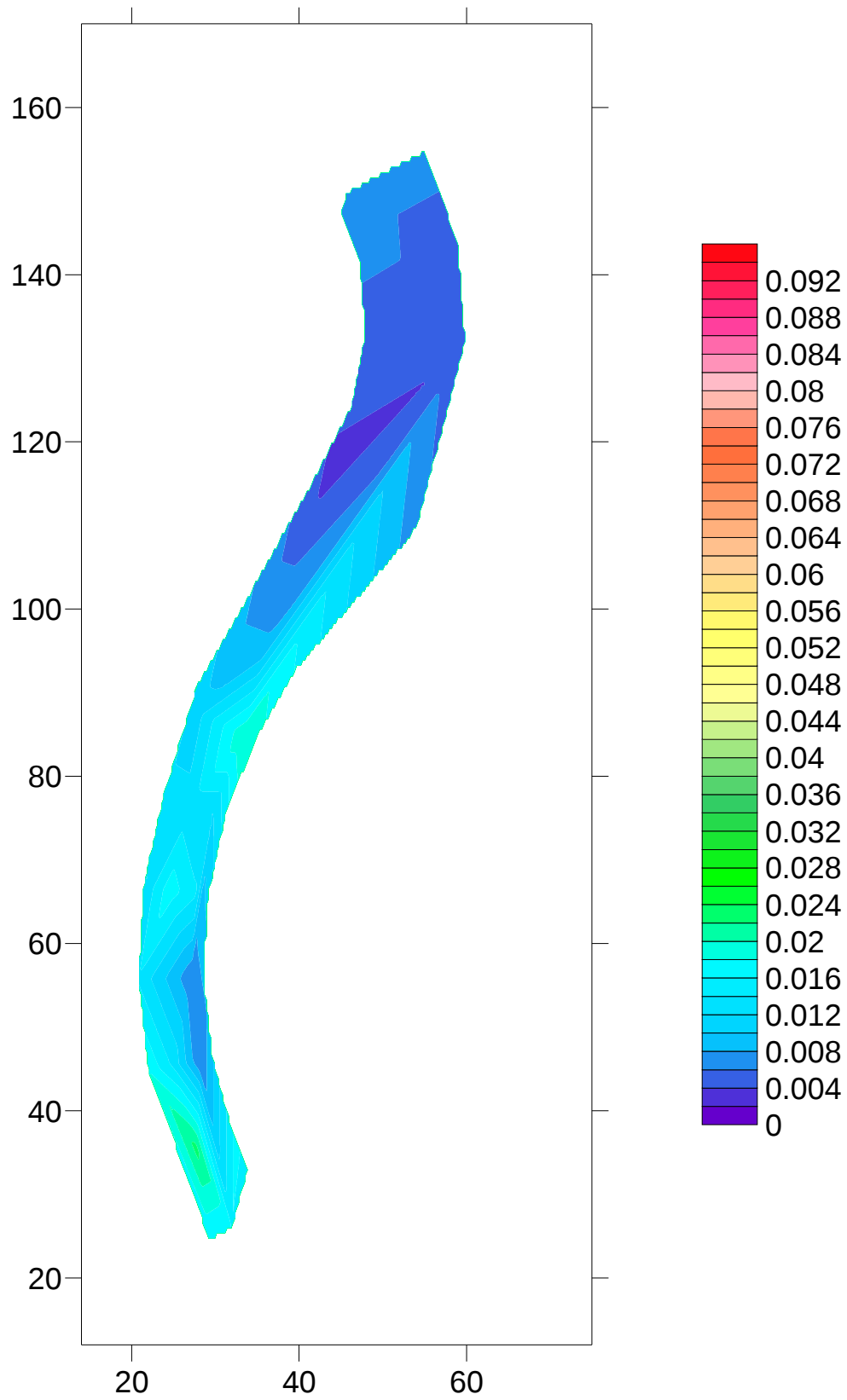


Figure 3.13 Contour Map of  $\tau_{bed}$  from Reynolds Shear Stress for 8 cfs (psf)

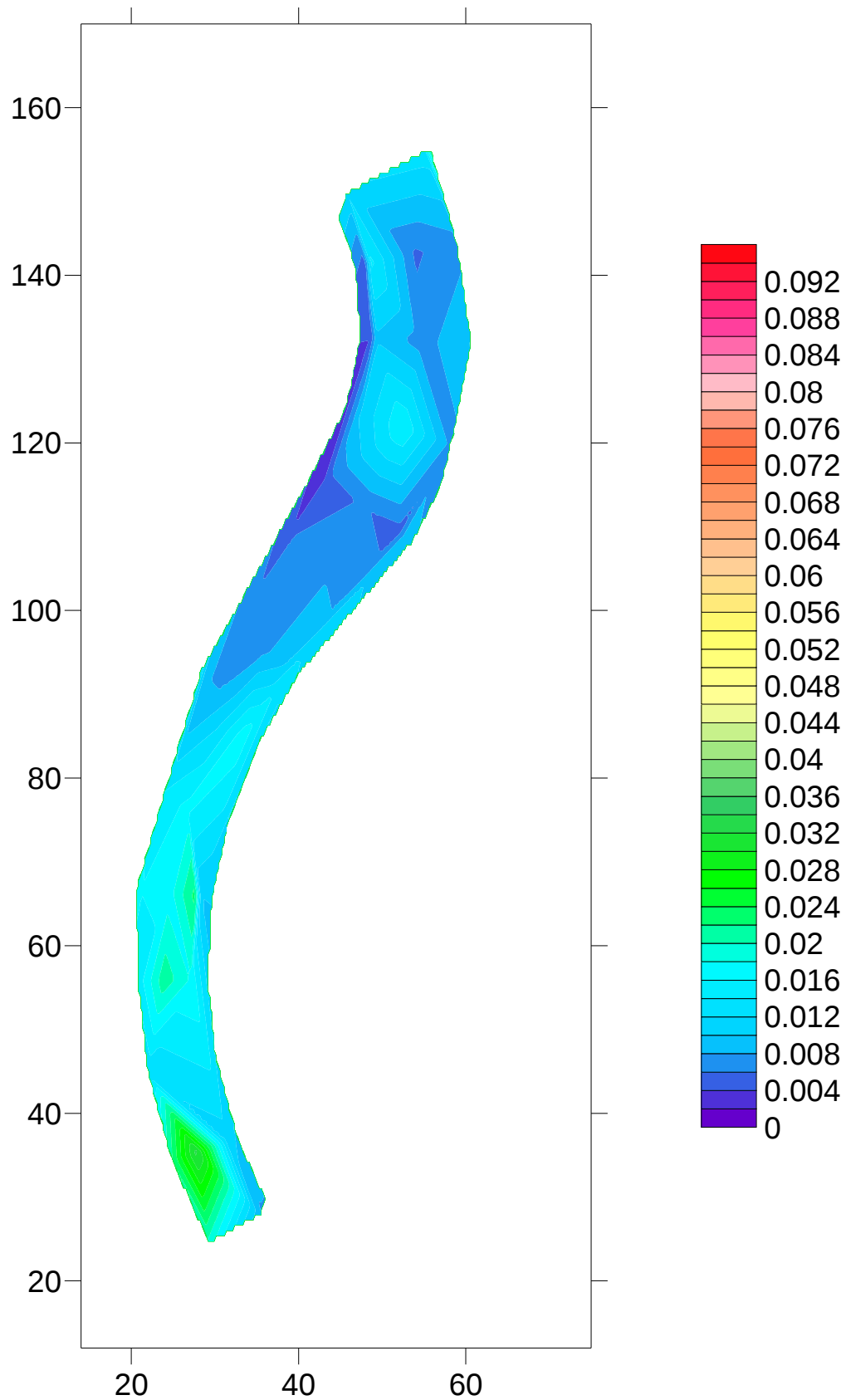


Figure 3.14 Contour Map of  $\tau_{bed}$  from Reynolds Shear Stress for 12 cfs (psf)

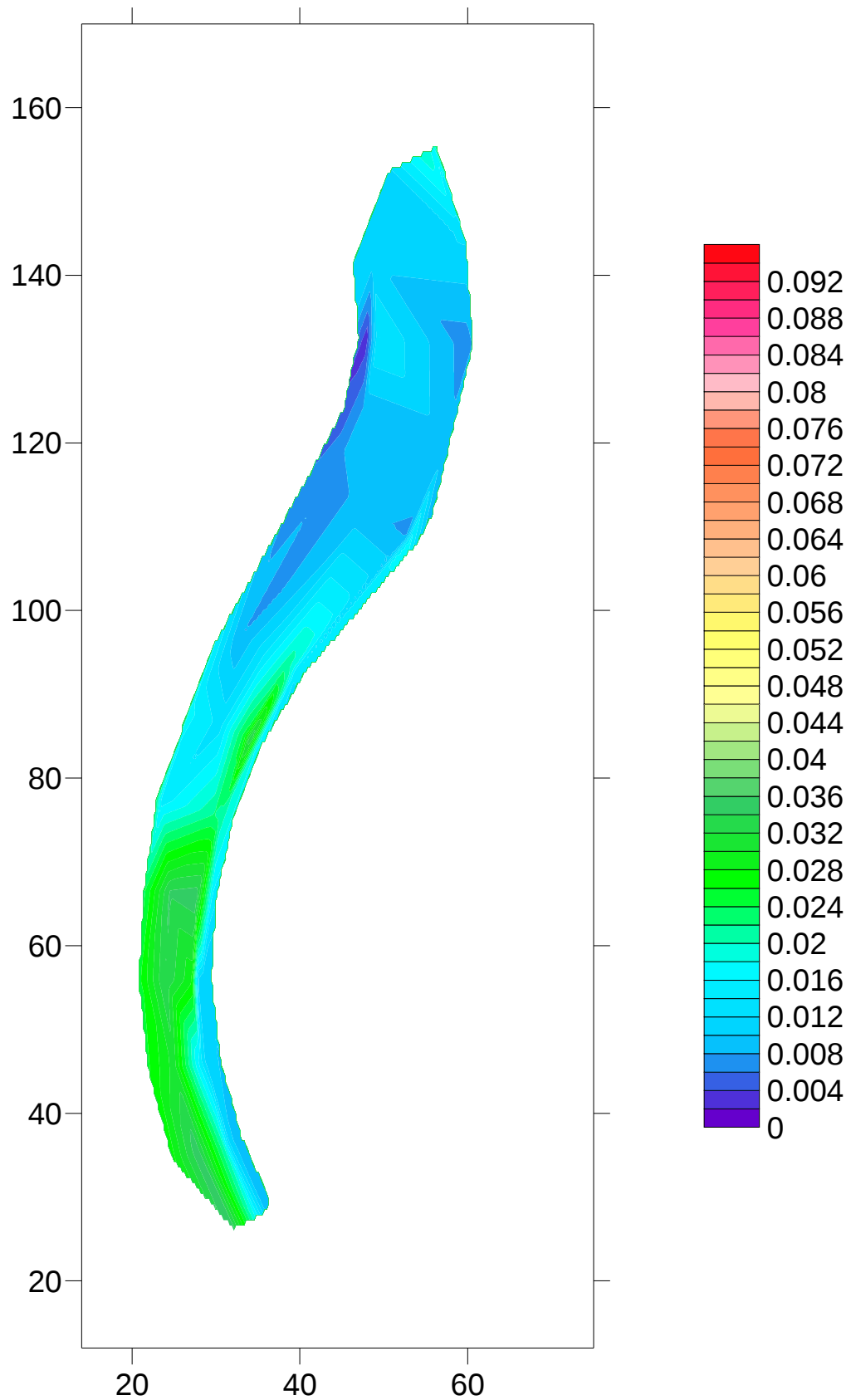


Figure 3.15 Contour Map of  $\tau_{bed}$  from Reynolds Shear Stress for 16 cfs (psf)

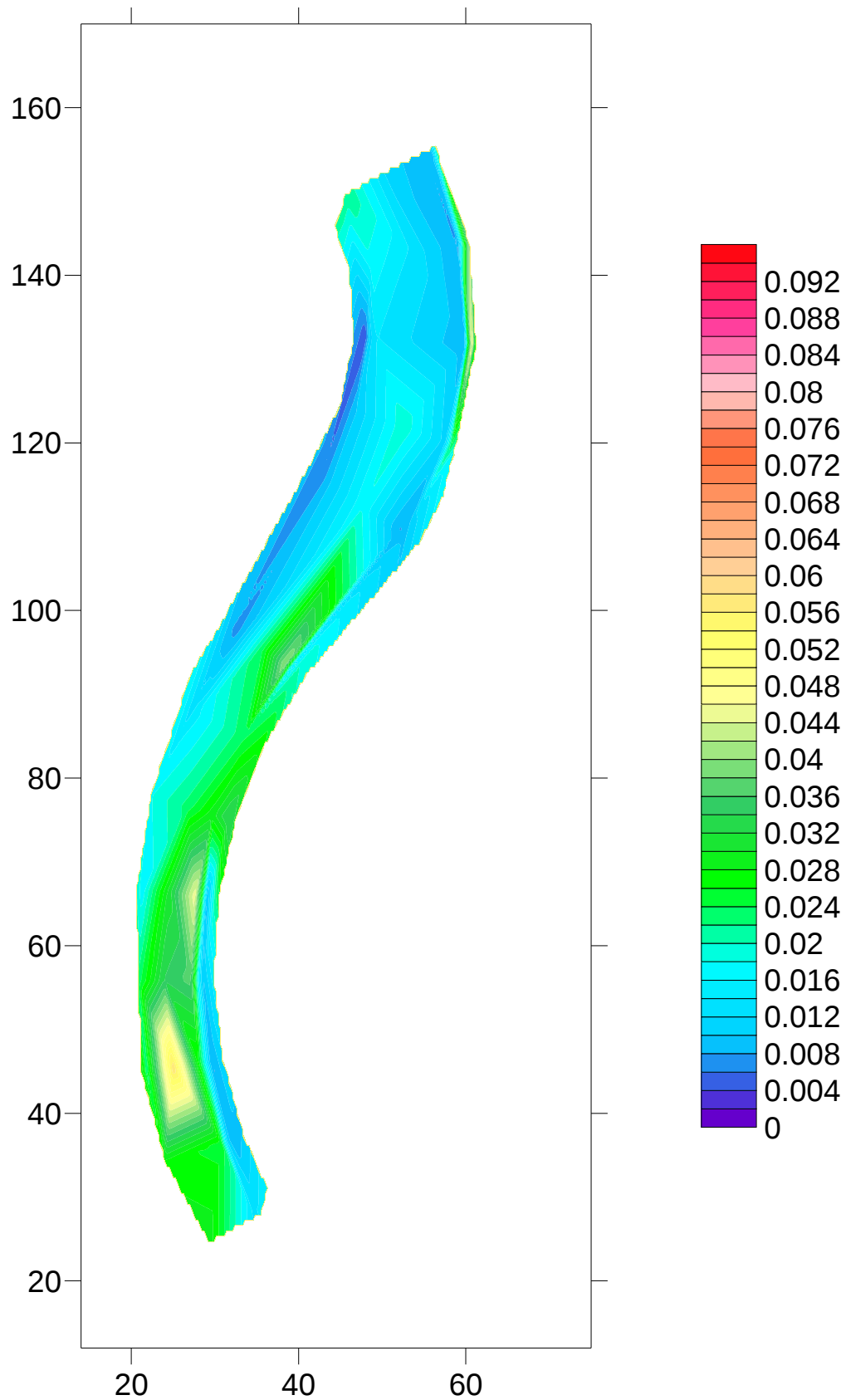


Figure 3.16 Contour Map of  $\tau_{bed}$  from Reynolds Shear Stress for 20 cfs (psf)

### 3.3 Summary

During this study, data analysis was conducted to calculate shear stress by using the following methods; a) Preston tube b) Linear regression of flow velocity profile c) Rozovskii method d) Reynolds shear stress extrapolation. Generally, shear stress from Preston tube showed higher values than any other shear stress from different methods. According to the results of the data analysis, shear stress calculation from Preston tube and Reynolds shear stress extrapolation showed the best agreement because both methods showed proportionality of  $\tau_x$  with the increase of flow rate and showed similar distribution of the value of  $\tau_x$ . Especially, both methods showed that the similar trend of  $\tau_x$  value that indicates reinforced bank protection is required at the inside of the downstream bend in the channel. In addition, the agreements indicated that the flow velocity from the ADV meter is a good parameter for predicting the shear stress distribution.

## 4 Comparisons of Shear Stress Calculation Methods

In Chapter 3, there were differences of shear stress calculation results due to the choice of different shear stress calculation methods. In this chapter, the differences in the shear stress calculations will be described. The method of comparison is presented in Figure 4.1.

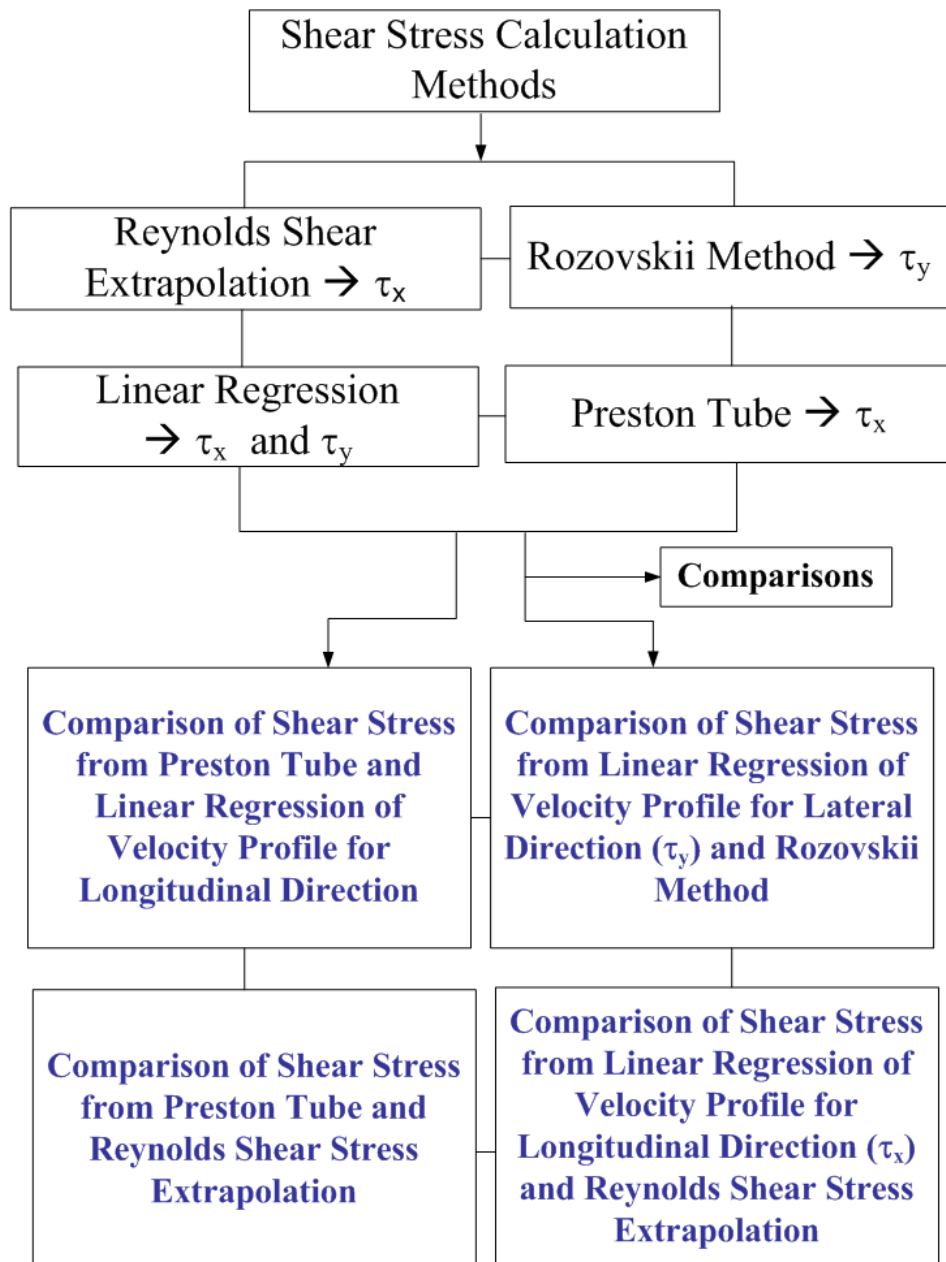


Figure 4.1 Chart of Shear Stress Calculation Methods Comparison

#### **4.1 Comparison of Shear Stress from Preston Tube and Linear Regression of Velocity Profile for Longitudinal Direction**

Plots to observe the difference of the two methods are presented in Figure 4.2 through Figure 4.5. The x-axis is shear stress from linear regression of flow velocity profile and y-axis is shear stress from Preston tube, respectively. If the points perfectly fit the  $y=x$  line, then the two methods have perfect agreement. Figure 4.2 through Figure 4.5 indicate that most of the points are concentrated in the vicinity of the y-axis, which means shear stress calculated from Preston tube is much greater. The green line in the plots indicates the best fit line from different shear stress calculation methods. The most persuasive reason for the difference of the two methods is the difference of measurement method. Preston tube was directly installed on the bed but the ADV can not be located on the bed because the ADV can not recognize the flow velocity on the bed. Therefore, shear stress from a linear regression of the flow velocity profile underestimates bed shear stress. Additionally, the averaged percentage difference of the two methods with change of discharge was presented in Figure 4.6.

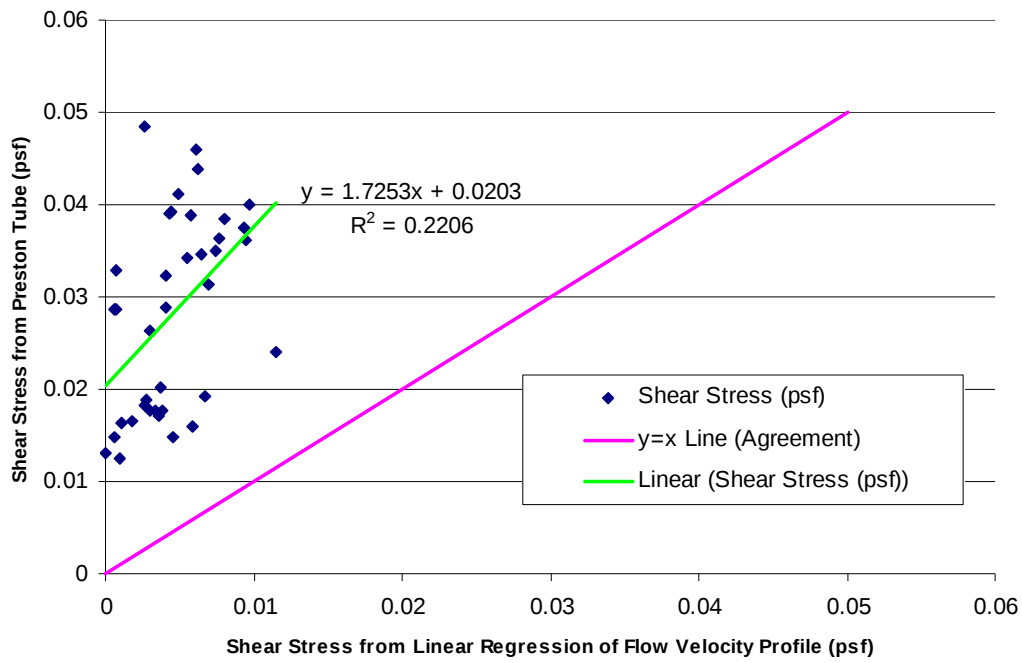


Figure 4.2 Comparison of Shear Stress from Preston Tube and Linear Regression of Flow Velocity Profile for 8 cfs

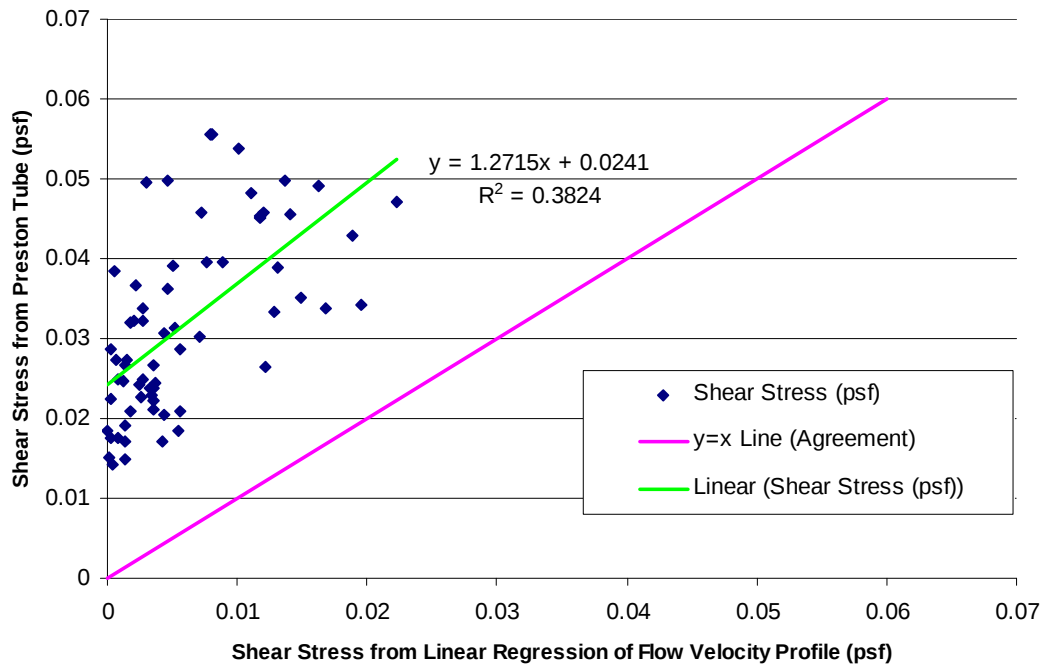


Figure 4.3 Comparison of Shear Stress from Preston Tube and Linear Regression of Flow Velocity Profile for 12 cfs

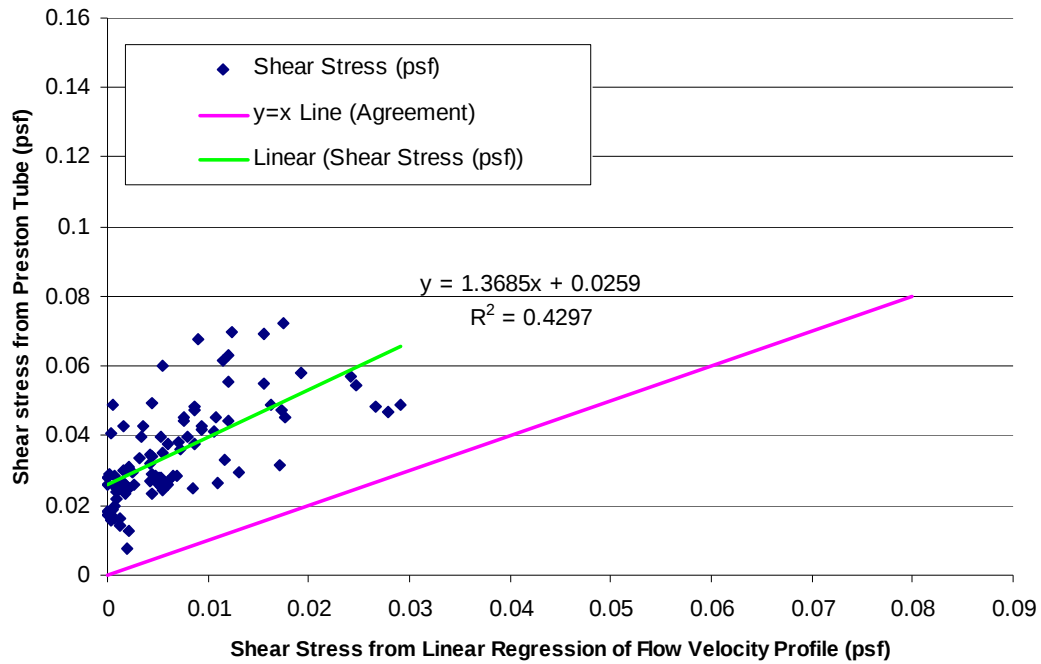


Figure 4.4 Comparison of Shear Stress from Preston Tube and Linear Regression of Flow Velocity Profile for 16 cfs

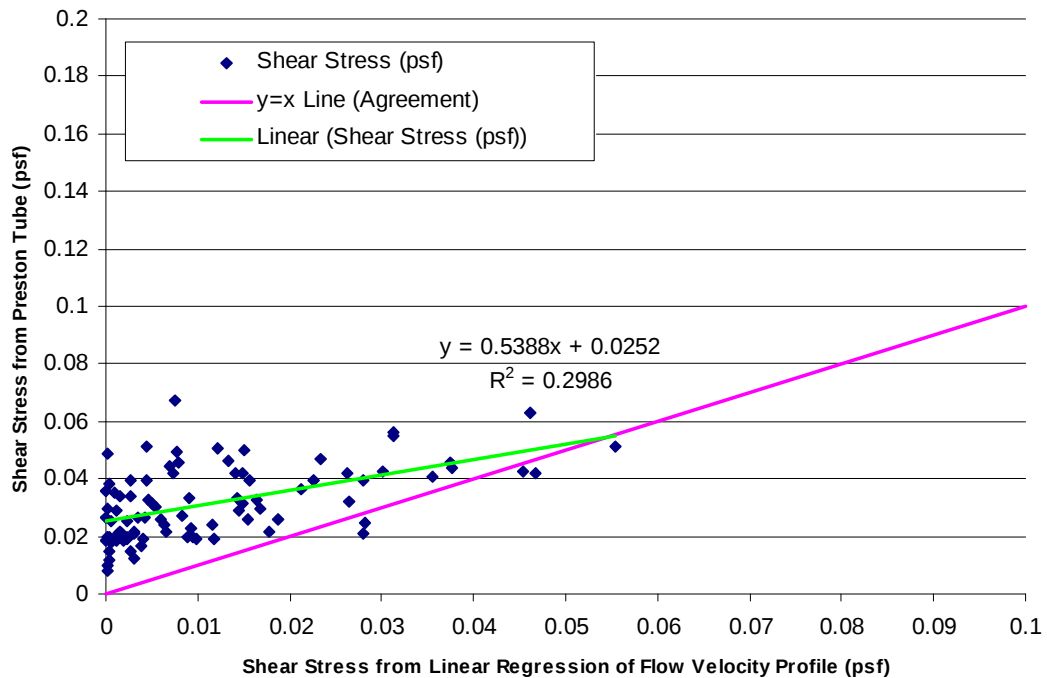


Figure 4.5 Comparison of Shear Stress from Preston Tube and Linear Regression of Flow Velocity Profile for 20 cfs

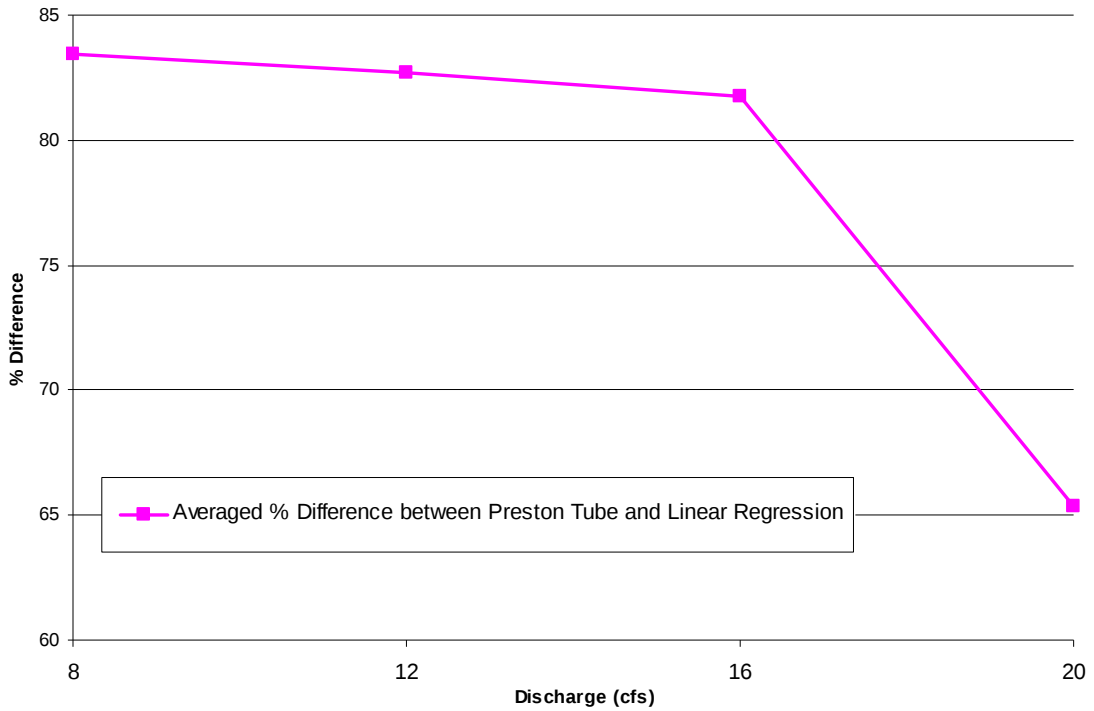


Figure 4.6 Averaged Percentage Difference between Preston Tube and Linear Regression with Change of Discharge

The percentage difference value of shear stress from Preston tube and linear regression of flow velocity profile was computed by using Equation 4.1.

$$\delta = \left( \frac{\alpha - \beta}{\alpha} \right) \times 100 \quad \text{Equation 4.1}$$

Where,  $\delta$  = the shear stress percentage difference between Preston tube and linear regression of flow velocity profile;

$\alpha$  = the value of shear stress by Preston tube; and

$\beta$  = the hear stress from linear regression of flow velocity profile.

A summary table of the maximum and minimum of the percentage difference of the two methods is presented in Table 4.1.

Table 4.1 Calculation Results of Percentage Difference between Preston Tube and Linear Regression of Linear Flow Velocity Profile

| Flow Rate (cfs) | Maximum Value (%) | Minimum Value (%) | Averaged Difference (%) |
|-----------------|-------------------|-------------------|-------------------------|
| 8               | 99.8              | 52.0              | 83.45                   |
| 12              | 99.8              | 43.0              | 82.69                   |
| 16              | 100               | 40.4              | 81.75                   |
| 20              | 100               | -6.7              | 67.42                   |

#### 4.2 Comparison of Shear Stress from Linear Regression of Velocity Profile for Lateral Direction ( $\tau_y$ ) and Rozovskii Method

For a detailed analysis of the differences between the two methods, plots are presented in Appendix F to show the difference of the two methods. The x-axis is the shear stress from Rozovskii method and the y-axis is shear stress from linear regression for lateral flow velocity,  $V_y$ . The plots indicate the points are mostly distributed horizontally because of the negative shear stress from Rozovskii method. The negative shear stress from Rozovskii method resulted from a lower water surface slope. As presented in Equation 2.22, the low water surface slope caused the right hand side bracket of Equation 2.22 to be greater. As a result, negative shear stress was observed from Rozovskii Method. The percentage difference between the shear stress from linear regression of the velocity profile for the lateral direction and Rozovskii method was calculated by using Equation 4.2. The summary of the comparison of two methods is shown in Table 4.2.

$$\delta_1 = \left( \frac{\alpha_1 - \beta_1}{\alpha_1} \right) \times 100 \quad \text{Equation 4.2}$$

Where,  $\delta_1$  = the percentage difference between Preston tube and Rozovskii Method (%);

$\alpha_1$  = the value of shear stress by linear regression of lateral flow velocity ( $V_y$ ); and

$\beta_1$  = the value of shear stress from the Rozovskii method.

Table 4.2 Calculation Results of Percentage Difference between Linear Regression and Rozovskii Method

| Flow Rate (cfs) | Maximum Value (%) | Minimum Value (%) | Averaged Difference (%) |
|-----------------|-------------------|-------------------|-------------------------|
| 8               | -123.17           | -84.64            | -99.20                  |
| 12              | 434.76            | -19.95            | -92.10                  |
| 16              | -757.42           | -45.01            | -104.78                 |
| 20              | -205.69           | -2.83             | -99.65                  |

#### 4.3 Comparison of Shear Stress from Preston Tube and Reynolds Shear Stress Extrapolation

Plots to compare the difference of shear stress from Preston tube and Reynolds shear stress are presented in Figure 4.7 through Figure 4.10. In addition, the averaged percentage difference of the two methods with change of discharge was presented in Figure 4.11. The x-axis is shear stress from Reynolds shear stress extrapolation obtained from Equation 4.3 and the y-axis is shear stress from Preston tube. The green line in the plots indicates the best fit line from different shear stress calculation methods. The plots indicates that the points are generally located between the y axis and the  $y=x$  curve. That means the shear stress from Preston tube is higher than shear stress from Reynolds shear stress extrapolation because the Preston tube directly touches on the bed surface of the flume but Reynolds shear from ADV does not touch the bed surface during data collection.

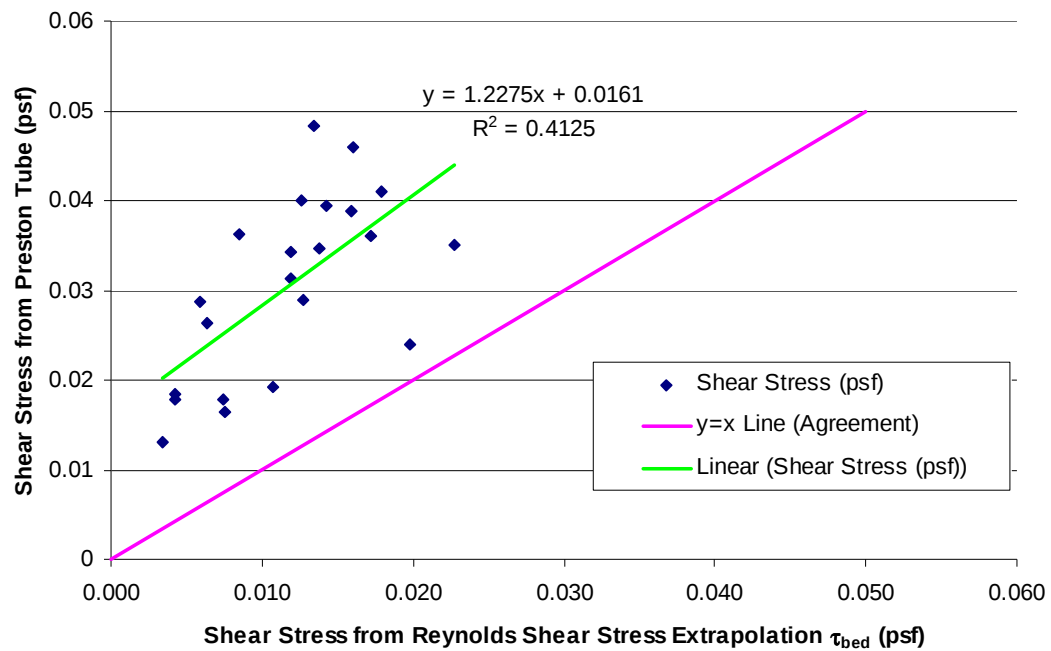


Figure 4.7 Comparison of Shear Stress from Preston Tube and Reynolds Shear Stress Extrapolation for 8 cfs

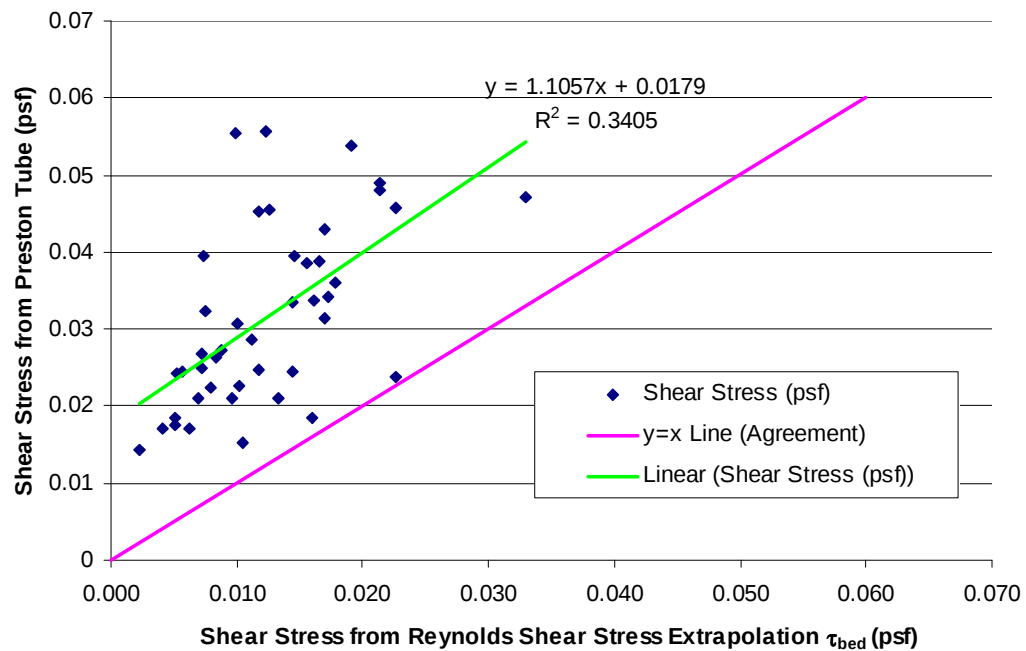


Figure 4.8 Comparison of Shear Stress from Preston Tube and Reynolds Shear Stress Extrapolation for 12 cfs

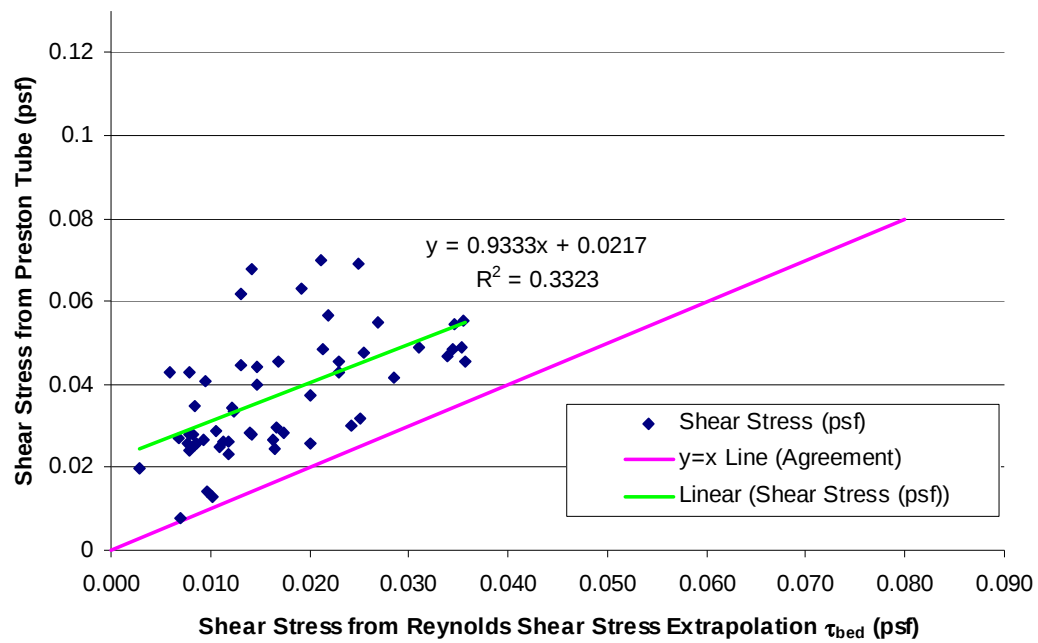


Figure 4.9 Comparison of Shear Stress from Preston Tube and Reynolds Shear Stress Extrapolation for 16 cfs

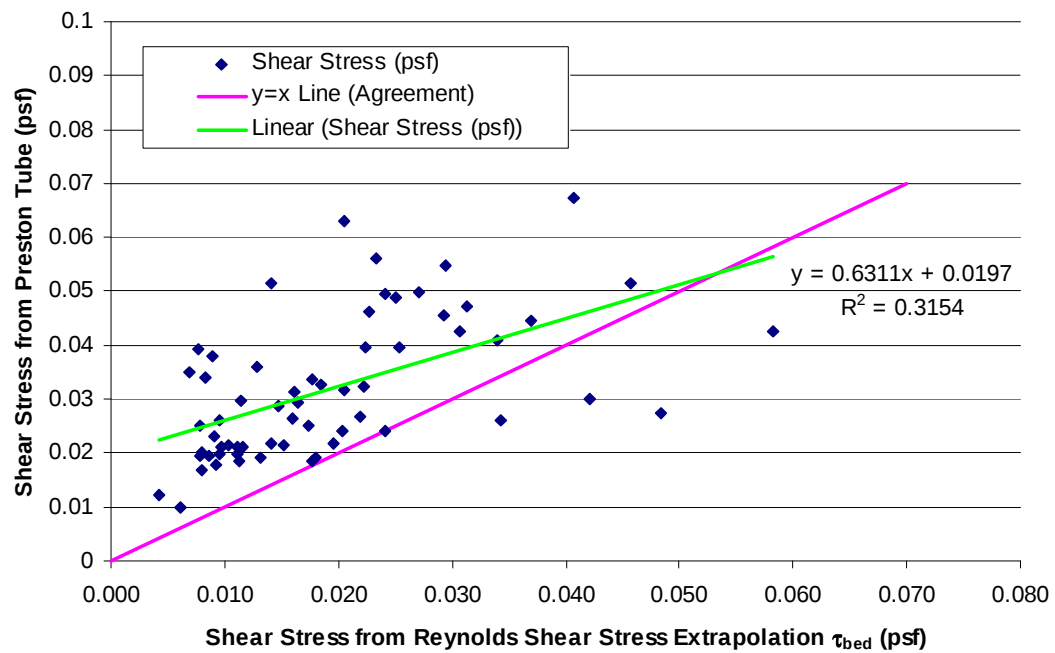


Figure 4.10 Comparison of Shear Stress from Preston Tube and Reynolds Shear Stress Extrapolation for 20 cfs

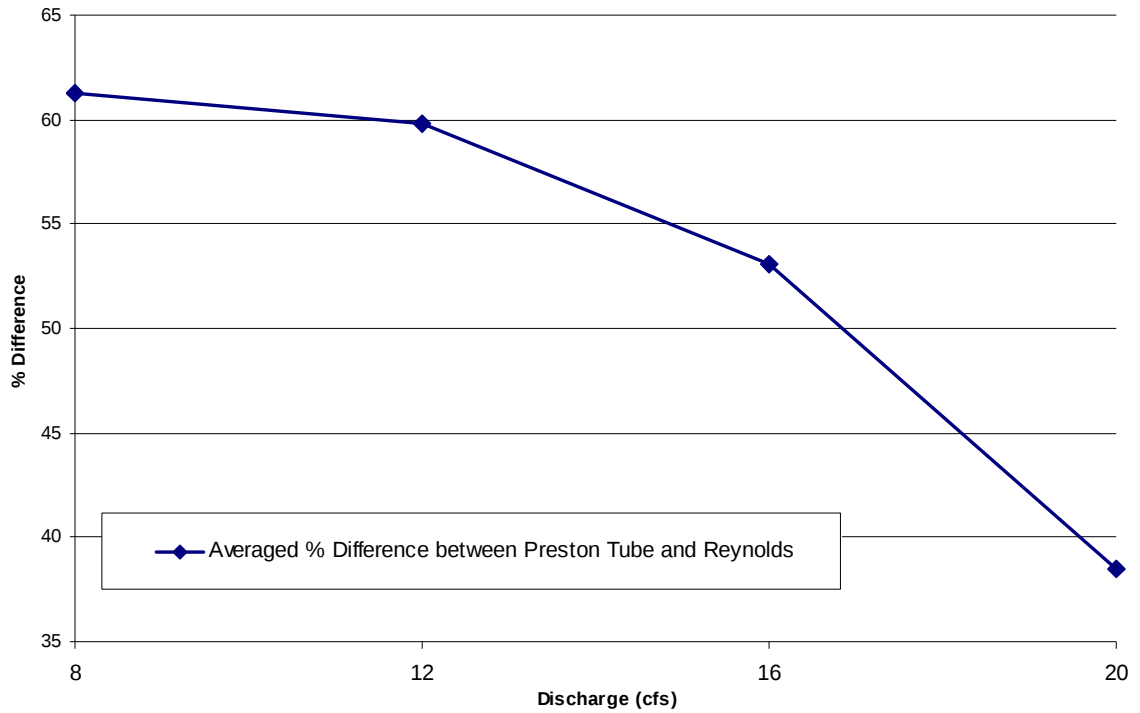


Figure 4.11 Averaged Percentage Difference between Preston Tube and Reynolds Shear Extrapolation with Change of Discharge

The percentage difference of shear stress from Preston tube and the Reynolds shear extrapolation method was obtained by using the Equation 4.3. Table 4.3 presents the difference of the calculation results.

$$\delta_2 = \left( \frac{\alpha_2 - \beta_2}{\alpha_2} \right) \times 100 \quad \text{Equation 4.3}$$

Where,  $\delta_2$  = the shear stress percentage difference between Preston tube and Reynolds shear stress extrapolation (%);

$\alpha_2$  = the value of shear stress calculated from the Preston tube; and

$\beta_2$  = the shear stress from Reynolds shear stress extrapolation.

Table 4.3 Calculation Results of Percentage Difference between Preston Tube and Reynolds Shear Extrapolation

| Flow Rate (cfs) | Maximum Value (%) | Minimum Value (%) | Averaged Difference (%) |
|-----------------|-------------------|-------------------|-------------------------|
| 8               | 79.37             | 17.64             | 61.28                   |
| 12              | 83.74             | 5.20              | 59.79                   |
| 16              | 86.24             | 6.89              | 53.04                   |
| 20              | 80.50             | 0.66              | 38.49                   |

#### 4.4 Comparison of Shear Stress from Linear Regression of Velocity Profile for Longitudinal Direction ( $\tau_x$ ) and Reynolds Shear Stress Extrapolation

Plots comparing differences of shear stress using a linear regression of the flow velocity profile along the x axis and Reynolds shear stress are presented in Figure 4.12 through Figure 4.15. The x-axis is shear stress from linear regression of longitudinal flow direction and y-axis is shear stress from Reynolds shear stress extrapolation. The plots indicate shear stress from Reynolds shear stress extrapolation is greater than shear stress from linear regression because Reynolds shear extrapolation was calculated by obtaining the x-axis intercept point of the linear portion of relative depth and shear stress, but shear stress from linear regression of the longitudinal flow velocity was obtained from the slope of the linear regression equation. The green line in the plots indicates the best fit line from different shear stress calculation methods. Additionally, the averaged percentage difference of the two methods with change of discharge is presented in Figure 4.16.

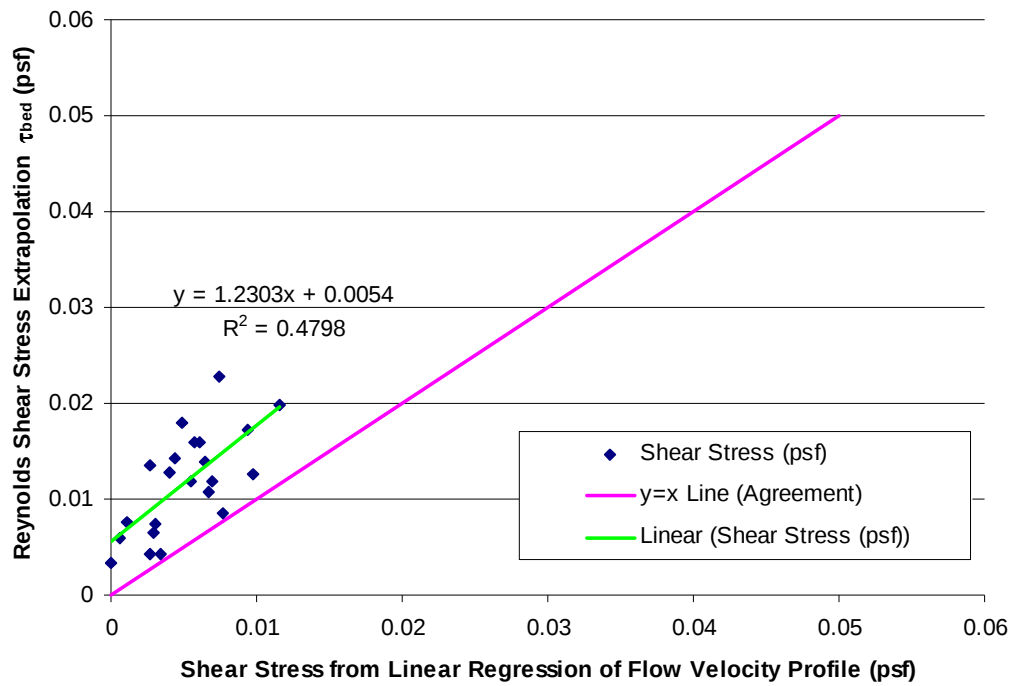


Figure 4.12 Comparison of Shear Stress from Linear Regression and Reynolds Shear Stress Extrapolation for 8 cfs

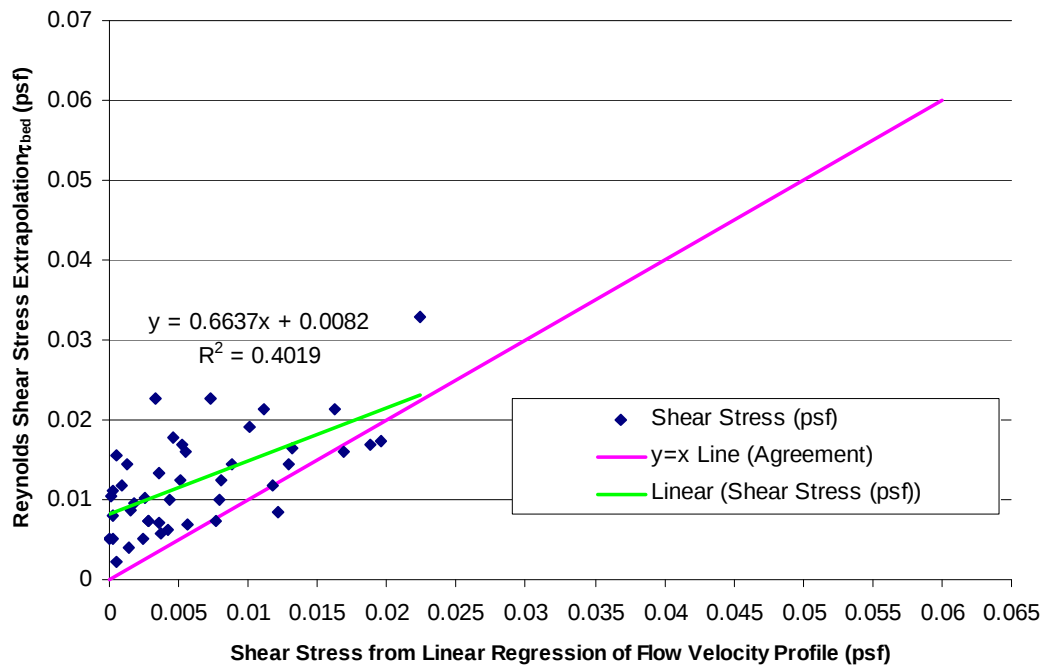


Figure 4.13 Comparison of Shear Stress from Linear Regression and Reynolds Shear Stress Extrapolation for 12 cfs

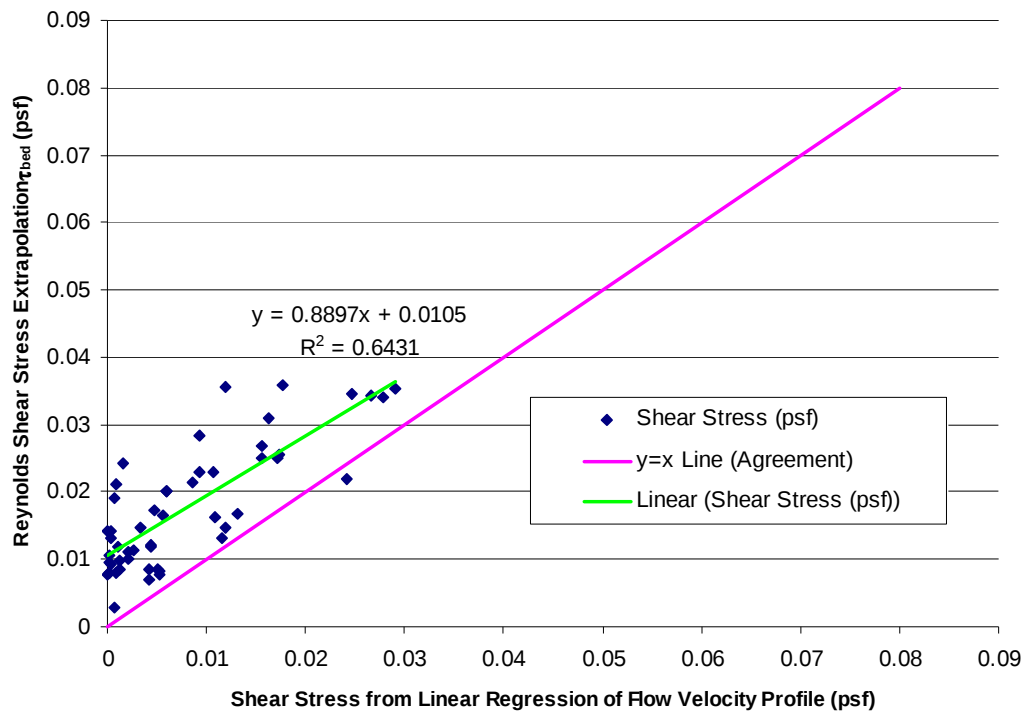


Figure 4.14 Comparison of Shear Stress from Linear Regression and Reynolds Shear Stress Extrapolation for 16 cfs

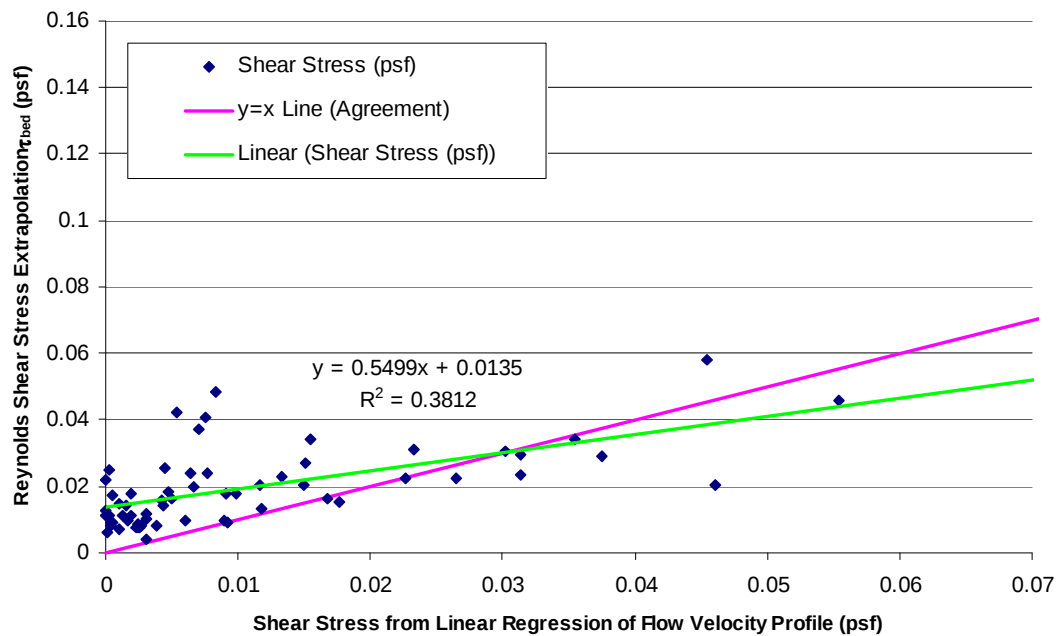


Figure 4.15 Comparison of Shear Stress from Linear Regression and Reynolds Shear Stress Extrapolation for 20 cfs

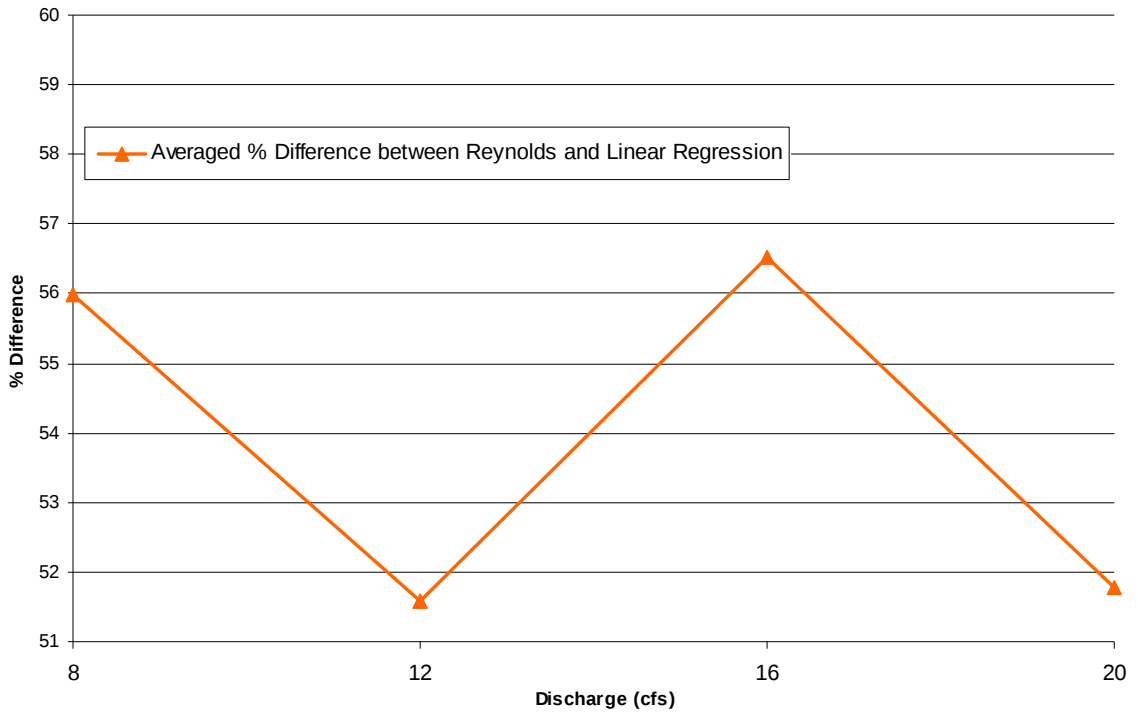


Figure 4.16 Averaged Percentage Difference between Reynolds Shear Extrapolation and Linear Regression with Change of Discharge

Another way to compare with shear stress calculation method is comparing shear stress from linear regression of x-direction flow velocity and shear stress by extrapolating Reynolds shear stress that applies in the bed ( $\tau_{bed}$ ). The percentage difference of shear stress calculated from linear regression of longitudinal flow velocity and Reynolds shear stress extrapolation was obtained using Equation 4.4. Table 4.4 presents the difference of the calculation results.

$$\delta_3 = \left( \frac{\alpha_3 - \beta_3}{\alpha_3} \right) \times 100 \quad \text{Equation 4.4}$$

Where,  $\delta_3$  = the shear stress percentage difference between linear regression of the longitudinal flow velocity and Reynolds shear stress extrapolation (%);

$\alpha_3$  = the value of shear stress by Reynolds shear stress extrapolation; and

$\beta_3$  = the shear stress from linear regression.

Table 4.4 Calculation Results of Percentage Difference between Linear Regression of longitudinal velocity and Reynolds Shear Extrapolation

| Flow Rate (cfs) | Maximum Value (%) | Minimum Value (%) | Averaged Difference (%) |
|-----------------|-------------------|-------------------|-------------------------|
| 8               | 99.25             | 9.24              | 55.99                   |
| 12              | 99.23             | 0.14              | 51.59                   |
| 16              | 99.93             | -10.07            | 56.53                   |
| 20              | -125.32           | -1.1              | 51.77                   |

## 4.5 Comprehensive Comparisons

Section 4.1 through Section 4.4 described the differences of shear stress calculation methods from Preston tube, linear regression of longitudinal flow velocity, Rozovskii method and Reynolds shear stress extrapolation. This chapter shows the shear stress calculated from Preston tube is the most accurate method because the Preston tube directly touched on the bed of the channel during data collection. In the case of Reynolds shear stress extrapolation and linear regression method, these methods are based on the ADV data, and the ADV that does not directly touch the bed of the channel during measurements.

Bar charts are presented in Figure 4.17 through Figure 4.20 that shows the percentage difference between maximum shear stress from Preston tube and other maximum shear stress values by using Reynolds shear stress extrapolation, linear regression and HEC-RAS. Due to the low accuracy, shear stress from Rozovskii method was excluded in the bar charts. The plots indicate that Reynolds shear stress extrapolation has relatively better agreement with shear stress from Preston tube than a linear regression of flow velocity profile.

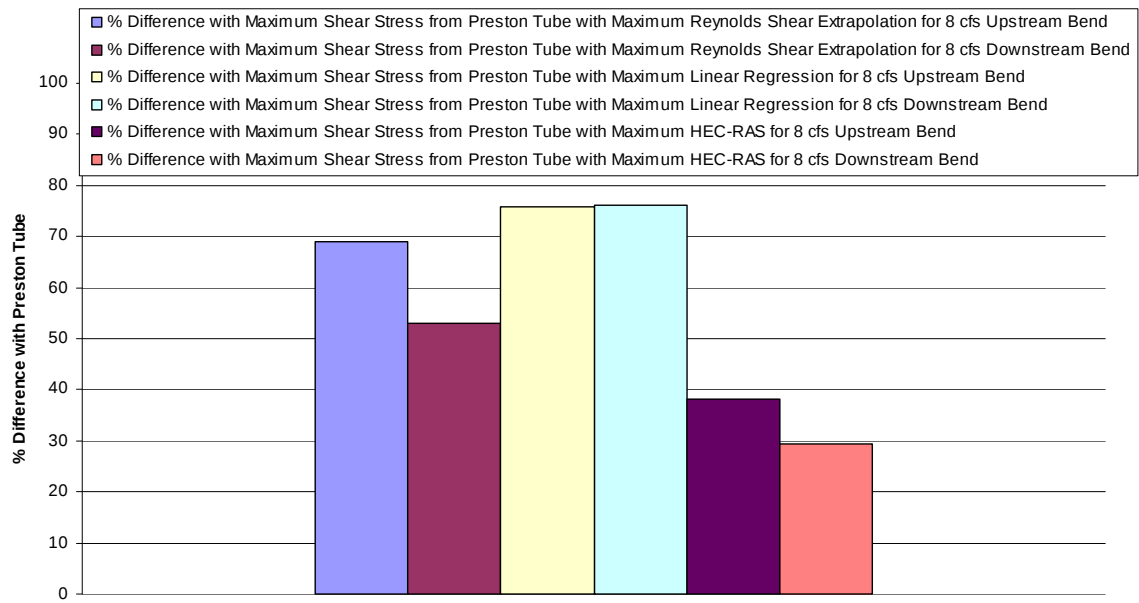


Figure 4.17 Percentage Difference of Maximum Shear Stress with Preston Tube for 8 cfs

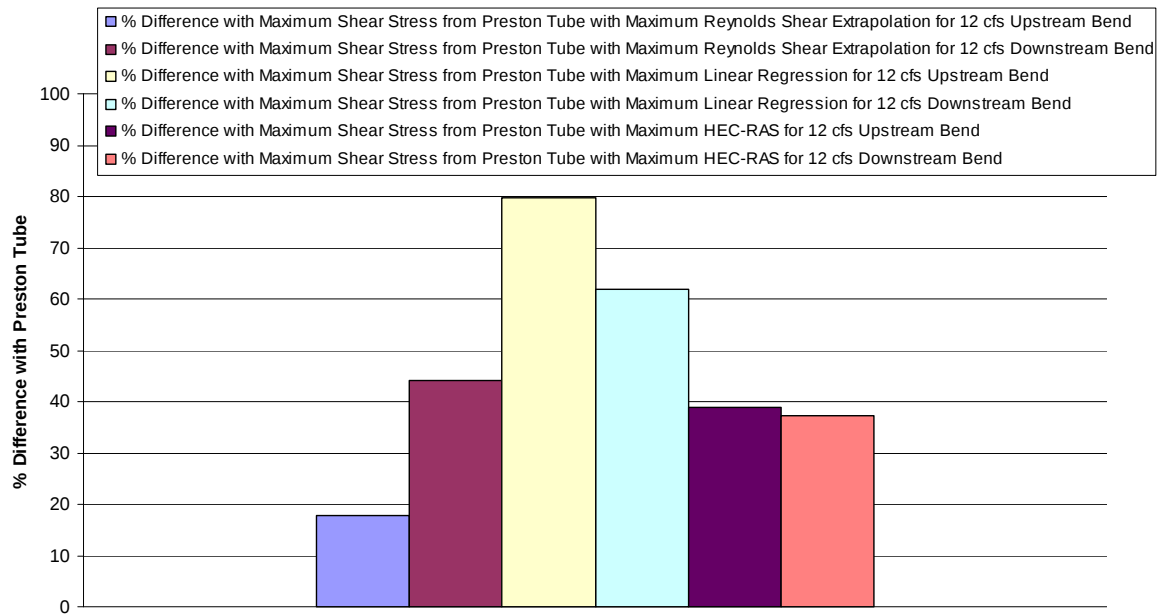


Figure 4.18 Percentage Difference of Maximum Shear Stress with Preston Tube for 12 cfs

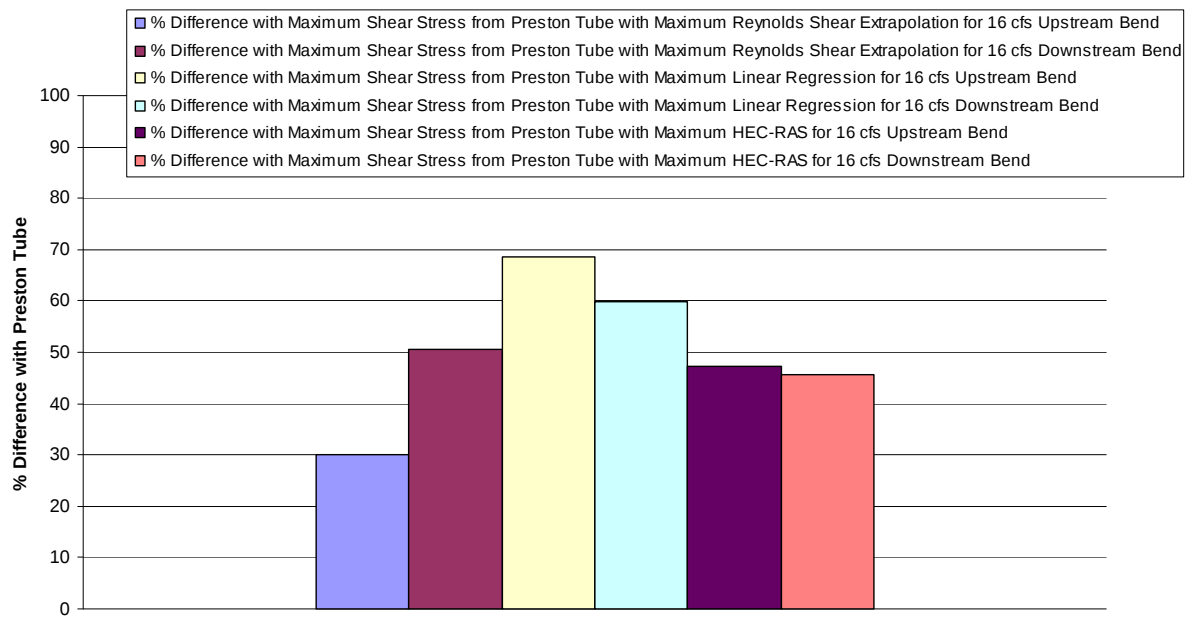


Figure 4.19 Percentage Difference of Maximum Shear Stress with Preston Tube for 16 cfs

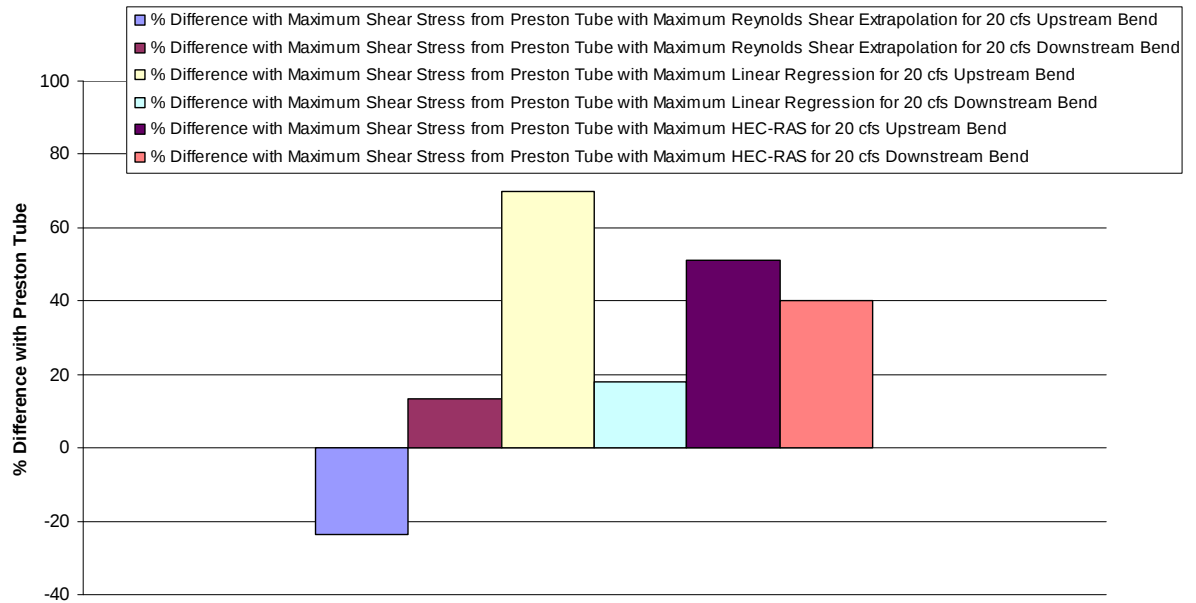


Figure 4.20 Percentage Difference of Maximum Shear Stress with Preston Tube for 20 cfs

#### **4.6 Averaged Shear Stress from HEC-RAS and $K_b$ Value**

Heintz (2002) explained that an adjustment factor,  $K_b$  should be developed due to the different geometry condition between the upstream and downstream bend. The definition of  $K_b$  is the ratio of maximum shear stress to averaged shear stress. In this study, averaged shear stress was calculated by taking average the HEC-RAS shear stress output of cross section 1 and 2 for the upstream bend and taking the average output of cross section 10 and 11 for the downstream bend to calculate cross section averaged shear stress. HEC-RAS modeling output for shear stress is presented in Table 4.5 and Table 4.6. Two maximum shear stresses were selected for analysis; from extrapolation of Reynolds shear stress profile and from Preston tube method. The  $K_b$  value, computed by dividing maximum shear stress by cross section averaged shear stress from HEC-RAS, is presented and summarized in Table 4.7 and Table 4.8.

Table 4.5 HEC-RAS Output for Shear Stress for Upstream Bend (psf)

| XS | 8 cfs    | 12 cfs   | 16 cfs   | 20 cfs   |
|----|----------|----------|----------|----------|
| 1  | 0.014551 | 0.016432 | 0.018744 | 0.02055  |
| 2  | 0.012438 | 0.014542 | 0.016896 | 0.018763 |
| 3  | 0.014991 | 0.016844 | 0.019166 | 0.020974 |
| 4  | 0.014289 | 0.016125 | 0.018418 | 0.020209 |
| 5  | 0.013597 | 0.01551  | 0.01782  | 0.019631 |
| 6  | 0.014445 | 0.016236 | 0.018536 | 0.020332 |
| 7  | 0.012989 | 0.015048 | 0.017457 | 0.019347 |
| 8  | 0.013057 | 0.015025 | 0.017375 | 0.019229 |

Table 4.6 HEC-RAS Output for Shear Stress for Downstream Bend (psf)

| XS | 8 cfs    | 12 cfs   | 16 cfs   | 20 cfs   |
|----|----------|----------|----------|----------|
| 10 | 0.025227 | 0.029593 | 0.034569 | 0.038344 |
| 11 | 0.028996 | 0.032956 | 0.038042 | 0.041828 |
| 12 | 0.034162 | 0.036949 | 0.041766 | 0.045203 |
| 13 | 0.025574 | 0.029527 | 0.034338 | 0.037916 |
| 14 | 0.025627 | 0.029753 | 0.034675 | 0.038318 |
| 15 | 0.02509  | 0.029061 | 0.033865 | 0.037415 |
| 16 | 0.025559 | 0.029464 | 0.034246 | 0.037739 |
| 17 | 0.028973 | 0.032477 | 0.037302 | 0.040723 |
| 18 | 0.028534 | 0.031707 | 0.036329 | 0.039591 |

Table 4.7  $K_b$  Value from Maximum Shear Stress of Reynolds Shear Stress

|            | Flow Rate | Averaged Shear Stress (psf) | Maximum Shear Stress (psf) | $R_c/T_w$   | $K_b$ Value | Location      |
|------------|-----------|-----------------------------|----------------------------|-------------|-------------|---------------|
| Upstream   | 8 cfs     | 0.0134945                   | 0.007502549                | 2.788572251 | 0.55597     | XS 4 Piezo e  |
| Downstream | 8 cfs     | 0.0271115                   | 0.022733373                | 6.913463558 | 0.83851     | XS 16 Piezo d |
| Upstream   | 12 cfs    | 0.015487                    | 0.022623014                | 2.617889474 | 1.46077     | XS 4 Piezo b  |
| Downstream | 12 cfs    | 0.0312745                   | 0.032936826                | 6.202185792 | 1.05315     | XS 16 Piezo d |
| Upstream   | 16 cfs    | 0.01782                     | 0.024180063                | 2.476354806 | 1.35691     | XS 4 Piezo a  |
| Downstream | 16 cfs    | 0.0363055                   | 0.03574071                 | 5.720368439 | 0.98444     | XS 17 Piezo d |
| Upstream   | 20 cfs    | 0.0196565                   | 0.048435716                | 2.41252646  | 2.46411     | XS 6 Piezo b  |
| Downstream | 20 cfs    | 0.040086                    | 0.058249589                | 5.442294974 | 1.45312     | XS 15 Piezo d |

Table 4.8  $K_b$  Value from Maximum Shear Stress of Preston Tube

|            | Flow Rate | Averaged Shear Stress (psf) | Maximum Shear Stress (psf) | $R_c/T_w$   | $K_b$ Value | Location      |
|------------|-----------|-----------------------------|----------------------------|-------------|-------------|---------------|
| Upstream   | 8 cfs     | 0.0134945                   | 0.024213                   | 2.819001891 | 1.794286    | XS 8 Piezo c  |
| Downstream | 8 cfs     | 0.0271115                   | 0.048366069                | 6.814699793 | 1.78397     | XS 15 Piezo d |
| Upstream   | 12 cfs    | 0.015487                    | 0.027531493                | 2.620013523 | 1.77772     | XS 5 Piezo a  |
| Downstream | 12 cfs    | 0.0312745                   | 0.05886005                 | 6.122581845 | 1.88205     | XS 10 Piezo a |
| Upstream   | 16 cfs    | 0.01782                     | 0.034551784                | 2.485886579 | 1.93893     | XS 6 Piezo b  |
| Downstream | 16 cfs    | 0.0363055                   | 0.072179902                | 5.720368439 | 1.98813     | XS 17 Piezo e |
| Upstream   | 20 cfs    | 0.0196565                   | 0.039212852                | 2.354478065 | 1.99491     | XS 8 Piezo c  |
| Downstream | 20 cfs    | 0.040086                    | 0.067410083                | 5.444995864 | 1.68164     | XS 10 Piezo c |

Before this study, Ippen and Drinker (1962), USBR (1964) and Yen (1965) performed research to figure out the empirical equations of  $K_b$ . After  $K_b$  values are obtained by using Reynolds shear stress and Preston tube, the empirical equations and upper envelope curves of  $K_b$  were obtained by taking the regression of the power function, including the data from previous studies by Ippen and Drinker (1962), USBR (1964) and Yen (1965). The plots are presented in Figure 4.21 and Figure 4.22.

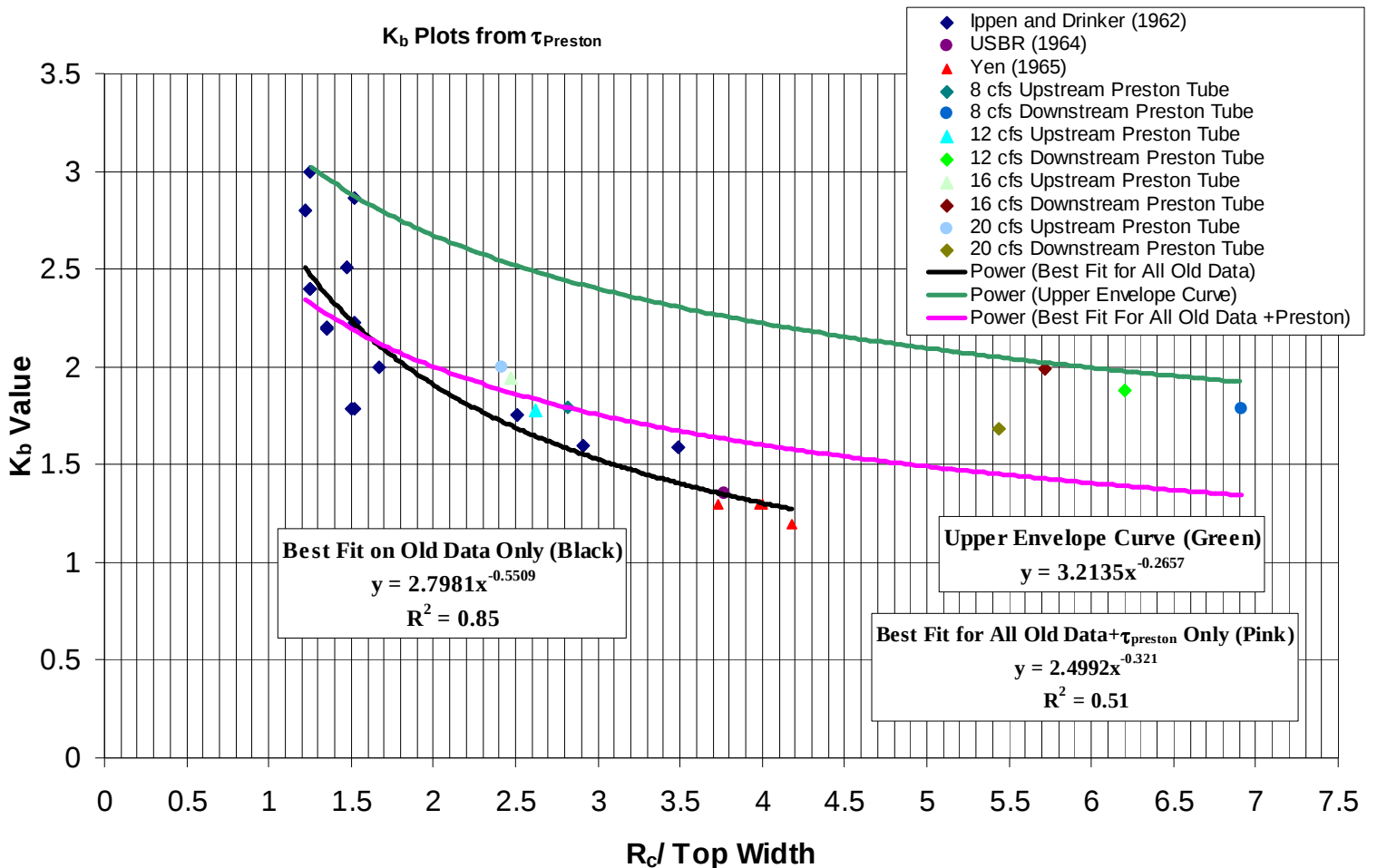


Figure 4.21  $K_b$  Plots from the Ratio of Maximum Shear Stress from Preston Tube to Cross Section Averaged Shear Stress from HEC-RAS

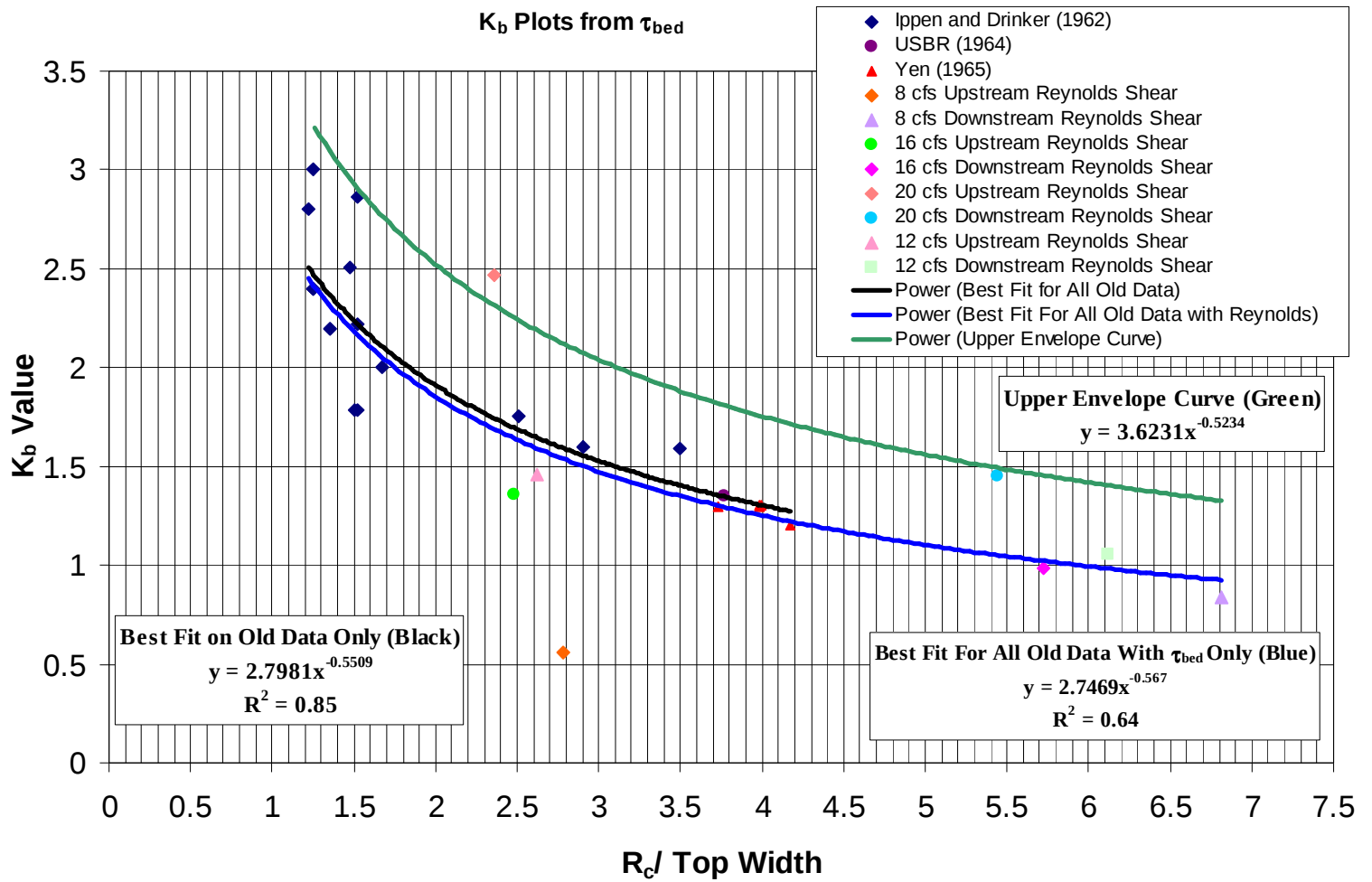


Figure 4.22  $K_b$  Plots from the Ratio of Maximum Shear Stress from Reynolds Shear Stress to Cross Section Averaged Shear Stress from HEC-RAS

## **5 Conclusions and Recommendations**

### **5.1 Overview**

The physical model study provided the distribution of shear stress in a meandering channel. The previous research and laboratory experiments presented a guideline of shear stress analysis in a meandering channel. However, the previous studies about flow in bends have limitations because they focused on the distribution of shear stress in a single bend. This study presented data analysis results to determine shear stress in a meandering channel by performing laboratory tests. The flume is constructed as the combination of two types of bends; type 1 and type 3. The ratio of radius of curvature and top width of type 1 and type 3 bend in the flume was 2.02 and 4.39, respectively.

### **5.2 Conclusions**

To determine the shear stress distribution in a meandering channel, the physical modeling study was conducted in the following phases.

- a) Model construction and calibration;
- b) Data collection of flow depth, flow velocity and boundary shear stress;
- c) Data analysis.

After the study procedures presented above, the following conclusions were drawn from this experimental study.

- The shear stress from the method of Rozovskii (1961) that was presented in Equation 2.2 only shows the shear stress that applies in the lateral direction. On the other hand, the shear stress from the Preston tube and the Reynolds shear extrapolation show total shear stress. Therefore, the shear stress from Rozovskii (1961) was significantly smaller than the shear stress from the Preston tube and the Reynolds shear stress extrapolation.
- The shear stress from the Preston tube is the most accurate value among those obtained by four different methods because the Preston tube collects directly on the surface of the channel but the other methods used ADV data. In other words, ADV has instrumentation limitations because it can not touch the bed of the channel.
- The shear stress from the Reynolds shear stress extrapolation showed the best agreement with the shear stress from the Preston tube because Reynolds shear stress extrapolation considers the limitation of instrumentation using ADV by extrapolating shear stress.
- This study obtained equations to estimate  $K_b$  value (the ratio of maximum shear stress to averaged shear stress) in meandering channels by using the Preston tube and the Reynolds shear stress extrapolation. The equations derived are: 1) the best fit equation by taking regression of  $K_b$  points from previous studies (Ippen and Drinker (1962), USBR (1964) and Yen (1965)) and this study; and 2) an upper envelope equation that was obtained from the maximum values of  $K_b$ . The  $K_b$  values from the upper envelope curve using the Preston tube were 27% higher in average than the  $K_b$  values from

the best fit curve. Also, the  $K_b$  values from the upper envelope curve using the Reynolds shear stress extrapolation was 28% higher in average than the  $K_b$  values from the best fit curve. Therefore, it was concluded that the effect of enveloping in both methods were similar.

- In design situations, the upper envelope equation from the Preston tube is recommended for design because the upper envelope equation from Preston tube considers the worst case scenario. The best fit and upper envelope equation for  $K_b$  value from the Preston tube is presented in Equation 5.1 and Equation 5.2 respectively.

$$K_b = 2.4992 \times \left( \frac{R_c}{T_w} \right)^{-0.321} \quad \text{Equation 5.1}$$

$$K_b = 3.2135 \times \left( \frac{R_c}{T_w} \right)^{-0.2657} \quad \text{Equation 5.2}$$

Where,  $K_b$  = ratio of maximum shear stress and averaged shear stress from HEC-RAS modeling (dimensionless);

$R_c$  = radius of curvature of meandering channel (L); and

$T_w$  = top width of channel (L).

- The upper envelope curve for the  $K_b$  value from the Preston tube showed that previous studies (Ippen and Drinker (1962), USBR (1964) and Yen (1965)) were underestimated by 46% when the ratio of radius of curvature and top width of channel was greater than 4. Therefore, cautious observation of the  $K_b$  value from the Preston tube is necessary for application of the upper envelope curve of  $K_b$  in real world situation.

- Due to the limitation of range of data points, it is recommended that use  $K_b$  chart presented in Figure 4.21 when the ratio of radius of curvature and top width of channel ranged between 1 and 7.

### **5.3 Recommendations for Future Research**

During the physical modeling study, model construction, data collection and experimental data analysis were conducted. The shear stress distribution was calculated and plotted by selecting four different ways. For future research, several recommendations are provided;

- It is recommended to investigate shear stress distribution in case of native topography geometry by using the same methods of this study that are applicable to hydraulic design in the real world.
- The number of data points (seven or eight) that were collected by the ADV in the velocity profile was not good enough to obtain an accurate result from a linear regression of the flow velocity profile. To increase the accuracy of the linear regression, the number of data points collected should be at least fifteen for a reasonable linear regression (about twice of current number of data points).

### **5.4 Limitations of this Study**

This experimental study introduced four different methods to calculate shear stress in a bend. Also, the study obtained equations to estimate how much shear stress in a bend is higher than in a straight channel, but this study is limited in the following points;

- This study was based on the laboratory data only from four discharges; 8, 12, 16 and 20 cfs.
- In the low flow rate case (8 and 12 cfs), data collection was limited because the ADV could not be submerged in the water due to low water surface elevation.

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## **Appendix A. Model Description**

## **A.1 Introduction**

In order to facilitate analysis of shear stress distribution in a meandering channel, physical modeling was conducted at the Colorado State University Engineering Research Center. In this chapter, the geometry of the model, construction procedure and methods of measurements will be introduced.

## **A.2 Model Description**

The physical model is an undistorted, 1:12 Froude scale model. The boundary of the channel is prismatic. That means the geometry of the channel is constant. The composition of the physical model is; two kinds of bends and one transitional area between two bends. A data collection cart was mounted on the top of the physical model with a point gage for the measurement of three dimensional flow velocity ( $V_x$ ,  $V_y$  and  $V_z$ ), flow depth ( $h$ ) and boundary shear stress ( $\tau$ ) (Heintz 2002). Figure A.1 presents the schematic view of the physical model.



Figure A.1 Schematic View of the Physical Model

### A.2.1 Model Geometry

It is impossible to construct a physical model that describes the whole of the study reach because study reach length of the prototype is 29 miles. Therefore, a representative section of the reach was selected to describe the flow in a meandering channel (Heintz 2002). The data of the reach geometry were obtained by using 1992 aerial photographs (Heintz 2002). The measured parameters of the study reach were; top width, radius of curvature, the length of the bend, relative curvature and the rotation angle of the bend. Table A.1 shows the geometry of the prototype. In addition, Table A.2 provides the information of the physical model geometry. Figure A.2 describes the geometry measurement results of the study reach. To maintain the 1:12 Froude scale, type 1 and type 3 bend were selected for the physical model (Heintz 2002).

Table A.1 The Geometry of the Prototype of Study Reach (from Heintz 2002)

| Type | Top Width    | Radius of Curvature | Bend Angle | Relative Curvature | Channel Length |
|------|--------------|---------------------|------------|--------------------|----------------|
|      | ft (m)       | ft (m)              | degrees    | r/b                | ft (m)         |
| 1    | 230.4 (70.2) | 465 (141.73)        | 125        | 2.02               | 1014 (309)     |
| 3    | 180 (54.86)  | 789.96 (240.77)     | 73         | 4.39               | 1002 (305)     |

Table A.2 The Geometry Information of the Physical Model (from Heintz 2002)

| Type | Top Width  | Radius of Curvature | Bend Angle | Relative Curvature | Channel Length |
|------|------------|---------------------|------------|--------------------|----------------|
|      | ft (m)     | ft (m)              | (degrees)  | r/b                | ft (m)         |
| 1    | 19.2 (5.9) | 38.75 (11.81)       | 125        | 2.02               | 84.5 (25.8)    |
| 3    | 15 (4.6)   | 65.83 (20.06)       | 73         | 4.39               | 83.5 (25.5)    |

**Cochiti to Bernallilo**  
**Radius of Curvature vs. Width**  
**with Corresponding Arc Angle, After Hey (1976)**

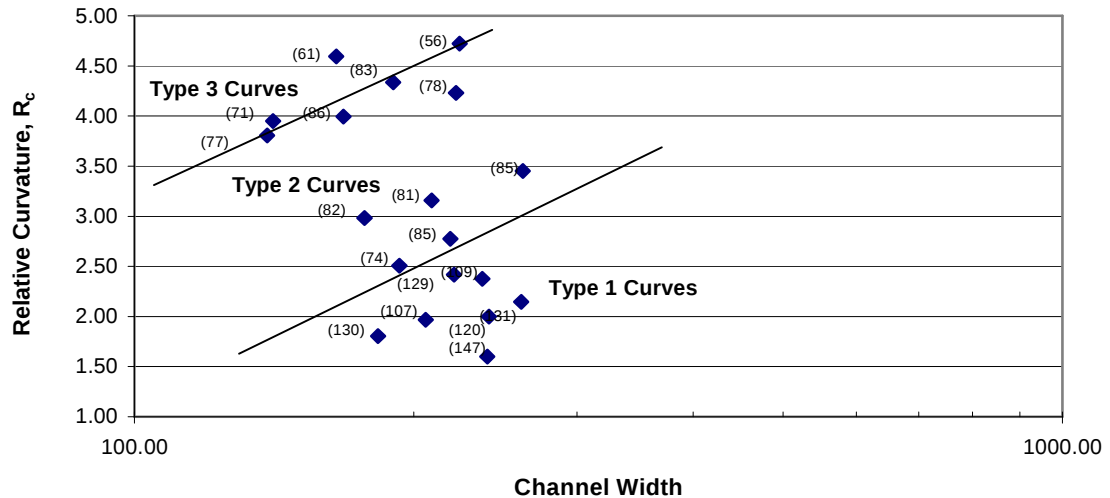


Figure A.2 The Type of the Bend of the Study Reach (from Heintz 2002)

The shape of the model is trapezoidal and the side slope of the channel is 1:3 (Vertical: Horizontal). The channel depth of 1.5ft (0.46m) was selected to satisfy the flow rate of the data collection (Heintz 2002). The bed slope of the model, 0.000863, was close enough as measured in the prototype reach. A straight transition area 10:1

for the smooth connection between upper bend and lower bend was installed (Heintz 2002). Figure A.3 provides the sketch of the physical model.

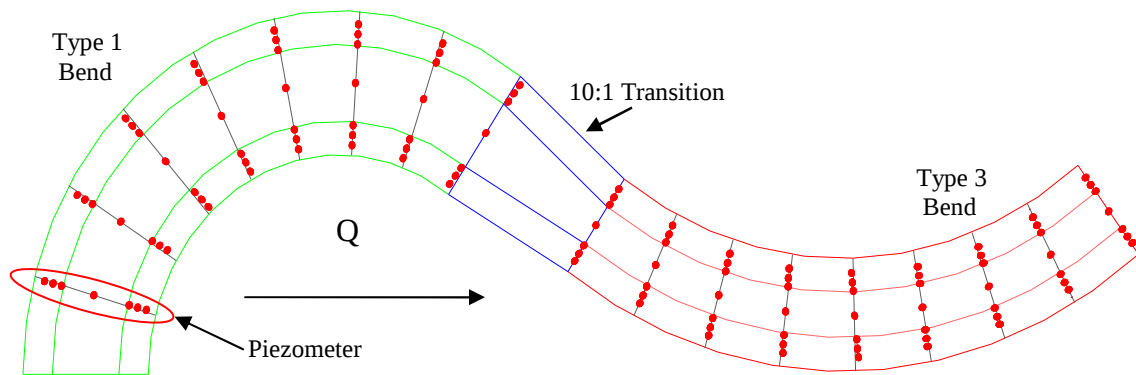


Figure A.3 Sketch of the Main Channel

### A.2.2 Model Construction

Model construction began in early August 2000. About 8 months were spent on the construction. During the construction project, the headbox, main channel and tailbox were constructed. Figure A.4 illustrates the schematic sketch of Hydromachinery Laboratory. In the end of the physical model, the tailbox was constructed for energy dissipation and consistent flow conditions. The components of the headbox are; pipe manifold, a rock baffle and side and bed transitional boundaries (Heintz 2002).

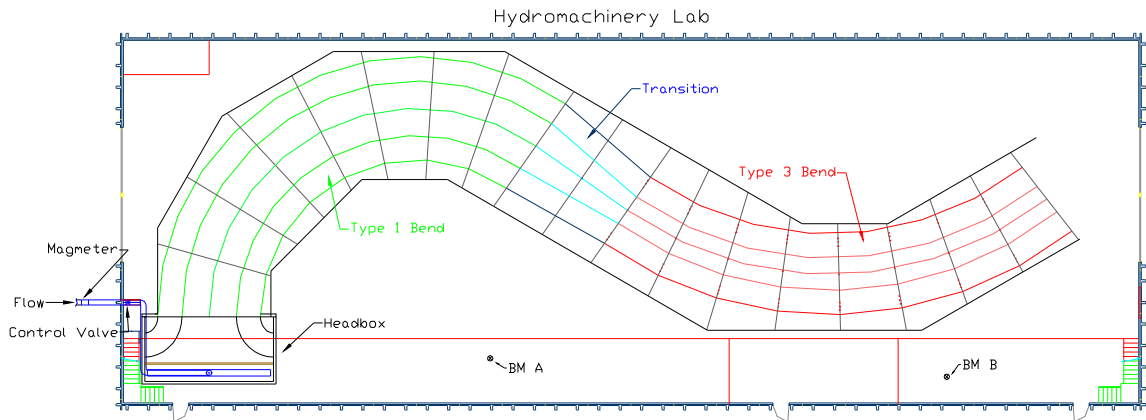


Figure A.4 Schematic Sketch of Hydromachinery Laboratory

The source of water used for the experiment is Horsetooth Reservoir (Heintz 2002). A 12 inch pipe line is directly connected to the headbox of the model from the reservoir (Heintz 2002). For energy dissipation and flow condition maintenance, a rock baffle was installed in the headbox. The averaged size of the rock is 2 inches. In addition, 4 ft high walls are located in the floor of the laboratory for reinforcement of the model security (Heintz 2002). Figure A.5 shows the walls of the model. To construct rigid channel geometry, a plywood skeleton was used in each cross section.

The plywood skeleton of the model placed eight pieces in the upstream bend and the other eight pieces located in the downstream bend. For the construction of the main channel, sand was filled, saturated, compacted and leveled for the construction of the main channel (Heintz 2002). Figure A.6 and Figure A.7 show the sand filling and leveling for main channel construction.



Figure A.5 4 ft High Walls of the Model



Figure A.6 Skeleton of the Main Channel and Filling Material of Main Channel



Figure A.7 Leveling of Fill Sand of the Main Channel

To maintain a rigid geometry in the bend, the cross section skeletons were connected to each other with 4 inch by 1/8<sup>th</sup> inch steel flashing (Heintz 2002). The flash was installed at each top bank point and channel toe in each cross section (Heintz 2002). Figure A.8 shows the installation of the steel flashing. After the completion of steel flashing and welding, a 2 inch thick concrete cap was placed over the top of the finished sand to reinforce the strength of the channel geometry. The next procedure of model construction was concrete placement. About 40 cubic yards of concrete and 600 tons of sand were used for the model construction. To obtain the roughness of the channel, a broom finish of concrete was applied. In addition, water sealant was sprayed on the main channel to prevent leaking. Figure A.9 and Figure A.10 present concrete placement and broom finish for desired channel roughness.

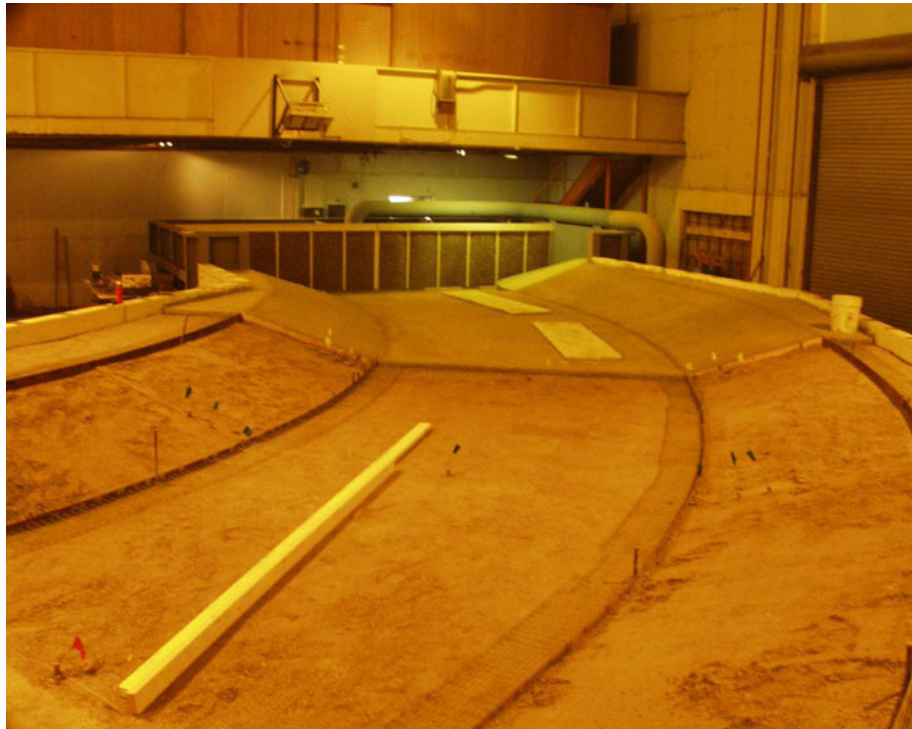


Figure A.8 Installation of Steel Flashing



Figure A.9 Concrete Placement for Model Construction



Figure A.10 Concrete Broom Finish for Desired Channel Roughness

In the downstream end of the model, a stop log was installed to develop backwater to generate the proper relationship between discharge and stage. Also, a 10 inch pipe and two 12 inch culverts were installed in tailbox to convey water flow to College Lake (Heintz 2002).

### **A.3 Instrumentation**

The physical model was constructed for the measurements of flow velocity, flow depth, flow rate and shear stress. Data collection facilities were placed on the cart that was installed above the main channel. In this section, the procedure and method of data collection will be introduced.

#### **A.3.1 Flow Rate Measurement**

For the measurement of the flow rate, a Georg Fischer® SIGNET 2550 Insertion Magmeter with an accuracy of  $\pm 2\%$  was used. The water source is Horsetooth Reservoir. The pipeline that connects Horsetooth Reservoir and the model is 12 inches and the material of the pipe is PVC (Polyvinyl Chloride). Figure A.11 shows the photographs of the flow meter.



Figure A.11 SIGNET Meters and Electronic Display Boxes (from Kinzli, 2005)

### A.3.2 Flow Depth Measurement

Two methods of flow depth measurement were used in the procedure of data collection. The first method is point gauge measurement that was presented in Figure A.12. For this method, a point gauge was installed on the data collection cart.

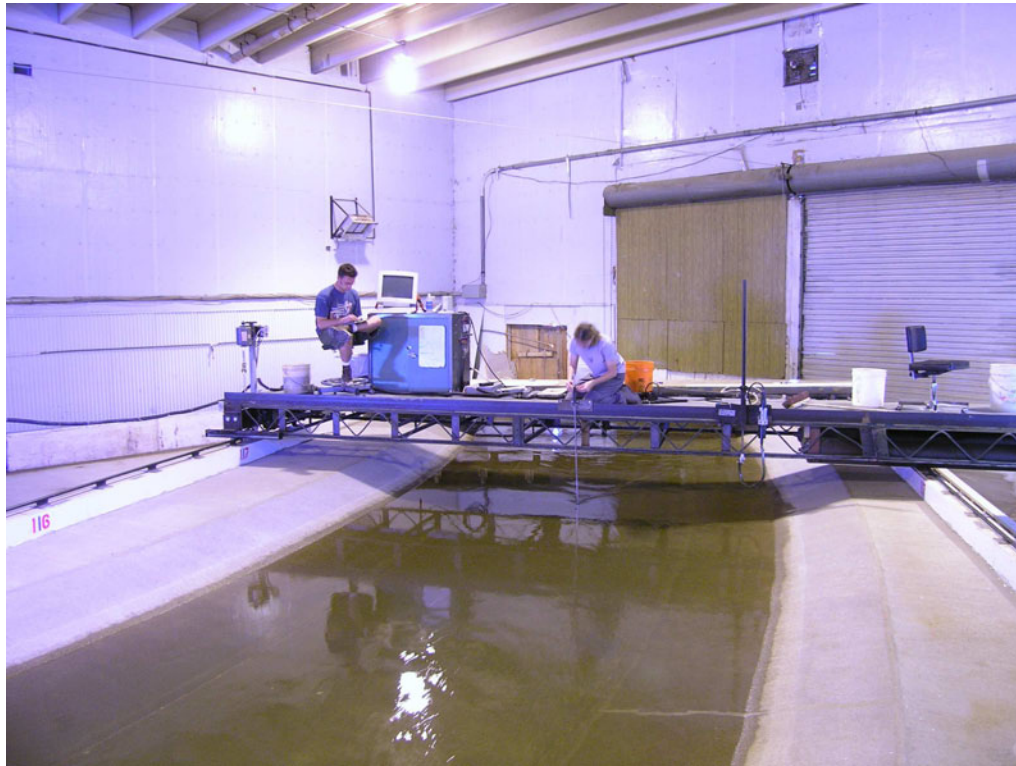


Figure A.12 Point Gauge Installation for Flow Depth Measurement

In addition to the point gage, piezometer taps were installed throughout the model. During the main channel construction procedure, a piezometer was placed at the skeleton of main channel. In each cross section, 7 piezo meters were installed. In total, 122 piezometers installed for data collection. The label in each piezometer was assigned a through g from left to right. Figure A.13 shows the sketch of the piezometer used. In addition, Figure A.14 shows the installation of the piezometers.

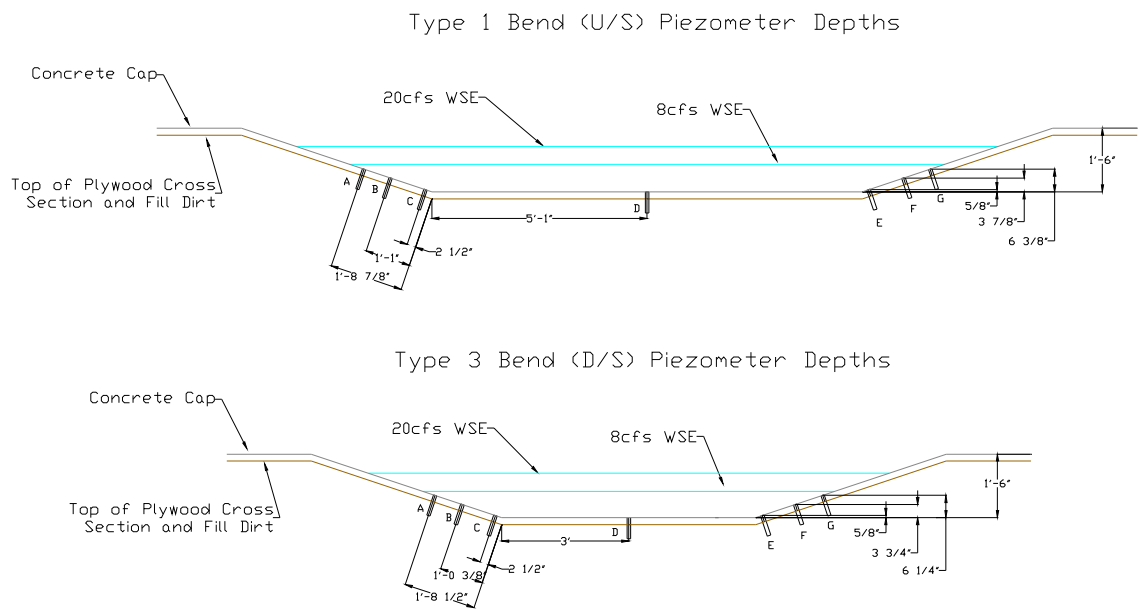


Figure A.13 The Location of Piezometer Type 1 and Type 3 Bend (from Heintz, 2002)



Figure A.14 Installation of Piezometer for Flow Depth Measurement

The piezometers installed in the main channel are connected with a stilling well to allow data collection of water surface elevation (Heintz 2002). 2 inch diameter PVC pipe was placed in the stilling well. All piezometer taps were equipped with a back-flushing system to ensure that the stilling wells and the connecting tubing and taps would not clog (Heintz 2002). Figure A.15 shows the stilling wells used for water surface elevation measurement. The bed elevation of the channel also was measured using a point gauge. Flow depth was calculated by subtracting the bed elevation from water surface elevation.



Figure A.15 Stilling wells for water surface elevation measurement

### **A.3.3 Velocity Measurement**

Since 1993, the ADV has been a popular instrument to collect flow data in field and laboratory studies (Wahl 2000). The installation of the ADV allowed for the measurement of flow velocity in each cross section of the model. The data of an

ADV is three- dimensional velocity measurements that were composed with  $V_x$ ,  $V_y$  and  $V_z$ . The ADV measured velocity from a sampling volume located 0.164 ft (5 cm) below the probe head. The sampling rate of the ADV is 10 Hz. The time period of data collection in each point is approximately 30 seconds. In each point, 300 measurements of flow velocity data were collected. The three-dimensional velocity measurements were collected with the probe of the ADV directed perpendicular to the cart, which was always oriented perpendicular to direction of the flow (Heintz 2002). Figure A.16 presents the photograph of ADV. Also, Figure A.17 shows ADV installation in the data collection cart. After data collection by ADV, data processing is necessary because it is impossible to perform data analysis with the original ADV file. As a result, computer software, WinADV was developed by Wahl (2000). The initial purpose of the software development was to provide the method of displaying the velocity time series (Wahl 2000).



Figure A.16 Photograph of ADV (from Heintz 2002)



Figure A.17 Installation of ADV in Data Collection Cart

#### **A.3.4 Shear Stress Measurement**

Sclafani (2008) performed shear stress data calibration in a 60-foot long, 4-foot wide, 2.5-foot tall flume. To collect data for the calculation of shear stress on the bed and bank of the channel, a Preston tube was used. The Preston tube presented in Figure A.18 allows for measuring boundary shear stress of the model. The Preston tube technique utilizes a modified pitot tube that is placed directly on the bed of the channel at the point of measurement. A pressure transducer was used for the collection of pressure data.



There are two kinds of calibration of the model; the first one is channel roughness calibration. Heintz (2002) conducted the model calibration by using the HEC-RAS program. As a result of the roughness calibration, the value of Manning's  $n$ , the roughness value was determined to be 0.018. The second calibration of the model is backwater calibration by installing stop logs in the tailbox of the model. Using the computed roughness value of 0.018, the HEC-RAS model was then used to calculate a water surface profile for normal depth conditions at all flow rates (Heintz 2002). For the confirmation of the model calibration, Heintz (2002) compared the measured value of water surface profile and calculated value of water surface profile by using HEC-RAS. Figure A.19 and Figure A.20 show the installed stop logs of the model.



Figure A.19 Stop Log Installation of the Model



Figure A.20 Stop Log for Calibration of the Model

## A.5 Test Program (Test Matrix)

There are four different discharge cases (8, 12, 16 and 20 cfs), 18 cross sections and 7 piezometers (a through g) in each cross section. Figure A.21 shows a test matrix for the case of baseline test condition. In case of the discharge of 8 cfs and 12 cfs, several piezometers are not submerged due to the low flow depth. Therefore, data of piezometer a, b, f and g for 8 cfs, are excluded from test matrix. Also, piezometer a and g for 12 cfs could not collected data due to the same situation of 8 cfs.

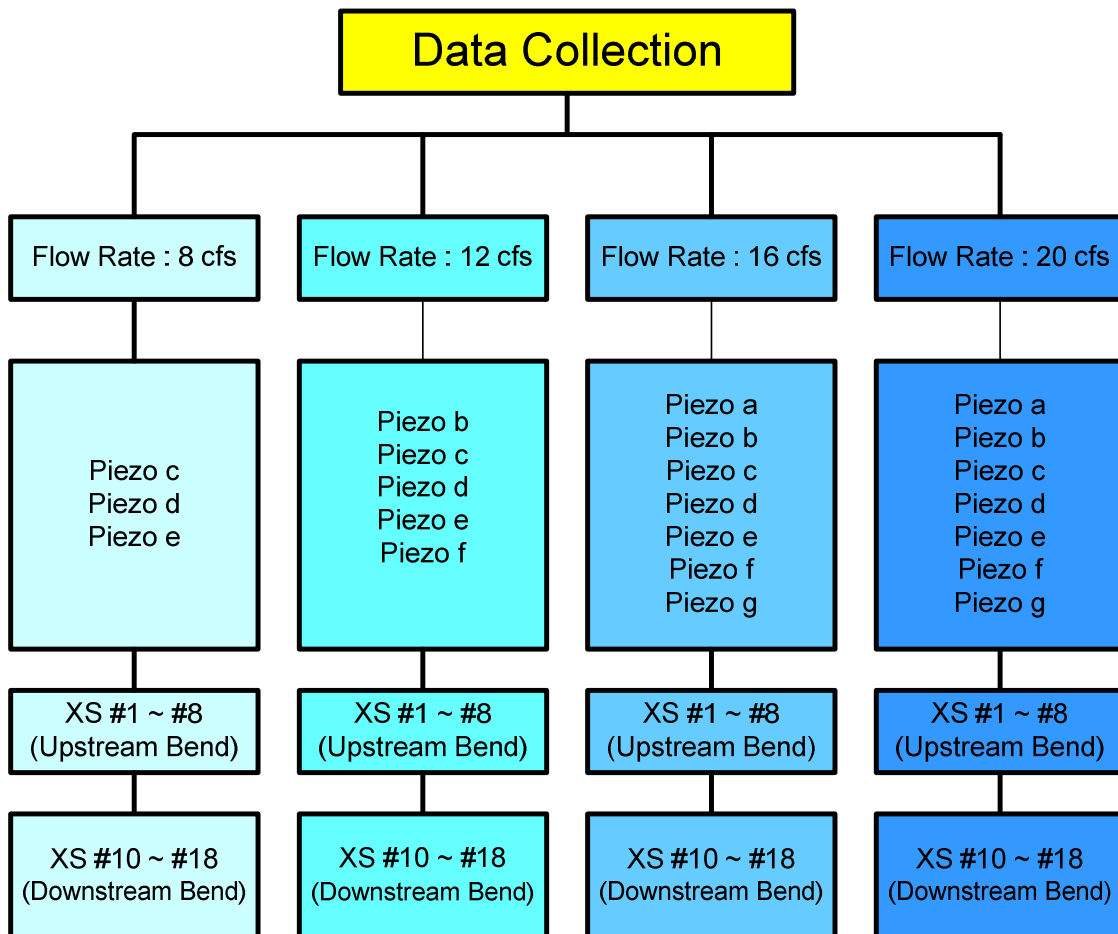


Figure A.21 Test Program of Baseline Condition

## **Appendix B. Preston Tube Calibration**

Table B.1 Shear Stress from Preston Tube Calibration for 8 cfs

| <b>XSEC</b> | <b>Piezo</b> | <b>Shear Stress (psf)</b> |
|-------------|--------------|---------------------------|
| 4           | c            | 0.0178                    |
| 4           | d            | 0.0166                    |
| 4           | e            | 0.0164                    |
| 5           | c            | 0.0183                    |
| 5           | d            | 0.0177                    |
| 5           | e            | 0.0000                    |
| 6           | c            | 0.0178                    |
| 6           | d            | 0.0189                    |
| 6           | e            | 0.0147                    |
| 7           | c            | 0.0172                    |
| 7           | d            | 0.0148                    |
| 7           | e            | 0.0125                    |
| 8           | c            | 0.0203                    |
| 8           | d            | 0.0160                    |
| 8           | e            | 0.0130                    |
| 10          | c            | 0.0438                    |
| 10          | d            | 0.0363                    |
| 10          | e            | 0.0322                    |
| 11          | c            | 0.0240                    |
| 11          | d            | 0.0384                    |
| 11          | e            | 0.0193                    |
| 12          | c            | 0.0342                    |
| 12          | d            | 0.0400                    |
| 12          | e            | 0.0289                    |
| 13          | c            | 0.0393                    |
| 13          | d            | 0.0361                    |
| 13          | e            | 0.0313                    |
| 14          | c            | 0.0263                    |
| 14          | d            | 0.0390                    |
| 14          | e            | 0.0346                    |
| 15          | c            | 0.0287                    |
| 15          | d            | 0.0484                    |
| 15          | e            | 0.0411                    |
| 16          | c            | 0.0286                    |
| 16          | d            | 0.0350                    |
| 16          | e            | 0.0376                    |
| 17          | c            | 0.0328                    |
| 17          | d            | 0.0388                    |
| 17          | e            | 0.0460                    |

Table B.2 Shear Stress from Preston Tube Calibration for 12 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | b     | 0.0239             | 14   | b     | 0.0230             |
| 4    | c     | 0.0211             | 14   | c     | 0.0361             |
| 4    | d     | 0.0223             | 14   | d     | 0.0490             |
| 4    | e     | 0.0248             | 14   | e     | 0.0395             |
| 4    | f     | 0.0175             | 14   | f     | 0.0303             |
| 5    | b     | 0.0273             | 15   | b     | 0.0266             |
| 5    | c     | 0.0267             | 15   | c     | 0.0367             |
| 5    | d     | 0.0244             | 15   | d     | 0.0498             |
| 5    | e     | 0.0246             | 15   | e     | 0.0454             |
| 5    | f     | 0.0175             | 15   | f     | 0.0390             |
| 6    | b     | 0.0227             | 16   | b     | 0.0287             |
| 6    | c     | 0.0238             | 16   | c     | 0.0385             |
| 6    | d     | 0.0209             | 16   | d     | 0.0471             |
| 6    | e     | 0.0210             | 16   | e     | 0.0481             |
| 6    | f     | 0.0172             | 16   | f     | 0.0498             |
| 7    | b     | 0.0250             | 17   | b     | 0.0224             |
| 7    | c     | 0.0205             | 17   | c     | 0.0321             |
| 7    | d     | 0.0185             | 17   | d     | 0.0457             |
| 7    | e     | 0.0152             | 17   | e     | 0.0539             |
| 7    | f     | 0.0148             | 17   | f     | 0.0453             |
| 8    | b     | 0.0274             |      |       |                    |
| 8    | c     | 0.0241             |      |       |                    |
| 8    | d     | 0.0170             |      |       |                    |
| 8    | e     | 0.0186             |      |       |                    |
| 8    | f     | 0.0143             |      |       |                    |
| 10   | b     | 0.0556             |      |       |                    |
| 10   | c     | 0.0555             |      |       |                    |
| 10   | d     | 0.0396             |      |       |                    |
| 10   | e     | 0.0320             |      |       |                    |
| 10   | f     | 0.0323             |      |       |                    |
| 11   | b     | 0.0352             |      |       |                    |
| 11   | c     | 0.0343             |      |       |                    |
| 11   | d     | 0.0452             |      |       |                    |
| 11   | e     | 0.0264             |      |       |                    |
| 11   | f     | 0.0192             |      |       |                    |
| 12   | b     | 0.0337             |      |       |                    |
| 12   | c     | 0.0496             |      |       |                    |
| 12   | d     | 0.0389             |      |       |                    |
| 12   | e     | 0.0334             |      |       |                    |
| 12   | f     | 0.0287             |      |       |                    |
| 13   | b     | 0.0307             |      |       |                    |
| 13   | c     | 0.0457             |      |       |                    |
| 13   | d     | 0.0430             |      |       |                    |
| 13   | e     | 0.0338             |      |       |                    |
| 13   | f     | 0.0313             |      |       |                    |

Table B.3 Shear Stress from Preston Tube Calibration for 16 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0299             | 11   | d     | 0.0617             |
| 4    | b     | 0.0266             | 11   | e     | 0.0331             |
| 4    | c     | 0.0258             | 11   | f     | 0.0297             |
| 4    | d     | 0.0260             | 11   | g     | 0.0271             |
| 4    | e     | 0.0285             | 12   | a     | 0.0429             |
| 4    | f     | 0.0234             | 12   | b     | 0.0483             |
| 4    | g     | 0.0165             | 12   | c     | 0.0568             |
| 5    | a     | 0.0335             | 12   | d     | 0.0579             |
| 5    | b     | 0.0343             | 12   | e     | 0.0444             |
| 5    | c     | 0.0261             | 12   | f     | 0.0455             |
| 5    | d     | 0.0271             | 12   | g     | 0.0380             |
| 5    | e     | 0.0289             | 13   | a     | 0.0075             |
| 5    | f     | 0.0251             | 13   | b     | 0.0494             |
| 5    | g     | 0.0185             | 13   | c     | 0.0555             |
| 6    | a     | 0.0311             | 13   | d     | 0.0487             |
| 6    | b     | 0.0346             | 13   | e     | 0.0429             |
| 6    | c     | 0.0270             | 13   | f     | 0.0415             |
| 6    | d     | 0.0283             | 13   | g     | 0.0397             |
| 6    | e     | 0.0280             | 14   | a     | 0.0129             |
| 6    | f     | 0.0238             | 14   | b     | 0.0232             |
| 6    | g     | 0.0198             | 14   | c     | 0.0417             |
| 7    | a     | 0.0321             | 14   | d     | 0.0469             |
| 7    | b     | 0.0290             | 14   | e     | 0.0317             |
| 7    | c     | 0.0259             | 14   | f     | 0.0249             |
| 7    | d     | 0.0285             | 14   | g     | 0.0256             |
| 7    | e     | 0.0251             | 15   | a     | 0.0174             |
| 7    | f     | 0.0219             | 15   | b     | 0.0248             |
| 7    | g     | 0.0162             | 15   | c     | 0.0397             |
| 8    | a     | 0.0243             | 15   | d     | 0.0488             |
| 8    | b     | 0.0278             | 15   | e     | 0.0476             |
| 8    | c     | 0.0293             | 15   | f     | 0.0377             |
| 8    | d     | 0.0280             | 15   | g     | 0.0361             |
| 8    | e     | 0.0259             | 16   | a     | 0.0142             |
| 8    | f     | 0.0188             | 16   | b     | 0.0263             |
| 8    | g     | 0.0158             | 16   | c     | 0.0375             |
| 10   | a     | 0.0678             | 16   | d     | 0.0488             |
| 10   | b     | 0.0630             | 16   | e     | 0.0551             |
| 10   | c     | 0.0700             | 16   | f     | 0.0472             |
| 10   | d     | 0.0445             | 16   | g     | 0.0351             |
| 10   | e     | 0.0428             | 17   | a     | 0.0160             |
| 10   | f     | 0.0408             | 17   | b     | 0.0264             |
| 10   | g     | 0.0395             | 17   | c     | 0.0283             |
| 11   | a     | 0.0454             | 17   | d     | 0.0455             |
| 11   | b     | 0.0543             | 17   | e     | 0.0722             |
| 11   | c     | 0.0691             | 17   | f     | 0.0599             |
|      |       |                    | 17   | g     | 0.0490             |

Table B.4 Shear Stress from Preston Tube Calibration for 20 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0240             | 11   | d     | 0.0505             |
| 4    | b     | 0.0213             | 11   | e     | 0.0213             |
| 4    | c     | 0.0170             | 11   | f     | 0.0209             |
| 4    | d     | 0.0210             | 11   | g     | 0.0249             |
| 4    | e     | 0.0268             | 12   | a     | 0.0262             |
| 4    | f     | 0.0198             | 12   | b     | 0.0397             |
| 4    | g     | 0.0151             | 12   | c     | 0.0455             |
| 5    | a     | 0.0299             | 12   | d     | 0.0461             |
| 5    | b     | 0.0265             | 12   | e     | 0.0366             |
| 5    | c     | 0.0194             | 12   | f     | 0.0333             |
| 5    | d     | 0.0192             | 12   | g     | 0.0336             |
| 5    | e     | 0.0252             | 13   | a     | 0.0230             |
| 5    | f     | 0.0197             | 13   | b     | 0.0337             |
| 5    | g     | 0.0150             | 13   | c     | 0.0515             |
| 6    | a     | 0.0265             | 13   | d     | 0.0426             |
| 6    | b     | 0.0273             | 13   | e     | 0.0294             |
| 6    | c     | 0.0196             | 13   | f     | 0.0317             |
| 6    | d     | 0.0195             | 13   | g     | 0.0327             |
| 6    | e     | 0.0219             | 14   | a     | 0.0198             |
| 6    | f     | 0.0199             | 14   | b     | 0.0327             |
| 6    | g     | 0.0123             | 14   | c     | 0.0445             |
| 7    | a     | 0.0193             | 14   | d     | 0.0410             |
| 7    | b     | 0.0242             | 14   | e     | 0.0322             |
| 7    | c     | 0.0212             | 14   | f     | 0.0257             |
| 7    | d     | 0.0219             | 14   | g     | 0.0289             |
| 7    | e     | 0.0186             | 15   | a     | 0.0252             |
| 7    | f     | 0.0210             | 15   | b     | 0.0314             |
| 7    | g     | 0.0119             | 15   | c     | 0.0395             |
| 8    | a     | 0.0194             | 15   | d     | 0.0426             |
| 8    | b     | 0.0260             | 15   | e     | 0.0397             |
| 8    | c     | 0.0392             | 15   | f     | 0.0472             |
| 8    | d     | 0.0186             | 15   | g     | 0.0419             |
| 8    | e     | 0.0177             | 16   | a     | 0.0200             |
| 8    | f     | 0.0099             | 16   | b     | 0.0296             |
| 8    | g     | 0.0080             | 16   | c     | 0.0490             |
| 10   | a     | 0.0630             | 16   | d     | 0.0420             |
| 10   | b     | 0.0514             | 16   | e     | 0.0397             |
| 10   | c     | 0.0674             | 16   | f     | 0.0499             |
| 10   | d     | 0.0493             | 16   | g     | 0.0420             |
| 10   | e     | 0.0381             | 17   | a     | 0.0188             |
| 10   | f     | 0.0349             | 17   | b     | 0.0287             |
| 10   | g     | 0.0339             | 17   | c     | 0.0360             |
| 11   | a     | 0.0399             | 17   | d     | 0.0441             |
| 11   | b     | 0.0459             | 17   | e     | 0.0549             |
| 11   | c     | 0.0562             | 17   | f     | 0.0420             |
|      |       |                    | 17   | g     | 0.0421             |

## **Appendix C. Linear Regression of Flow Velocity Profile**

Table C.1 Shear Stress ( $\tau_x$ ) from Linear Regression of Flow Velocity Profile for 8 cfs

| <b>XSEC</b> | <b>Piezo</b> | <b>Shear Stress (psf)</b> |
|-------------|--------------|---------------------------|
| <b>4</b>    | <b>c</b>     | 0.0030                    |
|             | <b>d</b>     | 0.0018                    |
|             | <b>e</b>     | 0.0011                    |
| <b>5</b>    | <b>c</b>     | 0.0027                    |
|             | <b>d</b>     | 0.0038                    |
|             | <b>e</b>     | 0.0009                    |
| <b>6</b>    | <b>c</b>     | 0.0034                    |
|             | <b>d</b>     | 0.0028                    |
|             | <b>e</b>     | 0.0006                    |
| <b>7</b>    | <b>c</b>     | 0.0036                    |
|             | <b>d</b>     | 0.0045                    |
|             | <b>e</b>     | 0.0010                    |
| <b>8</b>    | <b>c</b>     | 0.0037                    |
|             | <b>d</b>     | 0.0059                    |
|             | <b>e</b>     | 0.0000                    |
| <b>10</b>   | <b>c</b>     | 0.0063                    |
|             | <b>d</b>     | 0.0077                    |
|             | <b>e</b>     | 0.0041                    |
| <b>11</b>   | <b>c</b>     | 0.0115                    |
|             | <b>d</b>     | 0.0081                    |
|             | <b>e</b>     | 0.0067                    |
| <b>12</b>   | <b>c</b>     | 0.0055                    |
|             | <b>d</b>     | 0.0097                    |
|             | <b>e</b>     | 0.0041                    |
| <b>13</b>   | <b>c</b>     | 0.0044                    |
|             | <b>d</b>     | 0.0094                    |
|             | <b>e</b>     | 0.0070                    |
| <b>14</b>   | <b>c</b>     | 0.0030                    |
|             | <b>d</b>     | 0.0043                    |
|             | <b>e</b>     | 0.0064                    |
| <b>15</b>   | <b>c</b>     | 0.0006                    |
|             | <b>d</b>     | 0.0027                    |
|             | <b>e</b>     | 0.0049                    |
| <b>16</b>   | <b>c</b>     | 0.0007                    |
|             | <b>d</b>     | 0.0074                    |
|             | <b>e</b>     | 0.0094                    |
| <b>17</b>   | <b>c</b>     | 0.0007                    |
|             | <b>d</b>     | 0.0057                    |
|             | <b>e</b>     | 0.0061                    |

Table C.2 Shear Stress ( $\tau_x$ ) from Linear Regression of Flow Velocity Profile for 12  
cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | b     | 0.0033             | 14   | b     | 0.0034             |
| 4    | c     | 0.0036             | 14   | c     | 0.0046             |
| 4    | d     | 0.0035             | 14   | d     | 0.0163             |
| 4    | e     | 0.0008             | 14   | e     | 0.0089             |
| 4    | f     | 0.0008             | 14   | f     | 0.0071             |
| 5    | b     | 0.0007             | 15   | b     | 0.0014             |
| 5    | c     | 0.0036             | 15   | c     | 0.0022             |
| 5    | d     | 0.0037             | 15   | d     | 0.0137             |
| 5    | e     | 0.0013             | 15   | e     | 0.0140             |
| 5    | f     | 0.0002             | 15   | f     | 0.0051             |
| 6    | b     | 0.0025             | 16   | b     | 0.0003             |
| 6    | c     | 0.0036             | 16   | c     | 0.0005             |
| 6    | d     | 0.0056             | 16   | d     | 0.0223             |
| 6    | e     | 0.0018             | 16   | e     | 0.0111             |
| 6    | f     | 0.0014             | 16   | f     | 0.0047             |
| 7    | b     | 0.0028             | 17   | b     | 0.0003             |
| 7    | c     | 0.0043             | 17   | c     | 0.0021             |
| 7    | d     | 0.0055             | 17   | d     | 0.0121             |
| 7    | e     | 0.0001             | 17   | e     | 0.0101             |
| 7    | f     | 0.0014             | 17   | f     | 0.0118             |
| 8    | b     | 0.0015             |      |       |                    |
| 8    | c     | 0.0024             |      |       |                    |
| 8    | d     | 0.0042             |      |       |                    |
| 8    | e     | 0.0000             |      |       |                    |
| 8    | f     | 0.0005             |      |       |                    |
| 10   | b     | 0.0081             |      |       |                    |
| 10   | c     | 0.0079             |      |       |                    |
| 10   | d     | 0.0077             |      |       |                    |
| 10   | e     | 0.0017             |      |       |                    |
| 10   | f     | 0.0028             |      |       |                    |
| 11   | b     | 0.0149             |      |       |                    |
| 11   | c     | 0.0195             |      |       |                    |
| 11   | d     | 0.0118             |      |       |                    |
| 11   | e     | 0.0122             |      |       |                    |
| 11   | f     | 0.0013             |      |       |                    |
| 12   | b     | 0.0027             |      |       |                    |
| 12   | c     | 0.0030             |      |       |                    |
| 12   | d     | 0.0132             |      |       |                    |
| 12   | e     | 0.0129             |      |       |                    |
| 12   | f     | 0.0056             |      |       |                    |
| 13   | b     | 0.0043             |      |       |                    |
| 13   | c     | 0.0073             |      |       |                    |
| 13   | d     | 0.0188             |      |       |                    |
| 13   | e     | 0.0168             |      |       |                    |
| 13   | f     | 0.0052             |      |       |                    |

Table C.3 Shear Stress ( $\tau_x$ ) from Linear Regression of Flow Velocity Profile for 16  
cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0016             | 11   | d     | 0.0115             |
| 4    | b     | 0.0109             | 11   | e     | 0.0116             |
| 4    | c     | 0.0060             | 11   | f     | 0.0131             |
| 4    | d     | 0.0026             | 11   | g     | 0.0059             |
| 4    | e     | 0.0006             | 12   | a     | 0.0036             |
| 4    | f     | 0.0018             | 12   | b     | 0.0086             |
| 4    | g     | 0.0012             | 12   | c     | 0.0241             |
| 5    | a     | 0.0032             | 12   | d     | 0.0193             |
| 5    | b     | 0.0044             | 12   | e     | 0.0119             |
| 5    | c     | 0.0018             | 12   | f     | 0.0107             |
| 5    | d     | 0.0053             | 12   | g     | 0.0070             |
| 5    | e     | 0.0002             | 13   | a     | 0.0019             |
| 5    | f     | 0.0009             | 13   | b     | 0.0045             |
| 5    | g     | 0.0000             | 13   | c     | 0.0119             |
| 6    | a     | 0.0022             | 13   | d     | 0.0267             |
| 6    | b     | 0.0042             | 13   | e     | 0.0093             |
| 6    | c     | 0.0042             | 13   | f     | 0.0107             |
| 6    | d     | 0.0069             | 13   | g     | 0.0079             |
| 6    | e     | 0.0001             | 14   | a     | 0.0021             |
| 6    | f     | 0.0009             | 14   | b     | 0.0044             |
| 6    | g     | 0.0007             | 14   | c     | 0.0093             |
| 7    | a     | 0.0042             | 14   | d     | 0.0278             |
| 7    | b     | 0.0044             | 14   | e     | 0.0171             |
| 7    | c     | 0.0050             | 14   | f     | 0.0086             |
| 7    | d     | 0.0065             | 14   | g     | 0.0054             |
| 7    | e     | 0.0013             | 15   | a     | 0.0000             |
| 7    | f     | 0.0009             | 15   | b     | 0.0022             |
| 7    | g     | 0.0008             | 15   | c     | 0.0033             |
| 8    | a     | 0.0055             | 15   | d     | 0.0163             |
| 8    | b     | 0.0053             | 15   | e     | 0.0173             |
| 8    | c     | 0.0024             | 15   | f     | 0.0087             |
| 8    | d     | 0.0052             | 15   | g     | 0.0072             |
| 8    | e     | 0.0000             | 16   | a     | 0.0012             |
| 8    | f     | 0.0006             | 16   | b     | 0.0011             |
| 8    | g     | 0.0003             | 16   | c     | 0.0060             |
| 10   | a     | 0.0090             | 16   | d     | 0.0290             |
| 10   | b     | 0.0120             | 16   | e     | 0.0156             |
| 10   | c     | 0.0123             | 16   | f     | 0.0086             |
| 10   | d     | 0.0077             | 16   | g     | 0.0055             |
| 10   | e     | 0.0015             | 17   | a     | 0.0004             |
| 10   | f     | 0.0004             | 17   | b     | 0.0016             |
| 10   | g     | 0.0054             | 17   | c     | 0.0048             |
| 11   | a     | 0.0076             | 17   | d     | 0.0177             |
| 11   | b     | 0.0247             | 17   | e     | 0.0174             |
| 11   | c     | 0.0155             | 17   | f     | 0.0054             |
|      |       |                    | 17   | g     | 0.0006             |

Table C.4 Shear Stress ( $\tau_x$ ) from Linear Regression of Flow Velocity Profile for 20  
cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0116             | 11   | d     | 0.0121             |
| 4    | b     | 0.0030             | 11   | e     | 0.0177             |
| 4    | c     | 0.0038             | 11   | f     | 0.0280             |
| 4    | d     | 0.0030             | 11   | g     | 0.0282             |
| 4    | e     | 0.0000             | 12   | a     | 0.0154             |
| 4    | f     | 0.0001             | 12   | b     | 0.0280             |
| 4    | g     | 0.0027             | 12   | c     | 0.0375             |
| 5    | a     | 0.0054             | 12   | d     | 0.0133             |
| 5    | b     | 0.0036             | 12   | e     | 0.0212             |
| 5    | c     | 0.0024             | 12   | f     | 0.0143             |
| 5    | d     | 0.0118             | 12   | g     | 0.0091             |
| 5    | e     | 0.0005             | 13   | a     | 0.0093             |
| 5    | f     | 0.0003             | 13   | b     | 0.0015             |
| 5    | g     | 0.0004             | 13   | c     | 0.0554             |
| 6    | a     | 0.0042             | 13   | d     | 0.0301             |
| 6    | b     | 0.0083             | 13   | e     | 0.0168             |
| 6    | c     | 0.0024             | 13   | f     | 0.0149             |
| 6    | d     | 0.0094             | 13   | g     | 0.0164             |
| 6    | e     | 0.0016             | 14   | a     | 0.0089             |
| 6    | f     | 0.0019             | 14   | b     | 0.0047             |
| 6    | g     | 0.0031             | 14   | c     | 0.0070             |
| 7    | a     | 0.0099             | 14   | d     | 0.0355             |
| 7    | b     | 0.0064             | 14   | e     | 0.0265             |
| 7    | c     | 0.0013             | 14   | f     | 0.0187             |
| 7    | d     | 0.0066             | 14   | g     | 0.0145             |
| 7    | e     | 0.0001             | 15   | a     | 0.0024             |
| 7    | f     | 0.0017             | 15   | b     | 0.0050             |
| 7    | g     | 0.0004             | 15   | c     | 0.0045             |
| 8    | a     | 0.0040             | 15   | d     | 0.0455             |
| 8    | b     | 0.0060             | 15   | e     | 0.0226             |
| 8    | c     | 0.0026             | 15   | f     | 0.0233             |
| 8    | d     | 0.0019             | 15   | g     | 0.0148             |
| 8    | e     | 0.0005             | 16   | a     | 0.0003             |
| 8    | f     | 0.0002             | 16   | b     | 0.0003             |
| 8    | g     | 0.0002             | 16   | c     | 0.0002             |
| 10   | a     | 0.0461             | 16   | d     | 0.0467             |
| 10   | b     | 0.0044             | 16   | e     | 0.0157             |
| 10   | c     | 0.0075             | 16   | f     | 0.0151             |
| 10   | d     | 0.0077             | 16   | g     | 0.0141             |
| 10   | e     | 0.0004             | 17   | a     | 0.0011             |
| 10   | f     | 0.0010             | 17   | b     | 0.0011             |
| 10   | g     | 0.0027             | 17   | c     | 0.0000             |
| 11   | a     | 0.0756             | 17   | d     | 0.0377             |
| 11   | b     | 0.0079             | 17   | e     | 0.0313             |
| 11   | c     | 0.0313             | 17   | f     | 0.0262             |
|      |       |                    | 17   | g     | 0.0073             |

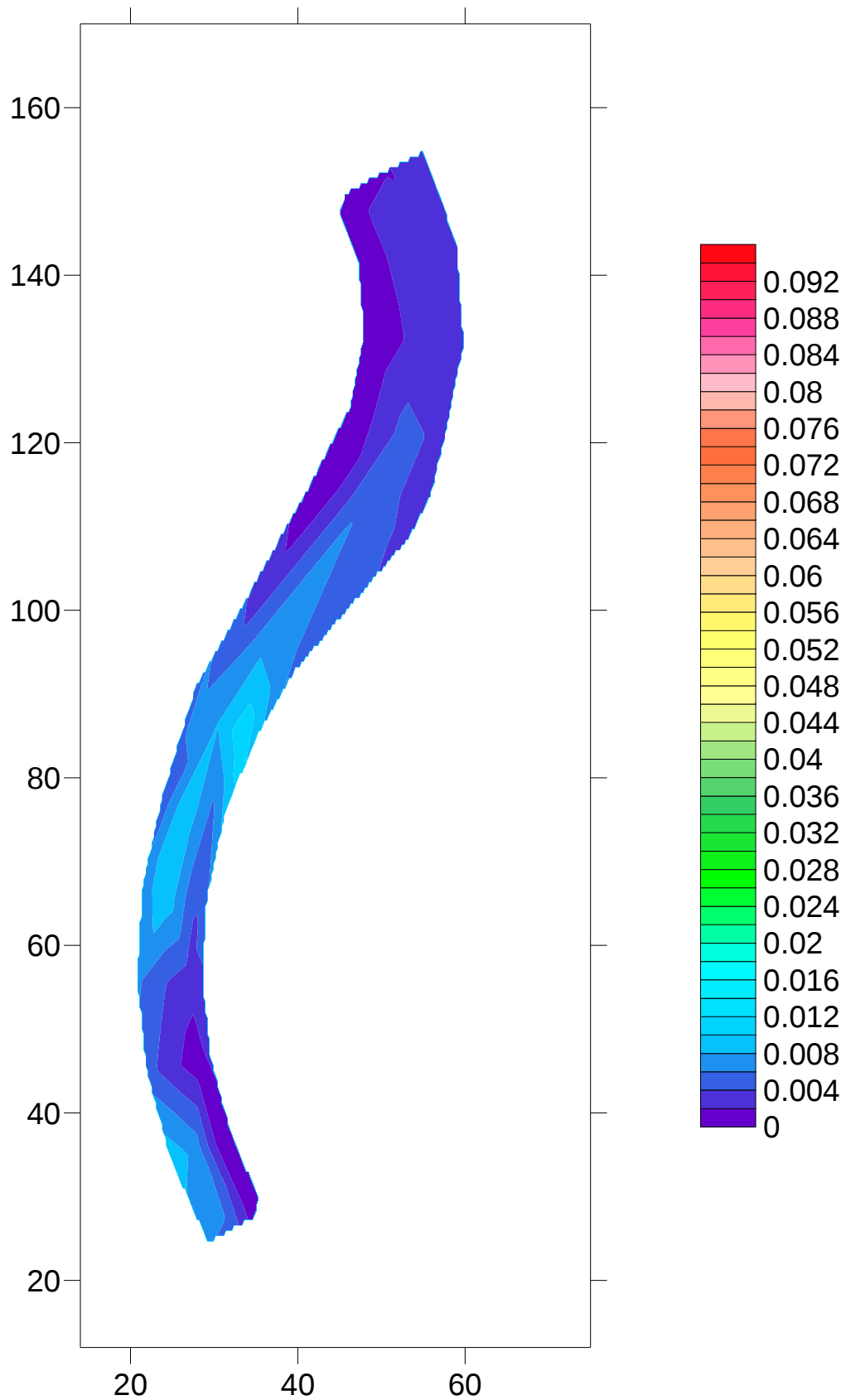


Figure C.1 Shear Stress Distribution  $\tau_x$ , by Linear Regression for 8 cfs (psf)

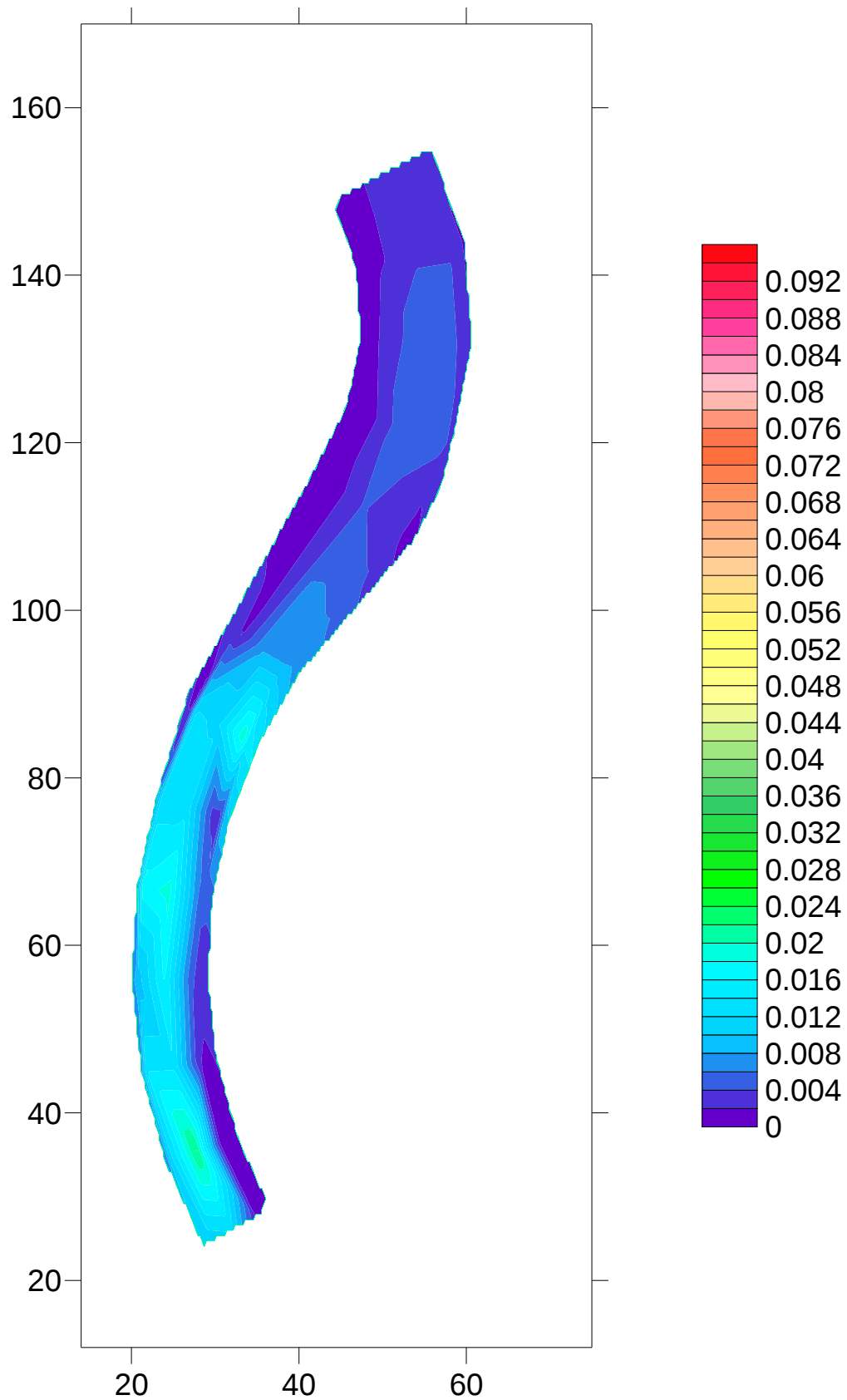


Figure C.2 Shear Stress Distribution  $\tau_x$ , by Linear Regression for 12 cfs (psf)

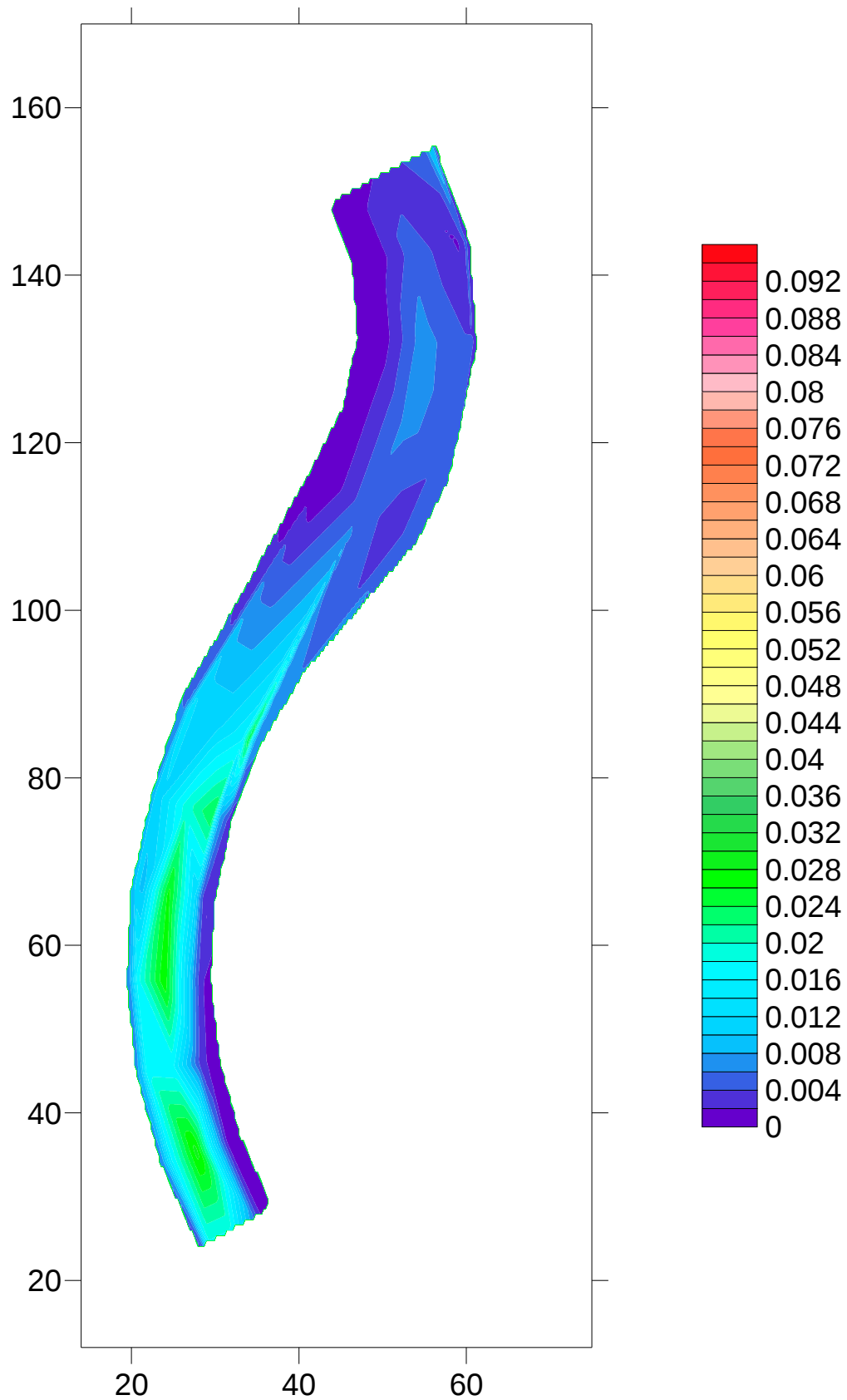


Figure C.3 Shear Stress Distribution,  $\tau_x$ , by Linear Regression for 16 cfs (psf)

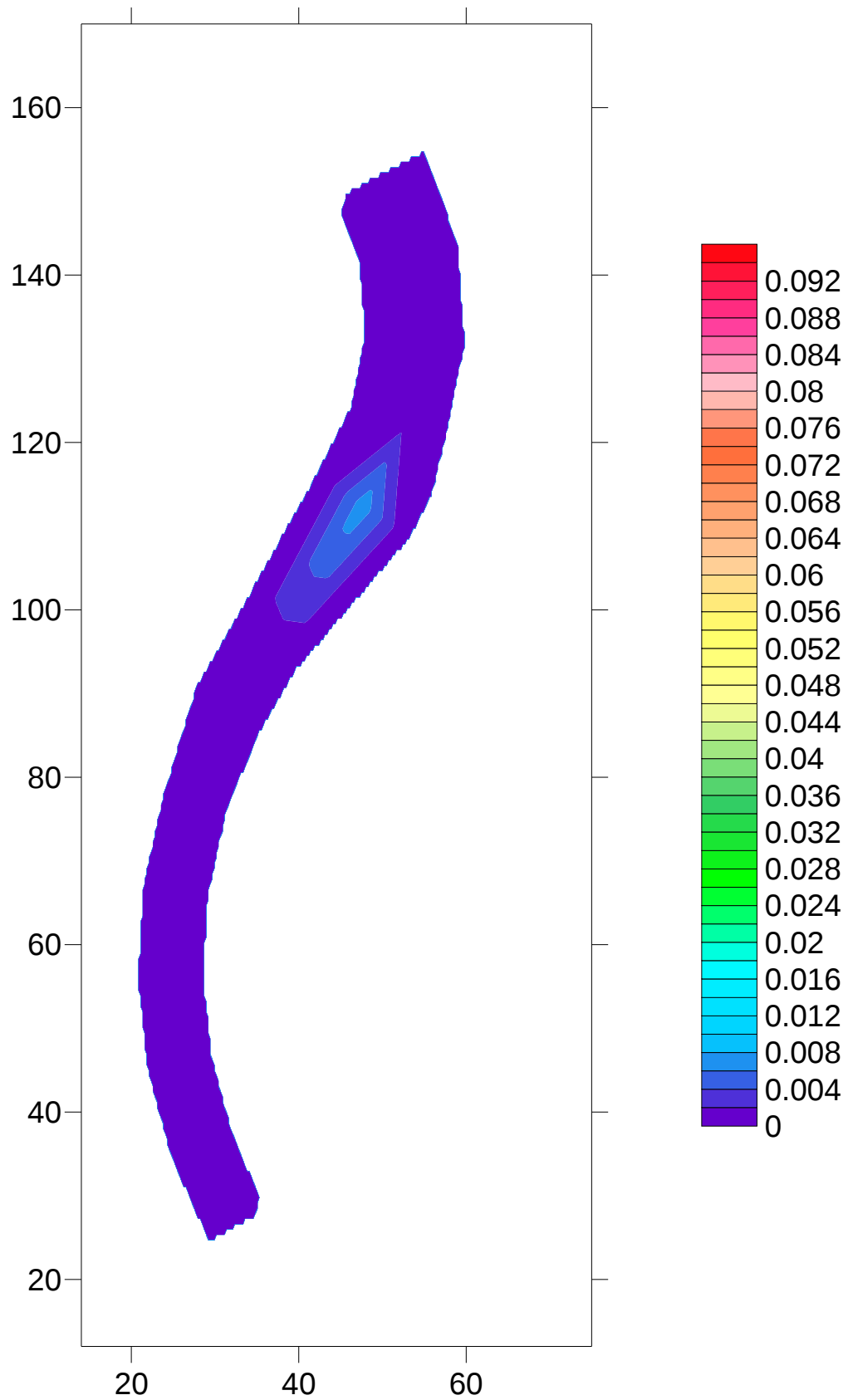


Figure C.4 Shear Stress Distribution,  $\tau_y$ , by Linear Regression for 8 cfs (psf)

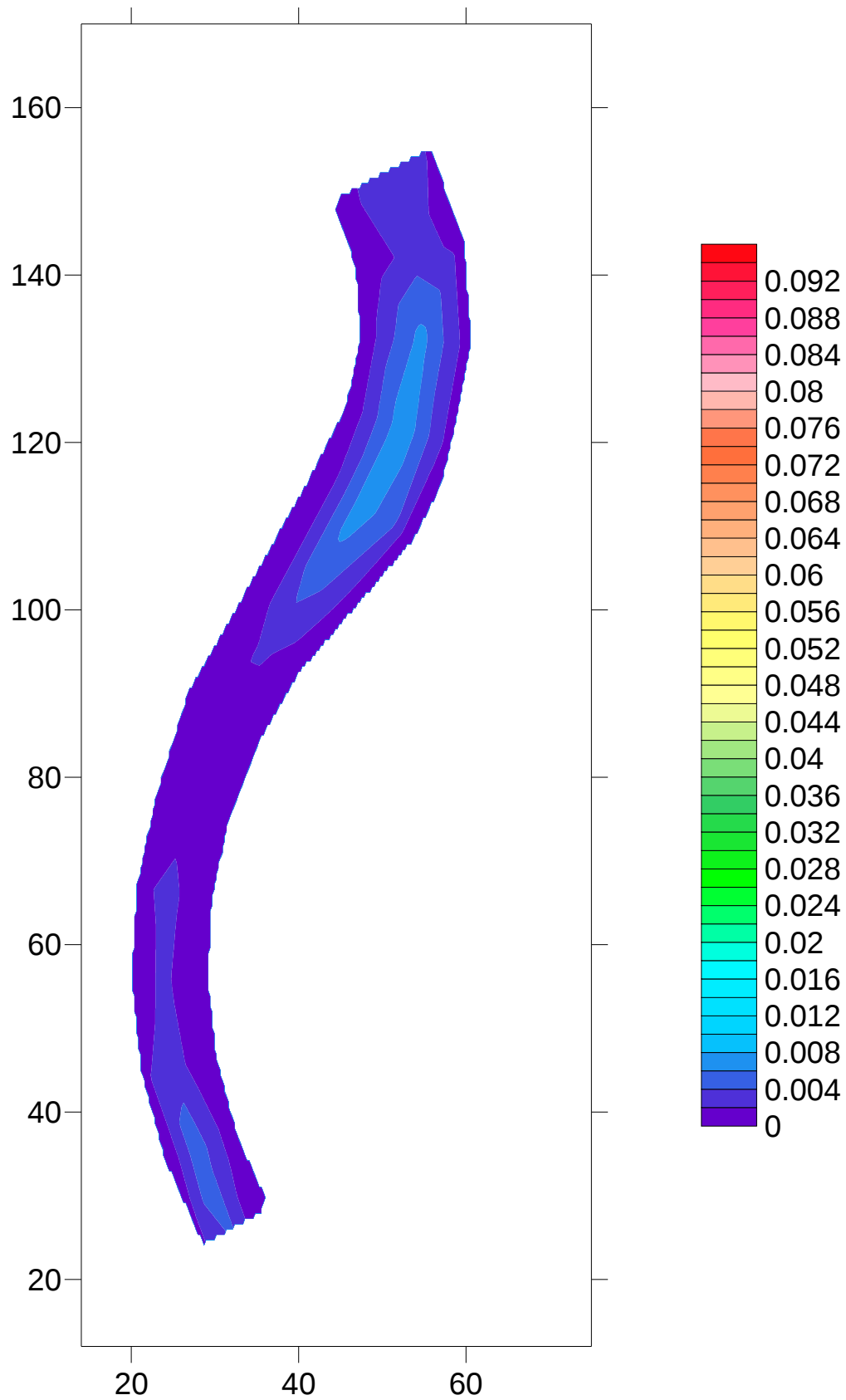


Figure C.5 Shear Stress Distribution,  $\tau_y$ , by Linear Regression for 12 cfs (psf)

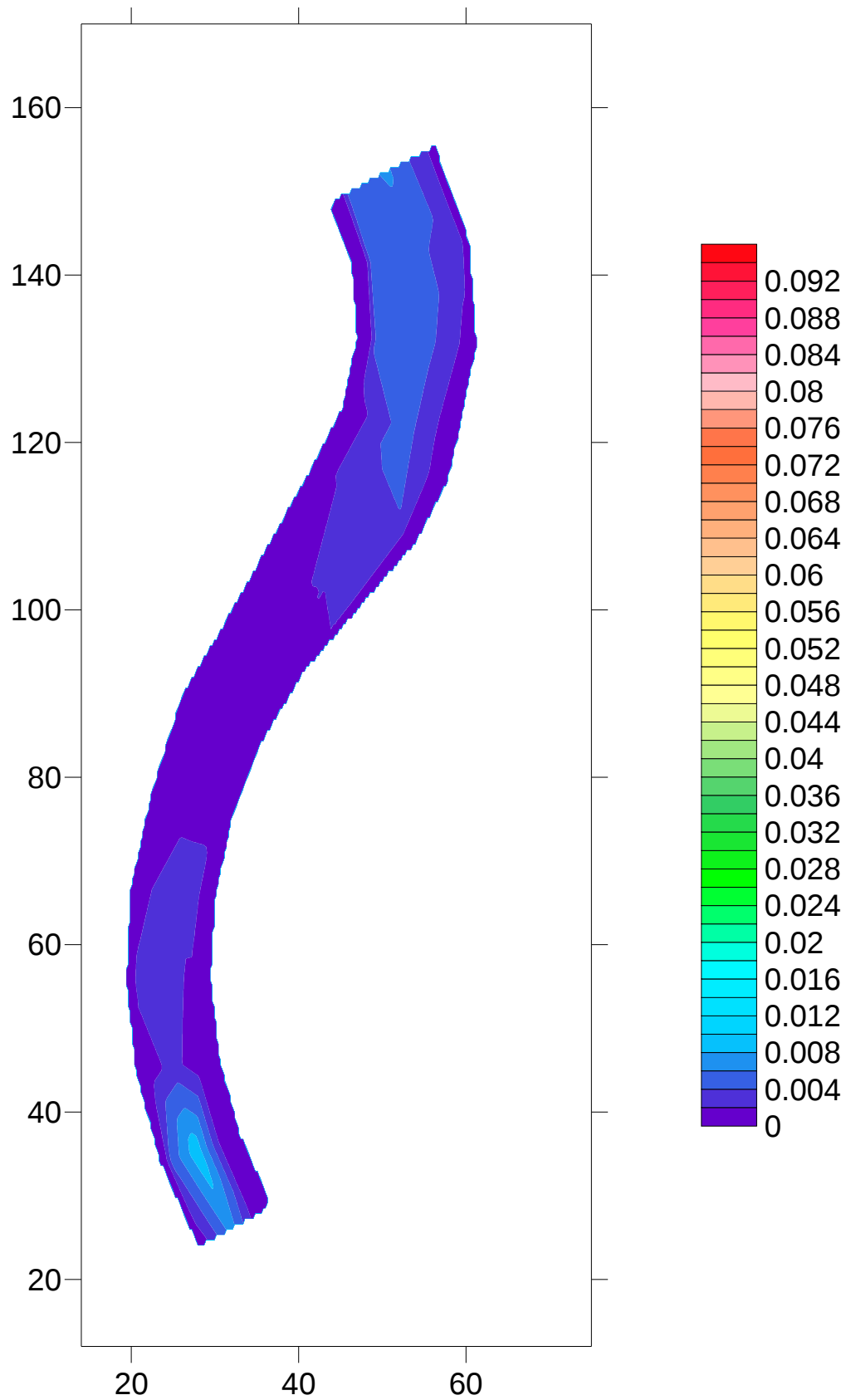


Figure C.6 Shear Stress Distribution,  $\tau_y$ , by Linear Regression for 16 cfs (psf)

## **Appendix D. Shear Stress from Rozovski (1961) Method**

Table D.1 Shear stress ( $\tau_v$ ) from Rozovskii (1961) Method for 8 cfs

| <b>XSEC</b> | <b>Piezo</b> | <b>Shear Stress (psf)</b> |
|-------------|--------------|---------------------------|
| 4           | c            | 0.0607                    |
| 4           | d            | 0.0683                    |
| 4           | e            | 0.0559                    |
| 5           | c            | 0.0090                    |
| 5           | d            | 0.0100                    |
| 5           | e            | 0.0104                    |
| 6           | c            | 0.0250                    |
| 6           | d            | 0.0247                    |
| 6           | e            | 0.0269                    |
| 7           | c            | -0.0218                   |
| 7           | d            | -0.0239                   |
| 7           | e            | -0.0135                   |
| 8           | c            | -0.0290                   |
| 8           | d            | -0.0314                   |
| 8           | e            | -0.0134                   |
| 10          | c            | -0.0478                   |
| 10          | d            | -0.0426                   |
| 10          | e            | -0.0344                   |
| 11          | c            | 0.0140                    |
| 11          | d            | 0.0145                    |
| 11          | e            | 0.0284                    |
| 12          | c            | 0.0347                    |
| 12          | d            | 0.0288                    |
| 12          | e            | 0.0367                    |
| 13          | c            | 0.0246                    |
| 13          | d            | 0.0200                    |
| 13          | e            | 0.0175                    |
| 14          | c            | 0.0054                    |
| 14          | d            | -0.0145                   |
| 14          | e            | -0.0093                   |
| 15          | c            | 0.0649                    |
| 15          | d            | 0.0547                    |
| 15          | e            | 0.0501                    |
| 16          | c            | 0.0383                    |
| 16          | d            | 0.0228                    |
| 16          | e            | 0.0188                    |
| 17          | c            | 0.0463                    |
| 17          | d            | 0.0280                    |
| 17          | e            | 0.0202                    |

Table D.2 Shear stress ( $\tau_v$ ) from Rozovskii (1961) Method for 12 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | b     | 0.0518             | 14   | b     | 0.0223             |
| 4    | c     | 0.0765             | 14   | c     | 0.0047             |
| 4    | d     | 0.0803             | 14   | d     | -0.0240            |
| 4    | e     | 0.0589             | 14   | e     | -0.0133            |
| 4    | f     | 0.0564             | 14   | f     | 0.0045             |
| 5    | b     | -0.0096            | 15   | b     | 0.0379             |
| 5    | c     | -0.0222            | 15   | c     | 0.0335             |
| 5    | d     | -0.0256            | 15   | d     | 0.0006             |
| 5    | e     | -0.0339            | 15   | e     | 0.0022             |
| 5    | f     | -0.0049            | 15   | f     | 0.0166             |
| 6    | b     | 0.0264             | 16   | b     | 0.0684             |
| 6    | c     | 0.0337             | 16   | c     | 0.0815             |
| 6    | d     | 0.0363             | 16   | d     | 0.0497             |
| 6    | e     | 0.0307             | 16   | e     | 0.0443             |
| 6    | f     | 0.0307             | 16   | f     | 0.0391             |
| 7    | b     | -0.0021            | 17   | b     | 0.1012             |
| 7    | c     | -0.0112            | 17   | c     | 0.1328             |
| 7    | d     | -0.0153            | 17   | d     | 0.1157             |
| 7    | e     | -0.0027            | 17   | e     | 0.0941             |
| 7    | f     | 0.0089             | 17   | f     | 0.0727             |
| 8    | b     | 0.0346             |      |       |                    |
| 8    | c     | 0.0397             |      |       |                    |
| 8    | d     | 0.0438             |      |       |                    |
| 8    | e     | 0.0639             |      |       |                    |
| 8    | f     | 0.0505             |      |       |                    |
| 10   | b     | -0.0074            |      |       |                    |
| 10   | c     | -0.0266            |      |       |                    |
| 10   | d     | -0.0068            |      |       |                    |
| 10   | e     | -0.0038            |      |       |                    |
| 10   | f     | 0.0043             |      |       |                    |
| 11   | b     | 0.0264             |      |       |                    |
| 11   | c     | 0.0176             |      |       |                    |
| 11   | d     | 0.0323             |      |       |                    |
| 11   | e     | 0.0460             |      |       |                    |
| 11   | f     | 0.0443             |      |       |                    |
| 12   | b     | 0.0240             |      |       |                    |
| 12   | c     | 0.0100             |      |       |                    |
| 12   | d     | 0.0050             |      |       |                    |
| 12   | e     | 0.0173             |      |       |                    |
| 12   | f     | 0.0239             |      |       |                    |
| 13   | b     | 0.0641             |      |       |                    |
| 13   | c     | 0.0659             |      |       |                    |
| 13   | d     | 0.0664             |      |       |                    |
| 13   | e     | 0.0694             |      |       |                    |
| 13   | f     | 0.0561             |      |       |                    |

Table D.3 Shear stress ( $\tau_v$ ) from Rozovskii (1961) Method for 16 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0273             | 11   | d     | 0.0004             |
| 4    | b     | 0.0324             | 11   | e     | 0.0199             |
| 4    | c     | 0.0453             | 11   | f     | 0.0269             |
| 4    | d     | 0.0504             | 11   | g     | 0.0238             |
| 4    | e     | 0.0163             | 12   | a     | 0.0106             |
| 4    | f     | 0.0372             | 12   | b     | 0.0162             |
| 4    | g     | 0.0368             | 12   | c     | 0.0231             |
| 5    | a     | 0.0181             | 12   | d     | 0.0247             |
| 5    | b     | 0.0186             | 12   | e     | 0.0234             |
| 5    | c     | 0.0266             | 12   | f     | 0.0167             |
| 5    | d     | 0.0289             | 12   | g     | 0.0112             |
| 5    | e     | 0.0085             | 13   | a     | 0.0526             |
| 5    | f     | 0.0239             | 13   | b     | 0.0626             |
| 5    | g     | 0.0261             | 13   | c     | 0.0384             |
| 6    | a     | 0.0386             | 13   | d     | 0.0417             |
| 6    | b     | 0.0478             | 13   | e     | 0.0516             |
| 6    | c     | 0.0651             | 13   | f     | 0.0495             |
| 6    | d     | 0.0598             | 13   | g     | 0.0409             |
| 6    | e     | 0.0546             | 14   | a     | 0.0316             |
| 6    | f     | 0.0535             | 14   | b     | 0.0316             |
| 6    | g     | 0.0438             | 14   | c     | 0.0070             |
| 7    | a     | -0.0084            | 14   | d     | -0.0208            |
| 7    | b     | -0.0203            | 14   | e     | 0.0265             |
| 7    | c     | -0.0317            | 14   | f     | 0.0070             |
| 7    | d     | -0.0396            | 14   | g     | 0.0154             |
| 7    | e     | -0.0310            | 15   | a     | 0.0261             |
| 7    | f     | -0.0049            | 15   | b     | 0.0206             |
| 7    | g     | 0.0061             | 15   | c     | 0.0000             |
| 8    | a     | 0.0208             | 15   | d     | -0.0425            |
| 8    | b     | 0.0208             | 15   | e     | -0.0368            |
| 8    | c     | 0.0229             | 15   | f     | -0.0144            |
| 8    | d     | 0.0203             | 15   | g     | 0.0039             |
| 8    | e     | 0.0518             | 16   | a     | 0.0709             |
| 8    | f     | 0.0467             | 16   | b     | 0.0972             |
| 8    | g     | 0.0380             | 16   | c     | 0.1124             |
| 10   | a     | -0.0258            | 16   | d     | 0.0768             |
| 10   | b     | -0.0639            | 16   | e     | 0.0652             |
| 10   | c     | -0.0958            | 16   | f     | 0.0575             |
| 10   | d     | -0.0722            | 16   | g     | 0.0485             |
| 10   | e     | -0.0590            | 17   | a     | 0.0259             |
| 10   | f     | -0.0234            | 17   | b     | 0.0246             |
| 10   | g     | -0.0067            | 17   | c     | 0.0101             |
| 11   | a     | 0.0587             | 17   | d     | -0.0374            |
| 11   | b     | -0.0001            | 17   | e     | -0.0476            |
| 11   | c     | -0.0197            | 17   | f     | -0.0152            |
|      |       |                    | 17   | g     | -0.0060            |

Table D.4 Shear stress ( $\tau_v$ ) from Rozovskii (1961) Method for 20 cfs

| XSEC | Piezo | Shear Stress (psf) | XSEC | Piezo | Shear Stress (psf) |
|------|-------|--------------------|------|-------|--------------------|
| 4    | a     | 0.0305             | 11   | d     | -0.0551            |
| 4    | b     | 0.0386             | 11   | e     | -0.0259            |
| 4    | c     | 0.0578             | 11   | f     | -0.0070            |
| 4    | d     | 0.0668             | 11   | g     | 0.0050             |
| 4    | e     | 0.0262             | 12   | a     | -0.0012            |
| 4    | f     | 0.0434             | 12   | b     | -0.0406            |
| 4    | g     | 0.0431             | 12   | c     | -0.1019            |
| 5    | a     | 0.0326             | 12   | d     | -0.0745            |
| 5    | b     | 0.0431             | 12   | e     | -0.0432            |
| 5    | c     | 0.0956             | 12   | f     | -0.0247            |
| 5    | d     | 0.0560             | 12   | g     | -0.0036            |
| 5    | e     | 0.0344             | 13   | a     | 0.0439             |
| 5    | f     | 0.0373             | 13   | b     | 0.0308             |
| 5    | g     | 0.0450             | 13   | c     | -0.0192            |
| 6    | a     | 0.0474             | 13   | d     | -0.0096            |
| 6    | b     | 0.0383             | 13   | e     | 0.0128             |
| 6    | c     | 0.0522             | 13   | f     | 0.0188             |
| 6    | d     | 0.0302             | 13   | g     | 0.0251             |
| 6    | e     | 0.0369             | 14   | a     | 0.0264             |
| 6    | f     | 0.0420             | 14   | b     | 0.0140             |
| 6    | g     | 0.0435             | 14   | c     | -0.0321            |
| 7    | a     | 0.0182             | 14   | d     | -0.0576            |
| 7    | b     | 0.0193             | 14   | e     | -0.0334            |
| 7    | c     | 0.0256             | 14   | f     | -0.0128            |
| 7    | d     | 0.0094             | 14   | g     | -0.0019            |
| 7    | e     | 0.0618             | 15   | a     | 0.0464             |
| 7    | f     | 0.0332             | 15   | b     | 0.0470             |
| 7    | g     | 0.0392             | 15   | c     | 0.0271             |
| 8    | a     | -0.0388            | 15   | d     | -0.0134            |
| 8    | b     | -0.0593            | 15   | e     | -0.0051            |
| 8    | c     | -0.0866            | 15   | f     | 0.0053             |
| 8    | d     | -0.0996            | 15   | g     | 0.0156             |
| 8    | e     | -0.0622            | 16   | a     | 0.0487             |
| 8    | f     | -0.0327            | 16   | b     | 0.0466             |
| 8    | g     | -0.0119            | 16   | c     | 0.0364             |
| 10   | a     | -0.0100            | 16   | d     | -0.0190            |
| 10   | b     | -0.0271            | 16   | e     | -0.0147            |
| 10   | c     | -0.0378            | 16   | f     | 0.0034             |
| 10   | d     | -0.0127            | 16   | g     | 0.0160             |
| 10   | e     | 0.0049             | 17   | a     | 0.0185             |
| 10   | f     | 0.0082             | 17   | b     | 0.0118             |
| 10   | g     | 0.0157             | 17   | c     | -0.0177            |
| 11   | a     | -0.0169            | 17   | d     | -0.0774            |
| 11   | b     | -0.0096            | 17   | e     | -0.0859            |
| 11   | c     | -0.0736            | 17   | f     | -0.0522            |
|      |       |                    | 17   | g     | -0.0231            |

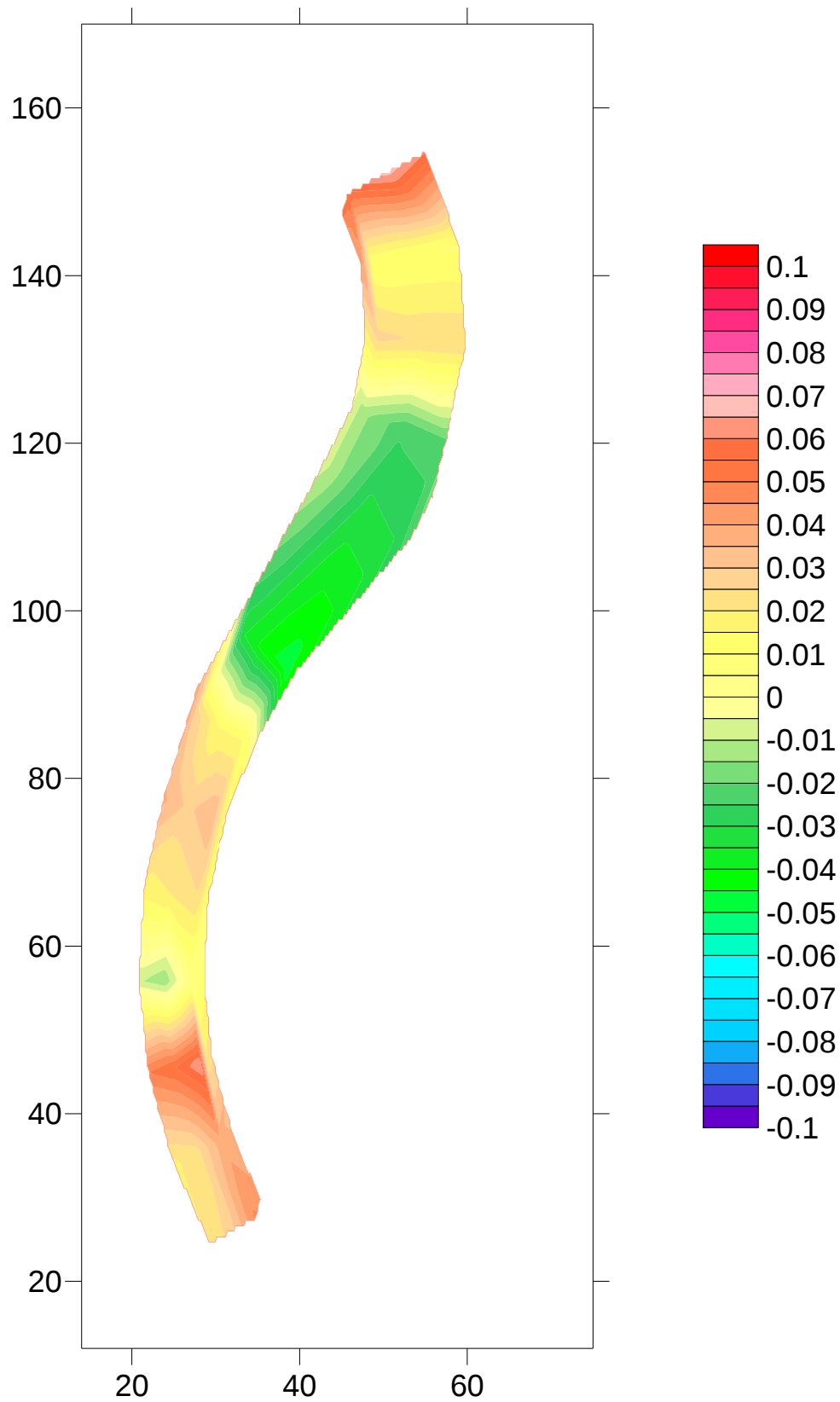


Figure D.1 Radial Shear Stress Distribution,  $\tau_r$ , from Rozovskii (1961) for 8 cfs (psf)

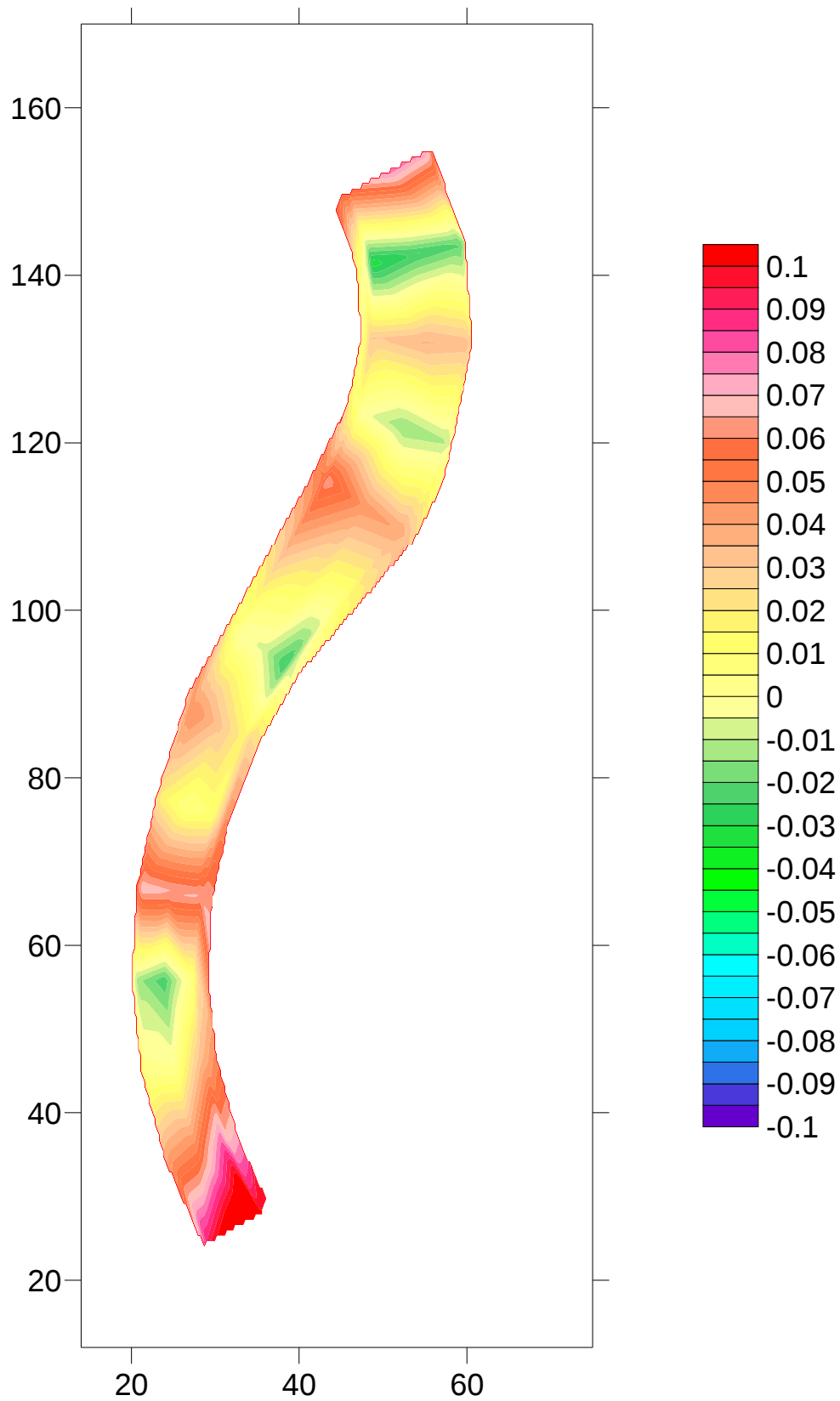


Figure D.2 Radial Shear Stress Distribution,  $\tau_r$ , from Rozovskii (1961) for 12 cfs (psf)

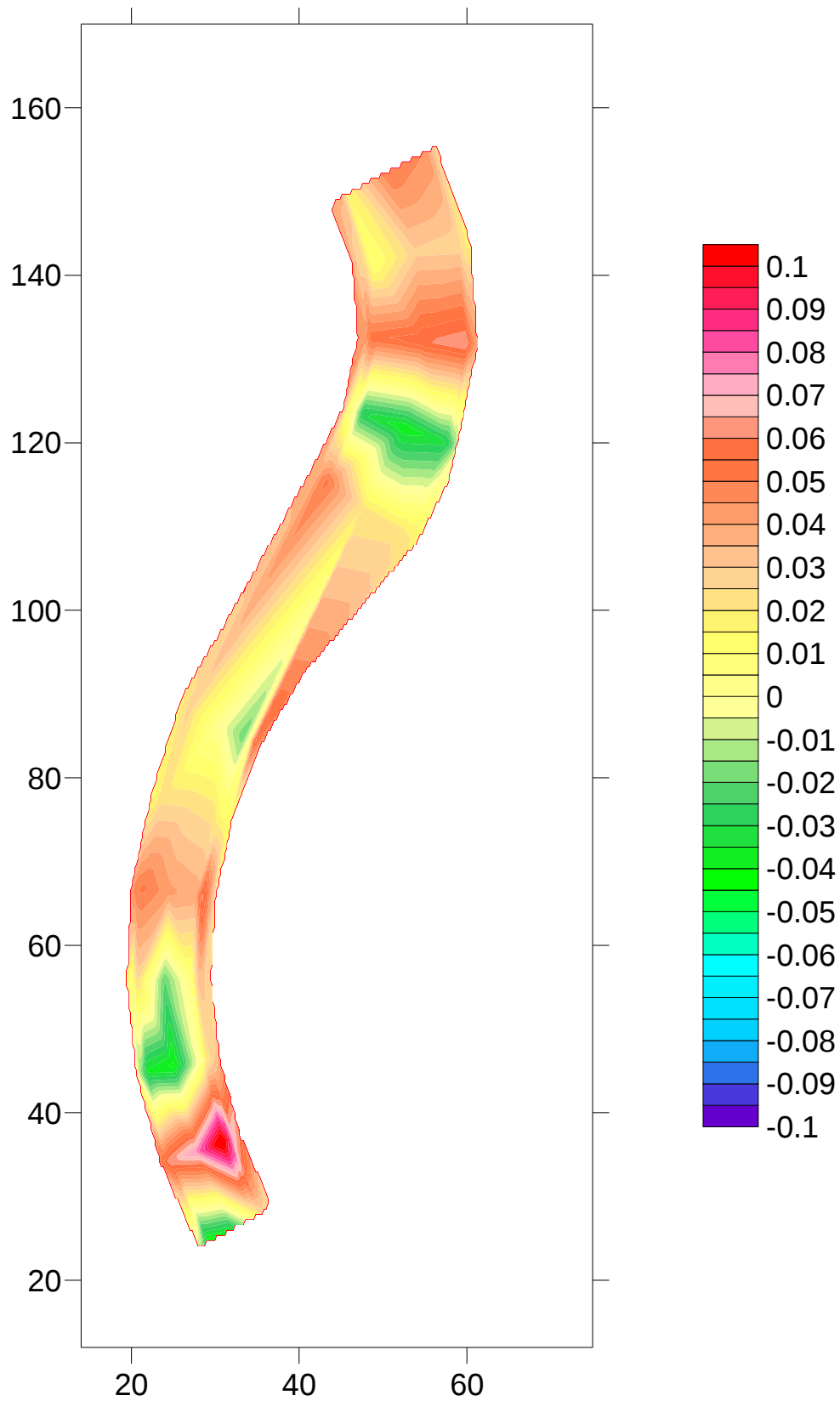
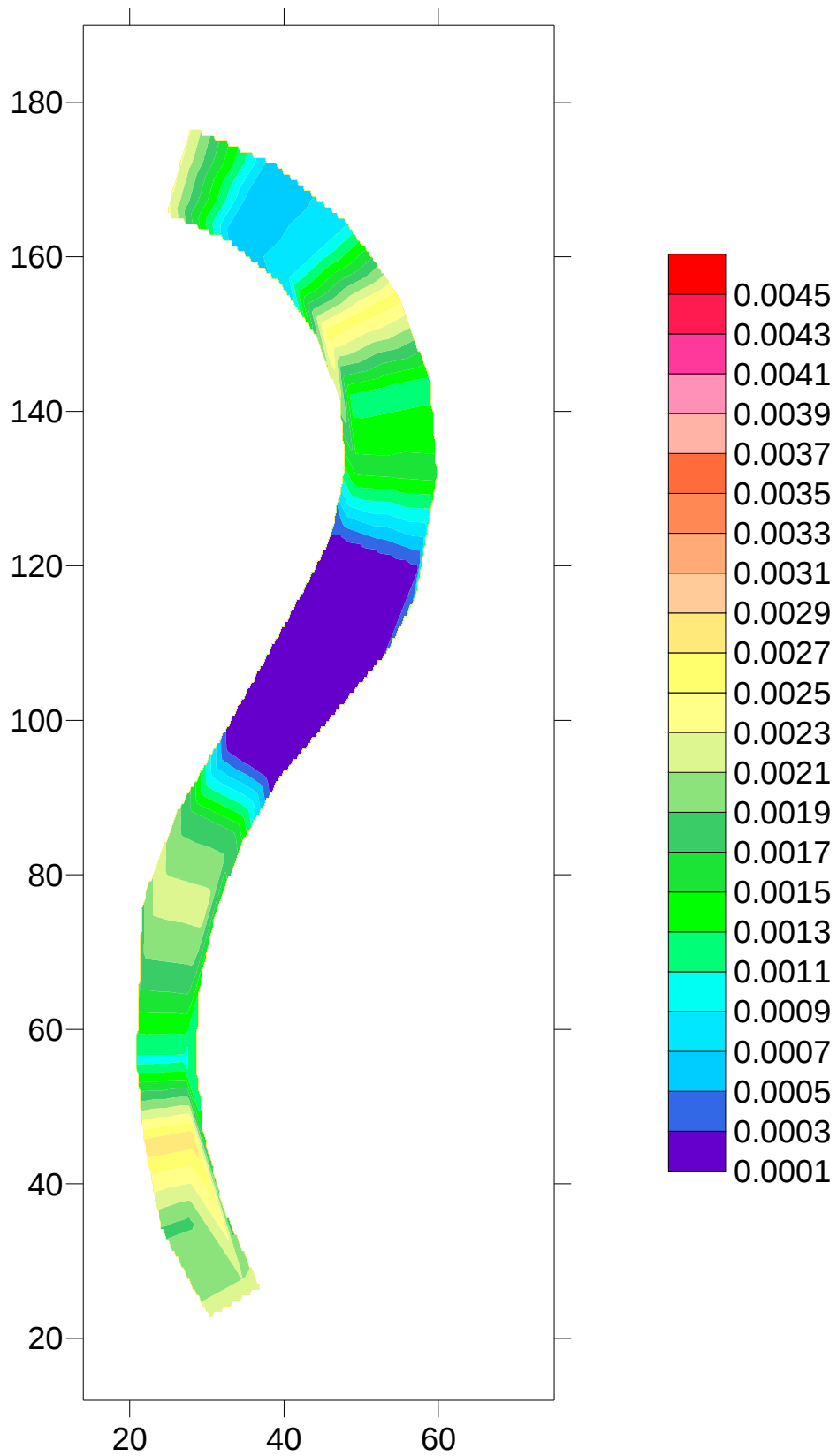


Figure D.3 Radial Shear Stress Distribution,  $\tau_r$ , from Rozovskii (1961) for 16 cfs (psf)



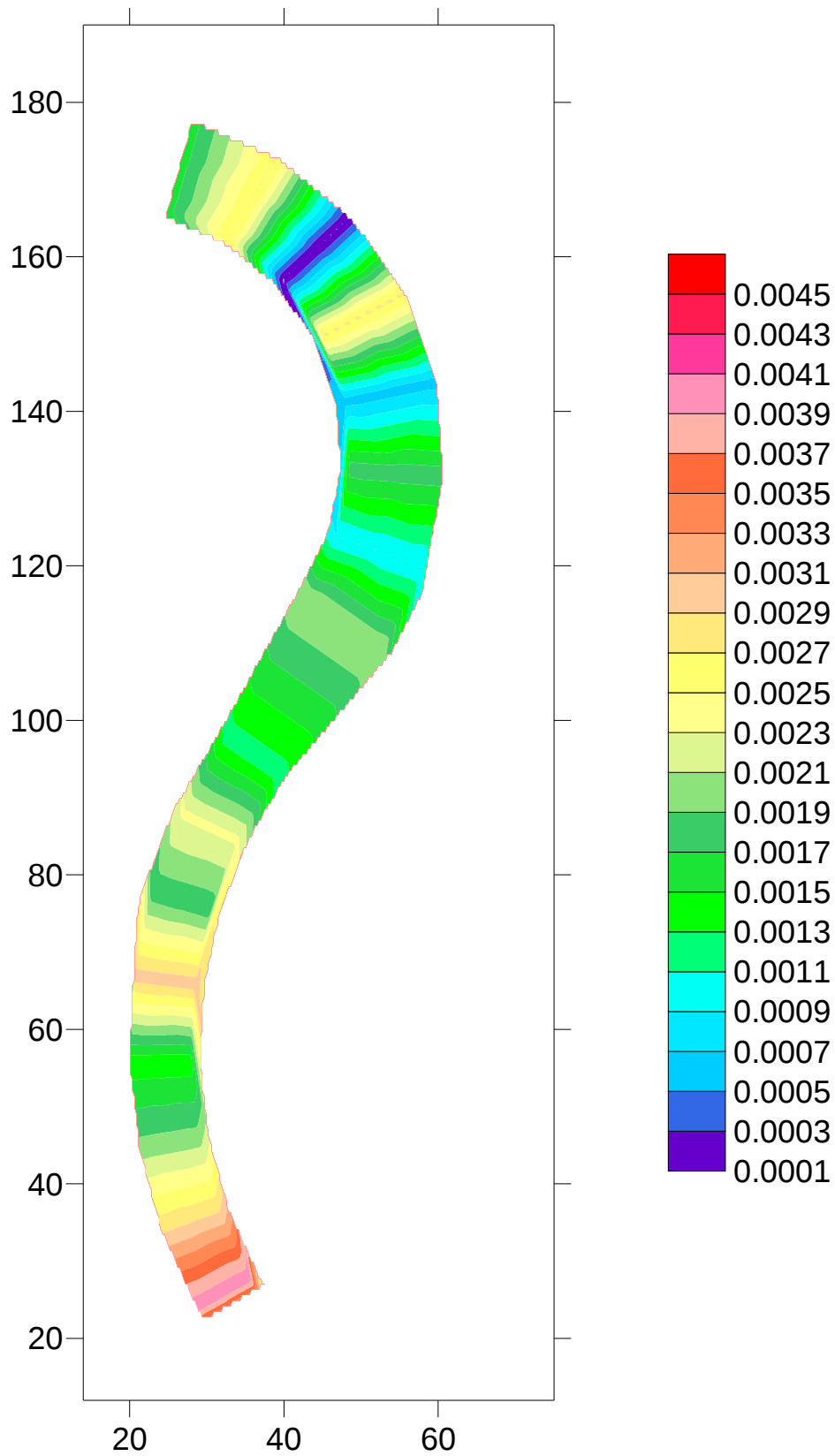


Figure D.5 Water Surface Slope Distribution for 12 cfs

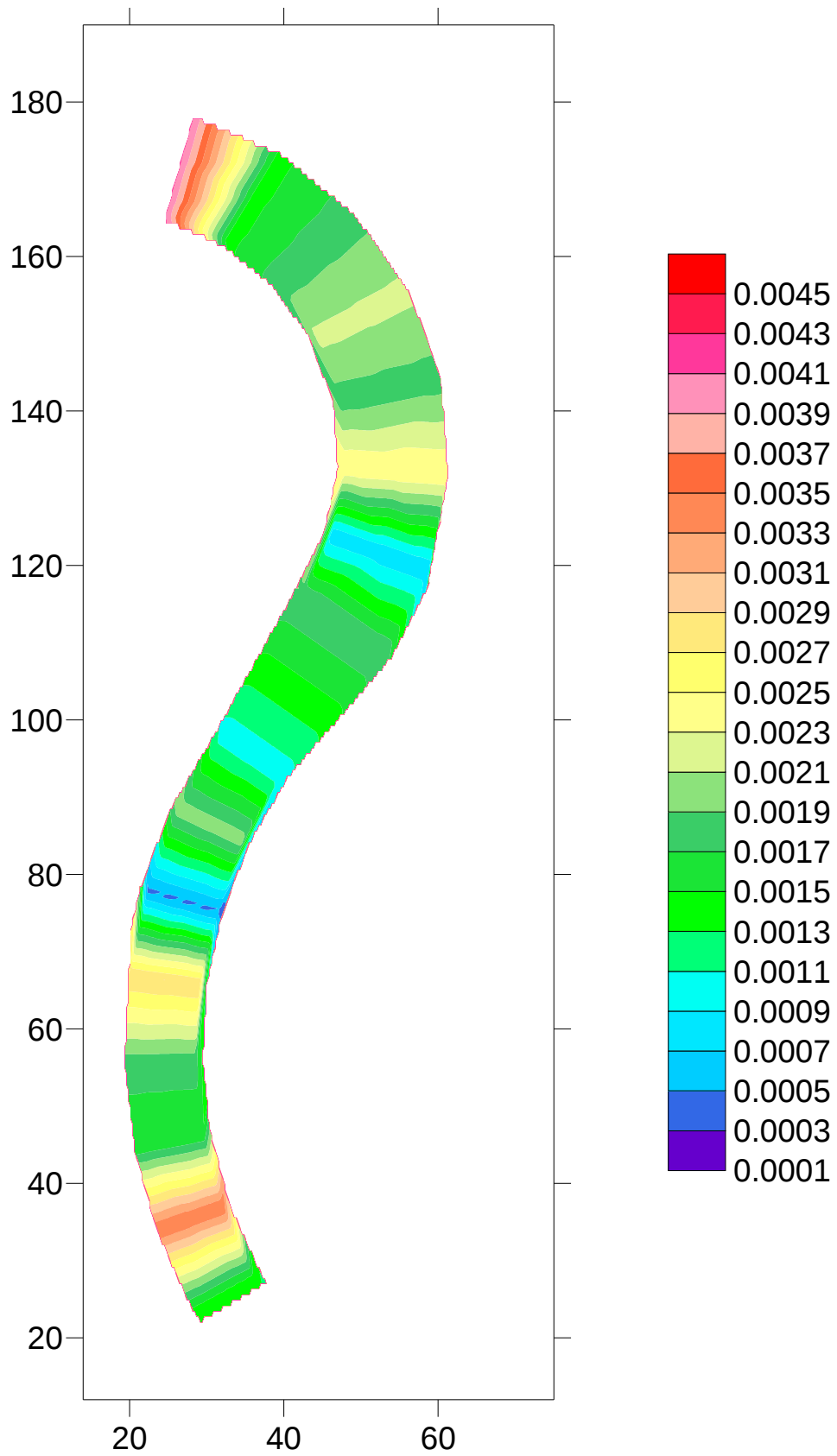


Figure D.6 Water Surface Slope Distribution for 16 cfs

## **Appendix E. Reynolds Shear Stress Extrapolation**

## E.1 Reynolds Shear Extrapolation

Appendix D shows the summary of the calculation result from Reynolds shear stress extrapolation. There are seven different columns in Table D.1 through Table D.9; Column 1 is the slope of linear regression equation of Reynolds shear stress profile,  $\tau_{xz}$ ; Column 2 is the intercept with y axis of the linear regression equation; Column 3 is the Reynolds shear stress, obtained from linear regression; and Column 4 through 6 is the same parameter of Reynolds shear stress; and Column 7 is bed shear stress computed from Equation 4.4. If Reynolds shear stress profile of  $\tau_{xz}$  or  $\tau_{zy}$  does not show similar trend with Figure 2.28, that data was presented as ‘out’ in Table E.1 through Table E.9.

Table E.1 Reynolds Shear Stress Calculation Summary for 8 cfs (psf)

|      | Column | 1        | 2     | 3           | 4         | 5      | 6           | 7            |
|------|--------|----------|-------|-------------|-----------|--------|-------------|--------------|
| XSEC | Piezo  | Slope    | b     | $\tau_{xz}$ | Slope     | b      | $\tau_{yz}$ | $\tau_{bed}$ |
| 4    | c      | -85.499  | 0.630 | 0.007       | 198.740   | 0.184  | -0.001      | 0.007        |
| 4    | d      | out      |       |             |           |        |             |              |
| 4    | e      | -74.965  | 0.508 | 0.007       | -210.300  | 0.679  | 0.003       | 0.008        |
| 5    | c      | -159.730 | 0.668 | 0.004       | 980.910   | 0.295  | 0.000       | 0.004        |
| 5    | d      | out      |       |             |           |        |             |              |
| 5    | e      | out      |       |             |           |        |             |              |
| 6    | c      | -159.730 | 0.668 | 0.004       | 980.910   | 0.295  | 0.000       | 0.004        |
| 6    | d      | out      |       |             |           |        |             |              |
| 6    | e      | out      |       |             |           |        |             |              |
| 7    | c      | out      |       |             |           |        |             |              |
| 7    | d      | out      |       |             |           |        |             |              |
| 7    | e      | out      |       |             |           |        |             |              |
| 8    | c      | out      |       |             |           |        |             |              |
| 8    | d      | out      |       |             |           |        |             |              |
| 8    | e      | -137.020 | 0.466 | 0.003       | -1720.500 | 0.595  | 0.000       | 0.003        |
| 10   | c      | out      |       |             |           |        |             |              |
| 10   | d      | -76.433  | 0.644 | 0.008       | 1017.000  | -0.052 | 0.000       | 0.008        |
| 10   | e      | out      |       |             |           |        |             |              |
| 11   | c      | -34.966  | 0.675 | 0.019       | 121.510   | 0.544  | -0.004      | 0.020        |
| 11   | d      | out      |       |             |           |        |             |              |
| 11   | e      | -56.983  | 0.607 | 0.011       | -349.550  | 0.570  | 0.002       | 0.011        |
| 12   | c      | -62.656  | 0.723 | 0.012       | 835.890   | 2.459  | -0.003      | 0.012        |
| 12   | d      | -60.051  | 0.756 | 0.013       | -225.230  | 0.168  | 0.001       | 0.013        |
| 12   | e      | -59.604  | 0.717 | 0.012       | -73.600   | 0.317  | 0.004       | 0.013        |
| 13   | c      | -45.212  | 0.588 | 0.013       | 113.030   | 0.669  | -0.006      | 0.014        |
| 13   | d      | -51.017  | 0.872 | 0.017       | -57.130   | 0.126  | 0.002       | 0.017        |
| 13   | e      | -67.681  | 0.779 | 0.012       | -174.290  | 0.532  | 0.003       | 0.012        |
| 14   | c      | -203.800 | 1.299 | 0.006       | -98.199   | 0.076  | 0.001       | 0.006        |
| 14   | d      | out      |       |             |           |        |             |              |
| 14   | e      | -54.947  | 0.727 | 0.013       | 31.162    | 0.125  | -0.004      | 0.014        |
| 15   | c      | -102.610 | 0.557 | 0.005       | 257.730   | 0.615  | -0.002      | 0.006        |
| 15   | d      | -137.450 | 1.853 | 0.013       | -150.880  | 0.060  | 0.000       | 0.013        |
| 15   | e      | -39.600  | 0.701 | 0.018       | -97.857   | 0.285  | 0.003       | 0.018        |
| 16   | c      | out      |       |             |           |        |             |              |
| 16   | d      | -32.438  | 0.732 | 0.023       | 237.930   | 0.655  | -0.003      | 0.023        |
| 16   | e      | out      |       |             |           |        |             |              |
| 17   | c      | out      |       |             |           |        |             |              |
| 17   | d      | -43.757  | 0.693 | 0.016       | -107.350  | 0.134  | 0.001       | 0.016        |
| 17   | e      | -47.680  | 0.741 | 0.016       | -86.199   | 0.325  | 0.004       | 0.016        |

Table E.2 Reynolds Shear Stress Calculation Summary of Upstream Bend for 12 cfs  
(psf)

|      | Column | 1        | 2     | 3           | 4        | 5      | 6           | 7            |
|------|--------|----------|-------|-------------|----------|--------|-------------|--------------|
| XSEC | Piezo  | Slope    | b     | $\tau_{xz}$ | Slope    | b      | $\tau_{yz}$ | $\tau_{bed}$ |
| 4    | b      | -19.205  | 0.432 | 0.022       | 158.380  | 0.382  | -0.002      | 0.023        |
| 4    | c      | -39.107  | 0.517 | 0.013       | -478.450 | 0.633  | 0.001       | 0.013        |
| 4    | d      | out      |       |             |          |        |             |              |
| 4    | e      | -50.955  | 0.516 | 0.010       | -98.052  | 0.584  | 0.006       | 0.012        |
| 4    | f      | out      |       |             |          |        |             |              |
| 5    | b      | out      |       |             |          |        |             |              |
| 5    | c      | -85.313  | 0.586 | 0.007       | 146.660  | 0.324  | -0.002      | 0.007        |
| 5    | d      | -120.490 | 0.684 | 0.006       | 128.660  | -0.016 | 0.000       | 0.006        |
| 5    | e      | -34.916  | 0.477 | 0.014       | -144.470 | 0.672  | 0.005       | 0.014        |
| 5    | f      | -129.830 | 0.501 | 0.004       | -188.650 | 0.607  | 0.003       | 0.005        |
| 6    | b      | -79.636  | 0.786 | 0.010       | 90.680   | 0.234  | -0.003      | 0.010        |
| 6    | c      | out      |       |             |          |        |             |              |
| 6    | d      | -137.420 | 0.942 | 0.007       | 95.307   | 0.125  | -0.001      | 0.007        |
| 6    | e      | -76.112  | 0.631 | 0.008       | -143.370 | 0.707  | 0.005       | 0.010        |
| 6    | f      | -111.540 | 0.448 | 0.004       | 241.340  | 0.089  | 0.000       | 0.004        |
| 7    | b      | -102.310 | 0.677 | 0.007       | 96.070   | 0.284  | -0.003      | 0.007        |
| 7    | c      | out      |       |             |          |        |             |              |
| 7    | d      | -66.081  | 0.695 | 0.011       | -62.375  | 0.747  | 0.012       | 0.016        |
| 7    | e      | -61.544  | 0.597 | 0.010       | -145.940 | 0.575  | 0.004       | 0.010        |
| 7    | f      | out      |       |             |          |        |             |              |
| 8    | b      | -65.609  | 0.501 | 0.008       | 73.638   | 0.306  | -0.004      | 0.009        |
| 8    | c      | -118.150 | 0.598 | 0.005       | 318.300  | 0.370  | -0.001      | 0.005        |
| 8    | d      | -127.520 | 0.785 | 0.006       | 173.020  | -0.142 | 0.001       | 0.006        |
| 8    | e      | -122.680 | 0.550 | 0.004       | -247.340 | 0.631  | 0.003       | 0.005        |
| 8    | f      | -180.860 | 0.420 | 0.002       | 337.130  | 0.045  | 0.000       | 0.002        |

Table E.3 Reynolds Shear Stress Calculation Summary of Downstream Bend for 12  
cfs (psf)

|      | Column | 1       | 2     | 3           | 4        | 5     | 6           | 7            |
|------|--------|---------|-------|-------------|----------|-------|-------------|--------------|
| XSEC | Piezo  | Slope   | b     | $\tau_{xz}$ | Slope    | b     | $\tau_{yz}$ | $\tau_{bed}$ |
| 10   | b      | -53.036 | 0.636 | 0.012       | 160.080  | 0.477 | -0.003      | 0.012        |
| 10   | c      | -43.527 | 0.422 | 0.010       | 179.770  | 0.405 | -0.002      | 0.010        |
| 10   | d      | -90.334 | 0.663 | 0.007       | 230.060  | 0.036 | 0.000       | 0.007        |
| 10   | e      | out     |       |             |          |       |             |              |
| 10   | f      | -69.233 | 0.514 | 0.007       | 139.520  | 0.029 | 0.000       | 0.007        |
| 11   | b      | out     |       |             |          |       |             |              |
| 11   | c      | -36.108 | 0.612 | 0.017       | 170.530  | 0.563 | -0.003      | 0.017        |
| 11   | d      | -60.498 | 0.652 | 0.011       | 69.190   | 0.332 | -0.005      | 0.012        |
| 11   | e      | -86.993 | 0.718 | 0.008       | -621.370 | 0.867 | 0.001       | 0.008        |
| 11   | f      | out     |       |             |          |       |             |              |
| 12   | b      | out     |       |             |          |       |             |              |
| 12   | c      | out     |       |             |          |       |             |              |
| 12   | d      | -46.024 | 0.760 | 0.017       | 396.510  | 0.309 | -0.001      | 0.017        |
| 12   | e      | -52.546 | 0.696 | 0.013       | -59.134  | 0.345 | 0.006       | 0.014        |
| 12   | f      | out     |       |             |          |       |             |              |
| 13   | b      | -46.268 | 0.459 | 0.010       | -90.676  | 0.120 | 0.001       | 0.010        |
| 13   | c      | -30.808 | 0.640 | 0.021       | 72.360   | 0.658 | -0.009      | 0.023        |
| 13   | d      | -60.780 | 1.010 | 0.017       | 192.070  | 0.667 | -0.003      | 0.017        |
| 13   | e      | -46.912 | 0.731 | 0.016       | -114.080 | 0.461 | 0.004       | 0.016        |
| 13   | f      | -32.038 | 0.489 | 0.015       | -57.870  | 0.429 | 0.007       | 0.017        |
| 14   | b      | out     |       |             |          |       |             |              |
| 14   | c      | -35.097 | 0.556 | 0.016       | 86.888   | 0.707 | -0.008      | 0.018        |
| 14   | d      | -48.936 | 1.025 | 0.021       | 230.900  | 1.032 | -0.004      | 0.021        |
| 14   | e      | -65.275 | 0.891 | 0.014       | -74.848  | 0.373 | 0.005       | 0.015        |
| 14   | f      | out     |       |             |          |       |             |              |
| 15   | b      | out     |       |             |          |       |             |              |
| 15   | c      | out     |       |             |          |       |             |              |
| 15   | d      | out     |       |             |          |       |             |              |
| 15   | e      | -63.118 | 0.719 | 0.011       | -93.491  | 0.488 | 0.005       | 0.013        |
| 15   | f      | out     |       |             |          |       |             |              |
| 16   | b      | -37.227 | 0.414 | 0.011       | -179.480 | 0.009 | 0.000       | 0.011        |
| 16   | c      | -32.074 | 0.477 | 0.015       | 179.940  | 0.795 | -0.004      | 0.016        |
| 16   | d      | -27.345 | 0.862 | 0.032       | 92.003   | 0.884 | -0.010      | 0.033        |
| 16   | e      | -42.445 | 0.846 | 0.020       | -68.900  | 0.533 | 0.008       | 0.021        |
| 16   | f      | out     |       |             |          |       |             |              |
| 17   | b      | -59.835 | 0.456 | 0.008       | 355.190  | 0.734 | -0.002      | 0.008        |
| 17   | c      | out     |       |             |          |       |             |              |
| 17   | d      | out     |       |             |          |       |             |              |
| 17   | e      | -33.915 | 0.605 | 0.018       | -98.617  | 0.680 | 0.007       | 0.019        |
| 17   | f      | out     |       |             |          |       |             |              |

Table E.4 Reynolds Shear Stress Calculation Summary of Upstream Bend for 16 cfs  
(psf)

|      | Column | 1        | 2     | 3           | 4        | 5      | 6           | 7            |
|------|--------|----------|-------|-------------|----------|--------|-------------|--------------|
| XSEC | Piezo  | Slope    | b     | $\tau_{xz}$ | Slope    | b      | $\tau_{yz}$ | $\tau_{bed}$ |
| 4    | a      | -41.251  | 0.597 | 0.014       | 15.382   | 0.298  | -0.019      | 0.024        |
| 4    | b      | -23.399  | 0.376 | 0.016       | 135.440  | 0.323  | -0.002      | 0.016        |
| 4    | c      | -13.906  | 0.263 | 0.019       | 28.790   | 0.201  | -0.007      | 0.020        |
| 4    | d      | -39.013  | 0.409 | 0.010       | -201.050 | 0.865  | 0.004       | 0.011        |
| 4    | e      | -33.259  | 0.419 | 0.013       | -74.613  | 0.452  | 0.006       | 0.014        |
| 4    | f      | out      |       |             |          |        |             |              |
| 4    | g      | out      |       |             |          |        |             |              |
| 5    | a      | -110.960 | 1.055 | 0.010       | 43.892   | 0.342  | -0.008      | 0.012        |
| 5    | b      | -41.011  | 0.480 | 0.012       | 96.719   | 0.312  | -0.003      | 0.012        |
| 5    | c      | out      |       |             |          |        |             |              |
| 5    | d      | out      |       |             |          |        |             |              |
| 5    | e      | -64.555  | 0.566 | 0.009       | -86.411  | 0.509  | 0.006       | 0.011        |
| 5    | f      | out      |       |             |          |        |             |              |
| 5    | g      | out      |       |             |          |        |             |              |
| 6    | a      | out      |       |             |          |        |             |              |
| 6    | b      | -80.810  | 0.628 | 0.008       | 180.710  | 0.577  | -0.003      | 0.008        |
| 6    | c      | -74.016  | 0.485 | 0.007       | 125.430  | 0.272  | -0.002      | 0.007        |
| 6    | d      | out      |       |             |          |        |             |              |
| 6    | e      | -43.589  | 0.539 | 0.012       | -71.690  | 0.491  | 0.007       | 0.014        |
| 6    | f      | -99.020  | 0.574 | 0.006       | -113.330 | 0.611  | 0.005       | 0.008        |
| 6    | g      | -171.370 | 0.475 | 0.003       | 407.430  | -0.153 | 0.000       | 0.003        |
| 7    | a      | out      |       |             |          |        |             |              |
| 7    | b      | out      |       |             |          |        |             |              |
| 7    | c      | -47.538  | 0.398 | 0.008       | 78.854   | 0.170  | -0.002      | 0.009        |
| 7    | d      | out      |       |             |          |        |             |              |
| 7    | e      | -67.955  | 0.522 | 0.008       | -189.170 | 0.679  | 0.004       | 0.008        |
| 7    | f      | out      |       |             |          |        |             |              |
| 7    | g      | out      |       |             |          |        |             |              |
| 8    | a      | -27.059  | 0.440 | 0.016       | 227.180  | 0.603  | -0.003      | 0.016        |
| 8    | b      | -89.206  | 0.679 | 0.008       | 172.470  | 0.312  | -0.002      | 0.008        |
| 8    | c      | out      |       |             |          |        |             |              |
| 8    | d      | -66.188  | 0.546 | 0.008       | 80.191   | 0.055  | -0.001      | 0.008        |
| 8    | e      | -66.734  | 0.470 | 0.007       | -198.710 | 0.585  | 0.003       | 0.008        |
| 8    | f      | out      |       |             |          |        |             |              |
| 8    | g      | out      |       |             |          |        |             |              |

Table E.5 Reynolds Shear Stress Calculation Summary of XS 10 ~ XS 15 for 16 cfs  
(psf)

|      | Column | 1        | 2     | 3           | 4        | 5      | 6           | 7            |
|------|--------|----------|-------|-------------|----------|--------|-------------|--------------|
| XSEC | Piezo  | Slope    | b     | $\tau_{xz}$ | Slope    | b      | $\tau_{yz}$ | $\tau_{bed}$ |
| 10   | a      | -49.208  | 0.695 | 0.014       | -145.130 | 0.058  | 0.000       | 0.014        |
| 10   | b      | -21.206  | 0.404 | 0.019       | 202.930  | 0.522  | -0.003      | 0.019        |
| 10   | c      | -15.326  | 0.323 | 0.021       | 212.810  | 0.433  | -0.002      | 0.021        |
| 10   | d      | -56.462  | 0.696 | 0.012       | -207.880 | 0.890  | 0.004       | 0.013        |
| 10   | e      | -70.256  | 0.529 | 0.008       | -298.600 | 0.701  | 0.002       | 0.008        |
| 10   | f      | -42.268  | 0.399 | 0.009       | 151.360  | 0.093  | -0.001      | 0.009        |
| 10   | g      | out      |       |             |          |        |             |              |
| 11   | a      | -27.333  | 0.462 | 0.017       | -100.770 | -0.034 | 0.000       | 0.017        |
| 11   | b      | -19.721  | 0.669 | 0.034       | 93.748   | 0.621  | -0.007      | 0.035        |
| 11   | c      | -19.130  | 0.468 | 0.024       | 87.194   | 0.414  | -0.005      | 0.025        |
| 11   | d      | -53.413  | 0.694 | 0.013       | 175.230  | 0.350  | -0.002      | 0.013        |
| 11   | e      | out      |       |             |          |        |             |              |
| 11   | f      | -41.670  | 0.681 | 0.016       | -155.000 | 0.514  | 0.003       | 0.017        |
| 11   | g      | out      |       |             |          |        |             |              |
| 12   | a      | -347.220 | 2.035 | 0.006       | -110.420 | 0.078  | 0.001       | 0.006        |
| 12   | b      | -25.429  | 0.542 | 0.021       | -56.215  | -0.068 | -0.001      | 0.021        |
| 12   | c      | -31.288  | 0.658 | 0.021       | 98.299   | 0.610  | -0.006      | 0.022        |
| 12   | d      | out      |       |             |          |        |             |              |
| 12   | e      | -44.729  | 0.626 | 0.014       | -60.891  | 0.271  | 0.004       | 0.015        |
| 12   | f      | -20.463  | 0.458 | 0.022       | -78.113  | 0.378  | 0.005       | 0.023        |
| 12   | g      | out      |       |             |          |        |             |              |
| 13   | a      | -94.605  | 0.631 | 0.007       | 260.210  | 0.570  | -0.002      | 0.007        |
| 13   | b      | out      |       |             |          |        |             |              |
| 13   | c      | -17.961  | 0.611 | 0.034       | 78.781   | 0.799  | -0.010      | 0.035        |
| 13   | d      | -21.909  | 0.745 | 0.034       | 133.100  | 0.640  | -0.005      | 0.034        |
| 13   | e      | -30.917  | 0.700 | 0.023       | -103.550 | 0.350  | 0.003       | 0.023        |
| 13   | f      | out      |       |             |          |        |             |              |
| 13   | g      | out      |       |             |          |        |             |              |
| 14   | a      | -61.407  | 0.601 | 0.010       | 216.920  | 0.581  | -0.003      | 0.010        |
| 14   | b      | -49.525  | 0.582 | 0.012       | -98.922  | -0.051 | -0.001      | 0.012        |
| 14   | c      | -19.658  | 0.549 | 0.028       | 146.640  | 0.817  | -0.006      | 0.028        |
| 14   | d      | -24.346  | 0.824 | 0.034       | -65.408  | 0.159  | 0.002       | 0.034        |
| 14   | e      | -31.980  | 0.788 | 0.025       | -86.134  | 0.370  | 0.004       | 0.025        |
| 14   | f      | out      |       |             |          |        |             |              |
| 14   | g      | out      |       |             |          |        |             |              |
| 15   | a      | out      |       |             |          |        |             |              |
| 15   | b      | -47.069  | 0.432 | 0.009       | 60.839   | 0.368  | -0.006      | 0.011        |
| 15   | c      | -39.447  | 0.548 | 0.014       | 145.200  | 0.712  | -0.005      | 0.015        |
| 15   | d      | -27.061  | 0.833 | 0.031       | -67.040  | 0.211  | 0.003       | 0.031        |
| 15   | e      | -26.746  | 0.666 | 0.025       | -76.329  | 0.436  | 0.006       | 0.026        |
| 15   | f      | out      |       |             |          |        |             |              |
| 15   | g      | out      |       |             |          |        |             |              |

Table E.6 Reynolds Shear Stress Calculation Summary of XS 16 ~ XS 17 for 16 cfs  
(psf)

|      | Column | 1       | 2     | 3           | 4        | 5     | 6           | 7            |
|------|--------|---------|-------|-------------|----------|-------|-------------|--------------|
| XSEC | Piezo  | Slope   | b     | $\tau_{xz}$ | Slope    | b     | $\tau_{yz}$ | $\tau_{bed}$ |
| 16   | a      | -47.288 | 0.458 | 0.010       | -199.770 | 0.175 | 0.001       | 0.010        |
| 16   | b      | -46.247 | 0.504 | 0.011       | 179.810  | 0.834 | -0.005      | 0.012        |
| 16   | c      | -29.265 | 0.577 | 0.020       | 176.080  | 0.710 | -0.004      | 0.020        |
| 16   | d      | -35.927 | 1.099 | 0.031       | 48.576   | 0.864 | -0.018      | 0.035        |
| 16   | e      | -36.451 | 0.896 | 0.025       | -30.185  | 0.325 | 0.011       | 0.027        |
| 16   | f      | out     |       |             |          |       |             |              |
| 16   | g      | out     |       |             |          |       |             |              |
| 17   | a      | out     |       |             |          |       |             |              |
| 17   | b      | -53.205 | 0.434 | 0.008       | 128.620  | 0.600 | -0.005      | 0.009        |
| 17   | c      | -24.473 | 0.407 | 0.017       | 113.890  | 0.580 | -0.005      | 0.017        |
| 17   | d      | -28.354 | 0.889 | 0.031       | 57.236   | 0.981 | -0.017      | 0.036        |
| 17   | e      | out     |       |             |          |       |             |              |
| 17   | f      | out     |       |             |          |       |             |              |
| 17   | g      | out     |       |             |          |       |             |              |

Table E.7 Reynolds Shear Stress Calculation Summary of Upstream Bend for 20 cfs  
(psf)

|      | Column | 1        | 2     | 3           | 4        | 5     | 6           | 7            |
|------|--------|----------|-------|-------------|----------|-------|-------------|--------------|
| XSEC | Piezo  | Slope    | b     | $\tau_{xz}$ | Slope    | b     | $\tau_{yz}$ | $\tau_{bed}$ |
| 4    | a      | -37.102  | 0.449 | 0.012       | 15.536   | 0.253 | -0.016      | 0.020        |
| 4    | b      | -85.760  | 0.415 | 0.005       | -32.778  | 0.297 | 0.009       | 0.010        |
| 4    | c      | -61.512  | 0.478 | 0.008       | 118.180  | 0.217 | -0.002      | 0.008        |
| 4    | d      | -68.330  | 0.666 | 0.010       | -105.620 | 0.648 | 0.006       | 0.012        |
| 4    | e      | -29.445  | 0.534 | 0.018       | -57.002  | 0.702 | 0.012       | 0.022        |
| 4    | f      | out      |       |             |          |       |             |              |
| 4    | g      | out      |       |             |          |       |             |              |
| 5    | a      | -72.948  | 0.603 | 0.008       | 7.410    | 0.306 | -0.041      | 0.042        |
| 5    | b      | out      |       |             |          |       |             |              |
| 5    | c      | -64.419  | 0.483 | 0.008       | -193.940 | 0.401 | 0.002       | 0.008        |
| 5    | d      | -95.145  | 0.838 | 0.009       | -103.370 | 1.020 | 0.010       | 0.013        |
| 5    | e      | -27.537  | 0.394 | 0.014       | -59.209  | 0.578 | 0.010       | 0.017        |
| 5    | f      | out      |       |             |          |       |             |              |
| 5    | g      | out      |       |             |          |       |             |              |
| 6    | a      | -71.402  | 0.747 | 0.010       | 20.729   | 0.252 | -0.012      | 0.016        |
| 6    | b      | -6.582   | 0.317 | 0.048       | -60.666  | 0.314 | 0.005       | 0.048        |
| 6    | c      | -48.443  | 0.410 | 0.008       | -395.840 | 0.541 | 0.001       | 0.009        |
| 6    | d      | out      |       |             |          |       |             |              |
| 6    | e      | -49.203  | 0.551 | 0.011       | -78.175  | 0.668 | 0.009       | 0.014        |
| 6    | f      | -60.304  | 0.536 | 0.009       | -103.610 | 0.698 | 0.007       | 0.011        |
| 6    | g      | -95.615  | 0.404 | 0.004       | 107.930  | 0.018 | 0.000       | 0.004        |
| 7    | a      | -28.184  | 0.502 | 0.018       | 182.830  | 0.487 | -0.003      | 0.018        |
| 7    | b      | -14.635  | 0.351 | 0.024       | -268.680 | 0.398 | 0.001       | 0.024        |
| 7    | c      | -37.299  | 0.415 | 0.011       | -696.570 | 0.714 | 0.001       | 0.011        |
| 7    | d      | -64.736  | 0.654 | 0.010       | -54.499  | 0.918 | 0.017       | 0.020        |
| 7    | e      | -63.306  | 0.528 | 0.008       | -91.264  | 0.687 | 0.008       | 0.011        |
| 7    | f      | -76.751  | 0.589 | 0.008       | -120.930 | 0.714 | 0.006       | 0.010        |
| 7    | g      | out      |       |             |          |       |             |              |
| 8    | a      | out      |       |             |          |       |             |              |
| 8    | b      | -63.233  | 0.583 | 0.009       | 77.498   | 0.215 | -0.003      | 0.010        |
| 8    | c      | -53.066  | 0.387 | 0.007       | -366.460 | 0.839 | 0.002       | 0.008        |
| 8    | d      | -80.959  | 0.686 | 0.008       | -53.388  | 0.827 | 0.015       | 0.018        |
| 8    | e      | -58.357  | 0.443 | 0.008       | -133.030 | 0.700 | 0.005       | 0.009        |
| 8    | f      | -121.830 | 0.526 | 0.004       | -152.670 | 0.659 | 0.004       | 0.006        |
| 8    | g      | out      |       |             |          |       |             |              |

Table E.8 Reynolds Shear Stress Calculation Summary of XS 10 ~ XS 15 for 20 cfs  
(psf)

|      | Column | 1       | 2     | 3           | 4        | 5      | 6           | 7            |
|------|--------|---------|-------|-------------|----------|--------|-------------|--------------|
| XSEC | Piezo  | Slope   | b     | $\tau_{xz}$ | Slope    | b      | $\tau_{yz}$ | $\tau_{bed}$ |
| 10   | a      | -34.832 | 0.713 | 0.020       | -269.780 | -0.042 | 0.000       | 0.020        |
| 10   | b      | -45.341 | 0.636 | 0.014       | 924.420  | 0.720  | -0.001      | 0.014        |
| 10   | c      | -8.296  | 0.338 | 0.041       | 198.940  | 0.386  | -0.002      | 0.041        |
| 10   | d      | -23.410 | 0.555 | 0.024       | -264.620 | 1.107  | 0.004       | 0.024        |
| 10   | e      | -73.351 | 0.596 | 0.008       | -181.650 | 0.681  | 0.004       | 0.009        |
| 10   | f      | -84.321 | 0.531 | 0.006       | -316.250 | 0.904  | 0.003       | 0.007        |
| 10   | g      | -73.644 | 0.576 | 0.008       | -388.540 | 1.040  | 0.003       | 0.008        |
| 11   | a      | out     |       |             |          |        |             |              |
| 11   | b      | out     |       |             |          |        |             |              |
| 11   | c      | -21.767 | 0.505 | 0.023       | 139.750  | 0.379  | -0.003      | 0.023        |
| 11   | d      | out     |       |             |          |        |             |              |
| 11   | e      | -49.223 | 0.692 | 0.014       | -92.230  | 0.514  | 0.006       | 0.015        |
| 11   | f      | out     |       |             |          |        |             |              |
| 11   | g      | out     |       |             |          |        |             |              |
| 12   | a      | -15.267 | 0.522 | 0.034       | -64.990  | 0.120  | 0.002       | 0.034        |
| 12   | b      | out     |       |             |          |        |             |              |
| 12   | c      | -22.967 | 0.661 | 0.029       | 127.750  | 0.627  | -0.005      | 0.029        |
| 12   | d      | -33.407 | 0.757 | 0.023       | 230.370  | 0.414  | -0.002      | 0.023        |
| 12   | e      | out     |       |             |          |        |             |              |
| 12   | f      | out     |       |             |          |        |             |              |
| 12   | g      | -46.766 | 0.729 | 0.016       | -41.799  | 0.353  | 0.008       | 0.018        |
| 13   | a      | -58.472 | 0.526 | 0.009       | -90.486  | 0.049  | 0.001       | 0.009        |
| 13   | b      | out     |       |             |          |        |             |              |
| 13   | c      | -15.042 | 0.671 | 0.045       | 70.757   | 0.694  | -0.010      | 0.046        |
| 13   | d      | -22.680 | 0.684 | 0.030       | 99.242   | 0.598  | -0.006      | 0.031        |
| 13   | e      | -47.751 | 0.780 | 0.016       | 289.290  | 0.465  | -0.002      | 0.016        |
| 13   | f      | -37.787 | 0.769 | 0.020       | -349.480 | 0.734  | 0.002       | 0.020        |
| 13   | g      | out     |       |             |          |        |             |              |
| 14   | a      | -59.165 | 0.562 | 0.010       | -105.600 | 0.014  | 0.000       | 0.010        |
| 14   | b      | -35.737 | 0.576 | 0.016       | 76.763   | 0.694  | -0.009      | 0.018        |
| 14   | c      | -17.143 | 0.610 | 0.036       | 67.368   | 0.684  | -0.010      | 0.037        |
| 14   | d      | -23.166 | 0.768 | 0.033       | 91.865   | 0.719  | -0.008      | 0.034        |
| 14   | e      | -36.839 | 0.813 | 0.022       | 209.000  | 0.615  | -0.003      | 0.022        |
| 14   | f      | out     |       |             |          |        |             |              |
| 14   | g      | out     |       |             |          |        |             |              |
| 15   | a      | -90.056 | 0.619 | 0.007       | 194.090  | 0.704  | -0.004      | 0.008        |
| 15   | b      | -46.539 | 0.653 | 0.014       | 107.430  | 0.858  | -0.008      | 0.016        |
| 15   | c      | -23.598 | 0.572 | 0.024       | 102.620  | 0.745  | -0.007      | 0.025        |
| 15   | d      | -13.616 | 0.767 | 0.056       | 48.387   | 0.722  | -0.015      | 0.058        |
| 15   | e      | -37.585 | 0.828 | 0.022       | 223.340  | 0.841  | -0.004      | 0.022        |
| 15   | f      | -24.744 | 0.765 | 0.031       | -104.440 | 0.505  | 0.005       | 0.031        |
| 15   | g      | out     |       |             |          |        |             |              |

Table E.9 Reynolds Shear Stress Calculation Summary of XS 16 ~ XS 17 for 20 cfs  
(psf)

|      | Column | 1       | 2     | 3           | 4       | 5     | 6           | 7            |
|------|--------|---------|-------|-------------|---------|-------|-------------|--------------|
| XSEC | Piezo  | Slope   | b     | $\tau_{xz}$ | Slope   | b     | $\tau_{yz}$ | $\tau_{bed}$ |
| 16   | a      | -76.102 | 0.555 | 0.007       | 336.330 | 1.135 | -0.003      | 0.008        |
| 16   | b      | -48.828 | 0.522 | 0.011       | 223.790 | 0.893 | -0.004      | 0.011        |
| 16   | c      | -25.677 | 0.594 | 0.023       | 78.620  | 0.760 | -0.010      | 0.025        |
| 16   | d      | out     |       |             |         |       |             |              |
| 16   | e      | out     |       |             |         |       |             |              |
| 16   | f      | -35.273 | 0.840 | 0.024       | -34.175 | 0.443 | 0.013       | 0.027        |
| 16   | g      | out     |       |             |         |       |             |              |
| 17   | a      | out     |       |             |         |       |             |              |
| 17   | b      | -53.979 | 0.571 | 0.011       | 60.137  | 0.612 | -0.010      | 0.015        |
| 17   | c      | -45.774 | 0.534 | 0.012       | 128.750 | 0.709 | -0.006      | 0.013        |
| 17   | d      | out     |       |             |         |       |             |              |
| 17   | e      | -23.885 | 0.678 | 0.028       | -34.993 | 0.272 | 0.008       | 0.029        |
| 17   | f      | out     |       |             |         |       |             |              |
| 17   | g      | out     |       |             |         |       |             |              |

**Appendix F. Comparison of Shear Stress from Linear  
Regression of Velocity Profile for Lateral Direction ( $\tau_y$ ) and  
Rozovskii Method**

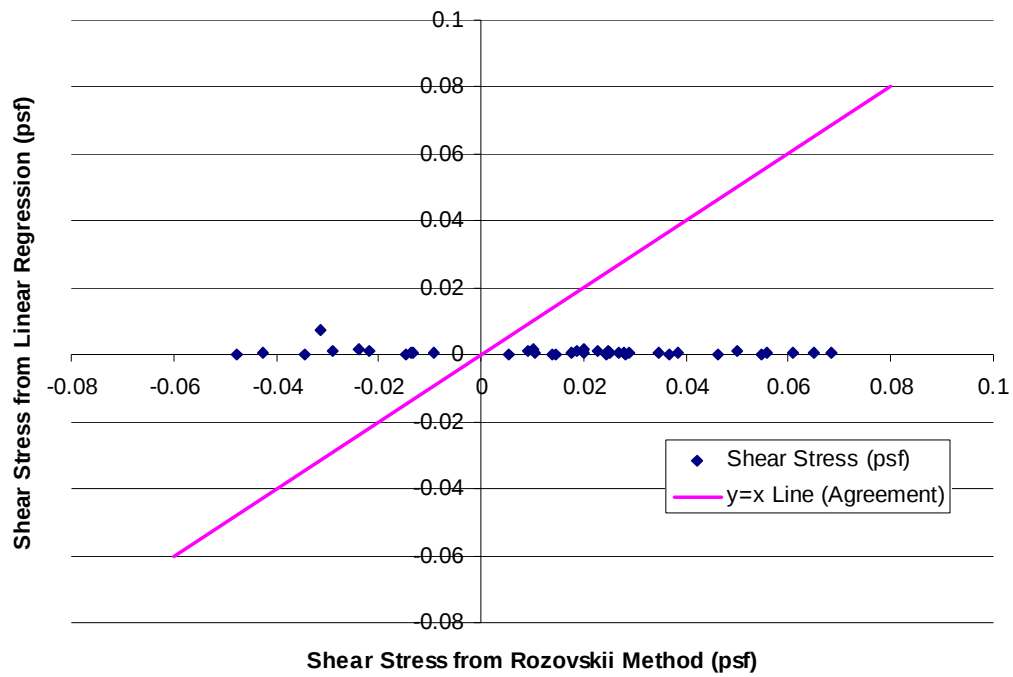


Figure F.1 Comparison of Shear Stress from Preston Tube and Rozovskii Method for 8 cfs

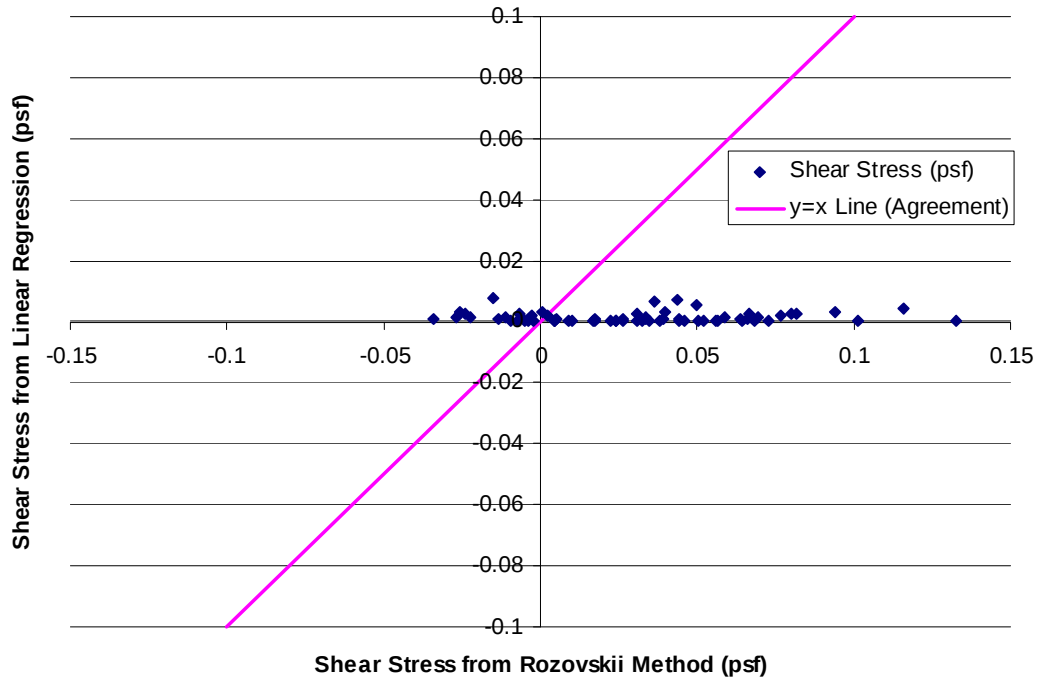


Figure F.2 Comparison of Shear Stress from Preston Tube and Rozovskii Method for 12 cfs

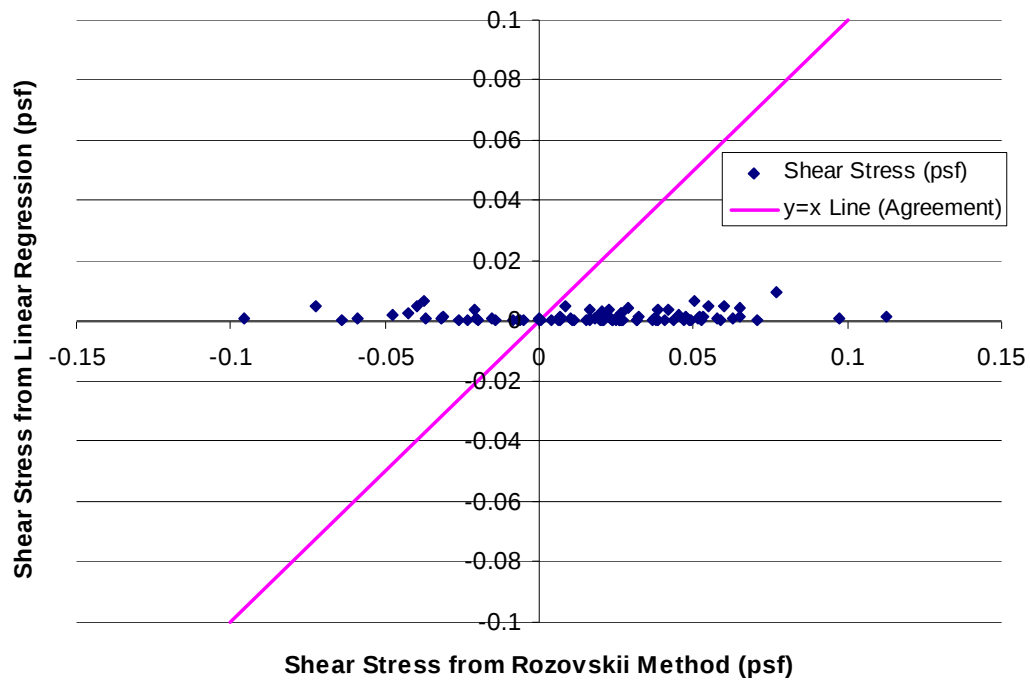


Figure F.3 Comparison of Shear Stress from Preston Tube and Rozovskii Method for 16 cfs

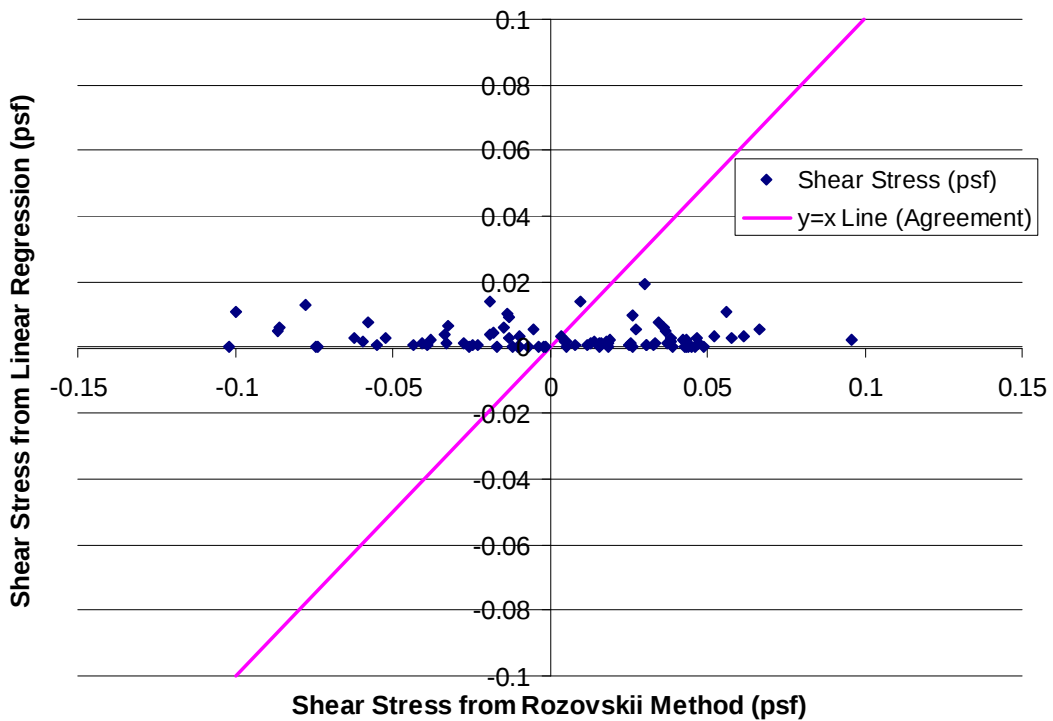


Figure F.4 Comparison of Shear Stress from Preston Tube and Rozovskii Method for 20 cfs

## **Appendix G. Comparison of Shear Stress Maximum Values**

## G.1 Comparison of Shear Stress Maximum Values

To compare shear stress calculation methods for different angles, maximum shear stress values from different methods are plotted in Appendix G. The blue lines in the plots show the averaged shear stress value from HEC-RAS. In upstream bend, shear stress from HEC-RAS in cross section 1 and 2 are averaged. For downstream bend, shear stresses from HEC-RAS in cross section 10 and 11 are averaged. Theoretically, the order of maximum value of shear stress should be; Shear stress from Preston tube > Shear stress from Reynolds shear extrapolation > Shear stress from linear regression because of the measurement method. The plots and prediction of the order of maximum shear stress was agreed well except for the case of 20 cfs in the upstream bend.

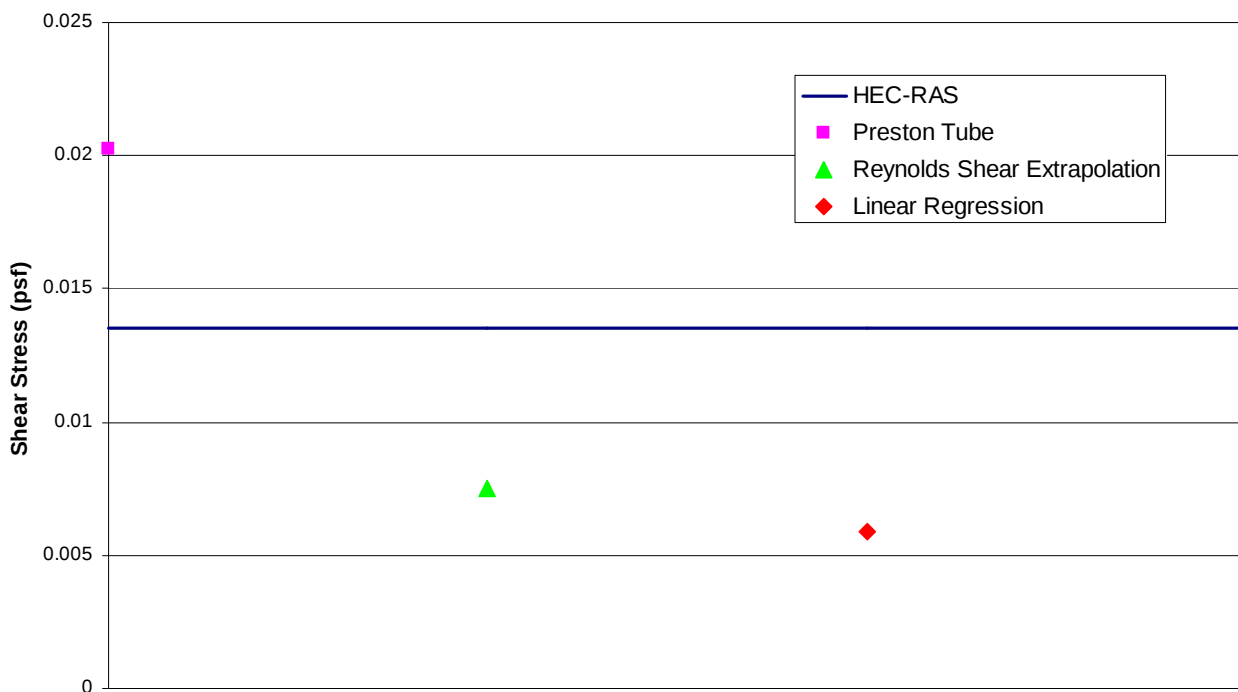


Figure G.1 Comparison of Shear Stress Maximum Values (8 cfs Upstream)

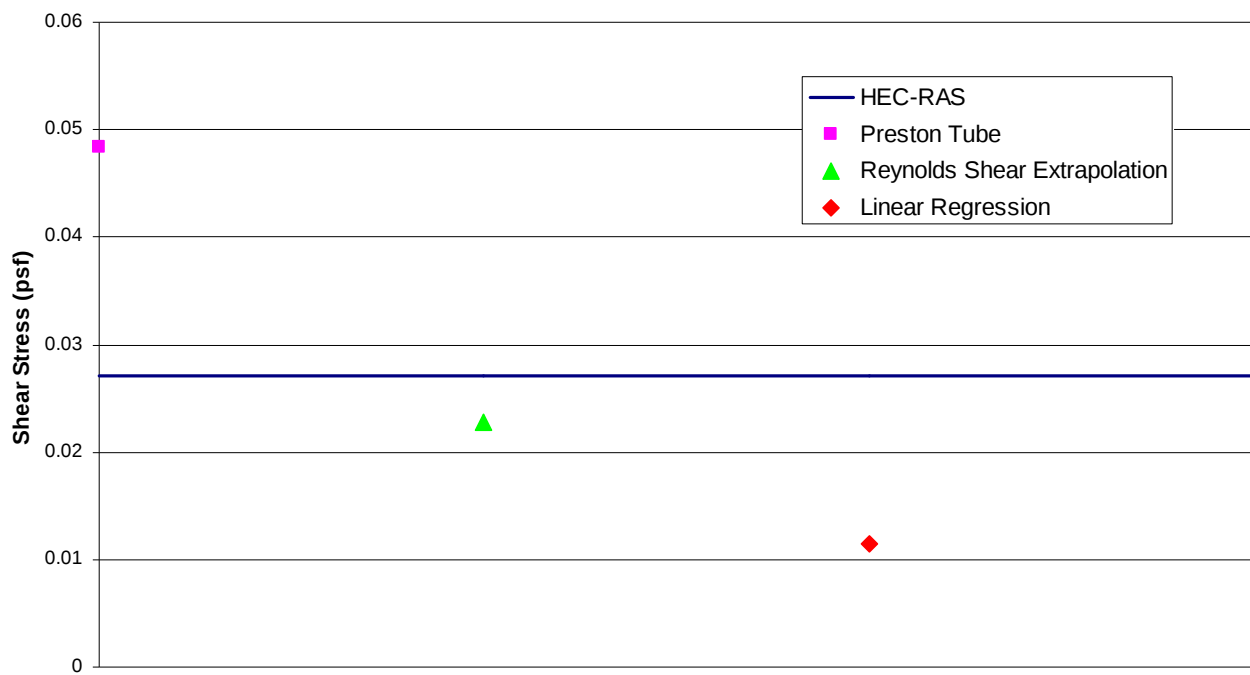


Figure G.2 Comparison of Shear Stress Maximum Values (8 cfs Downstream)

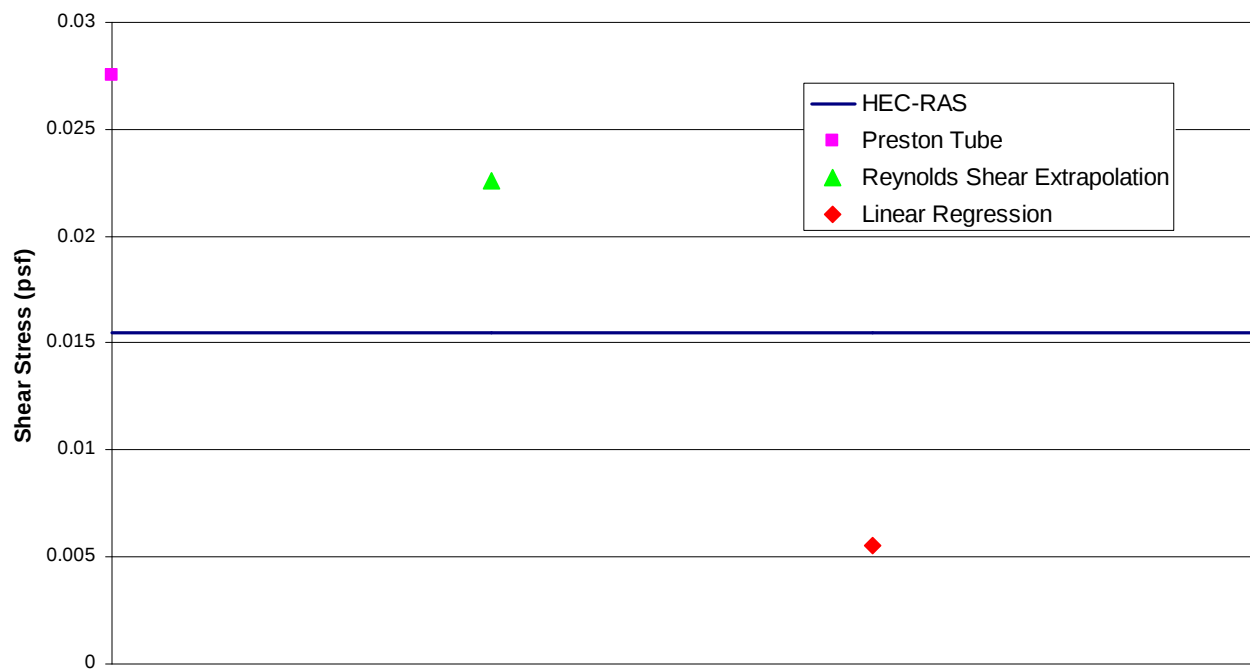


Figure G.3 Comparison of Shear Stress Maximum Values (12 cfs Upstream)

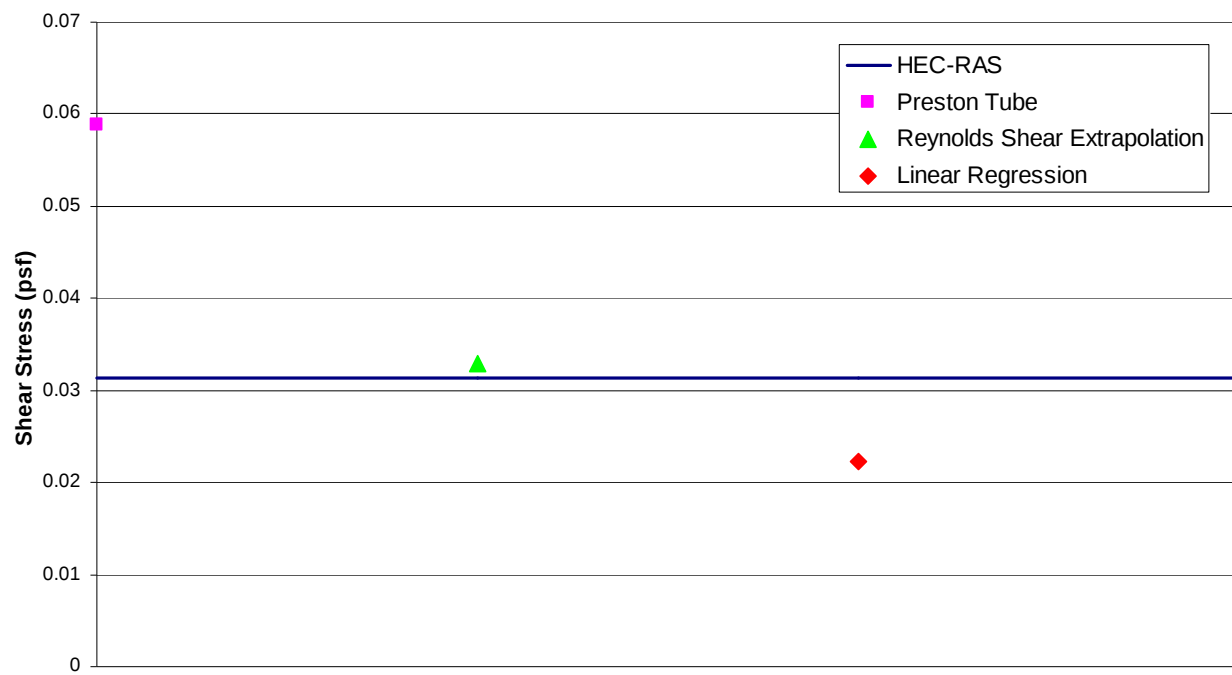


Figure G.4 Comparison of Shear Stress Maximum Values (12 cfs Downstream)

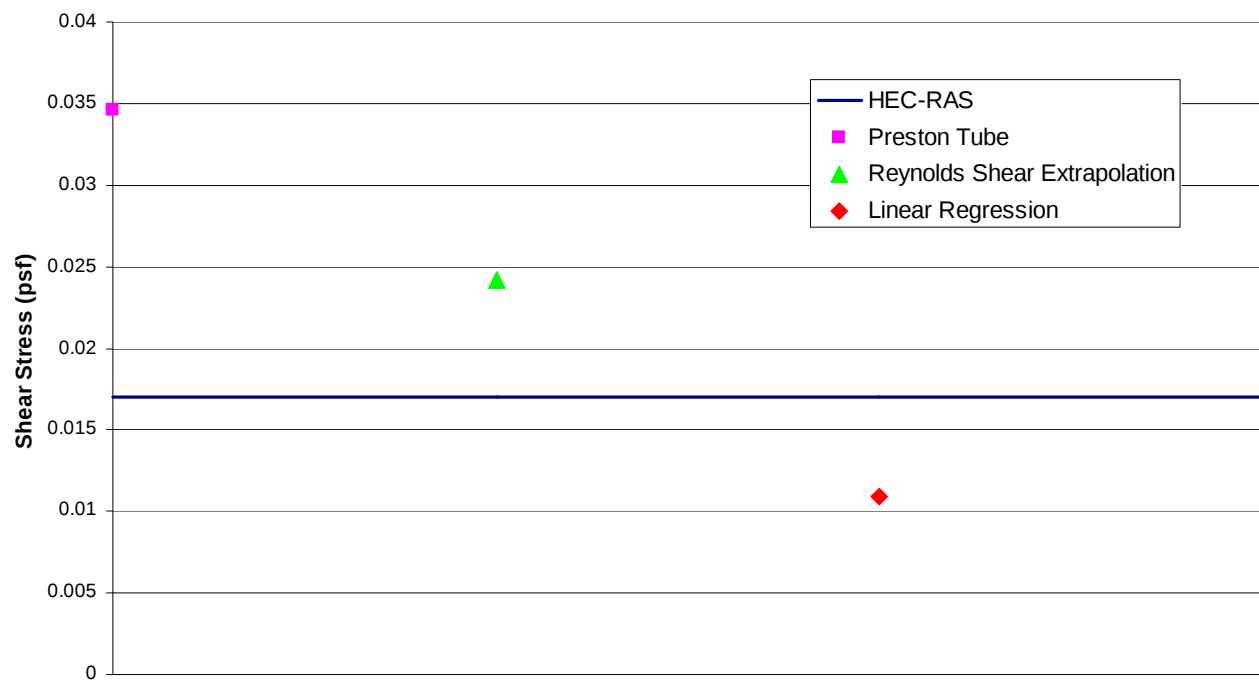


Figure G.5 Comparison of Shear Stress Maximum Values (16 cfs Upstream)

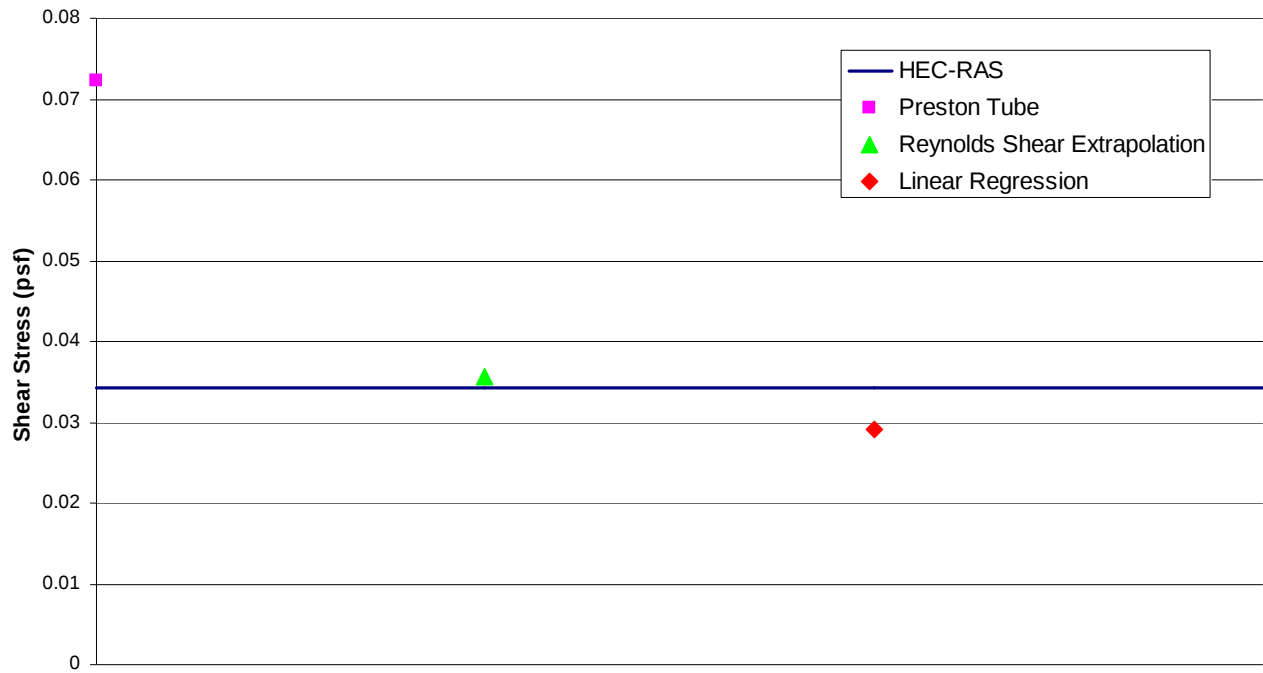


Figure G.6 Comparison of Shear Stress Maximum Values (16 cfs Downstream)

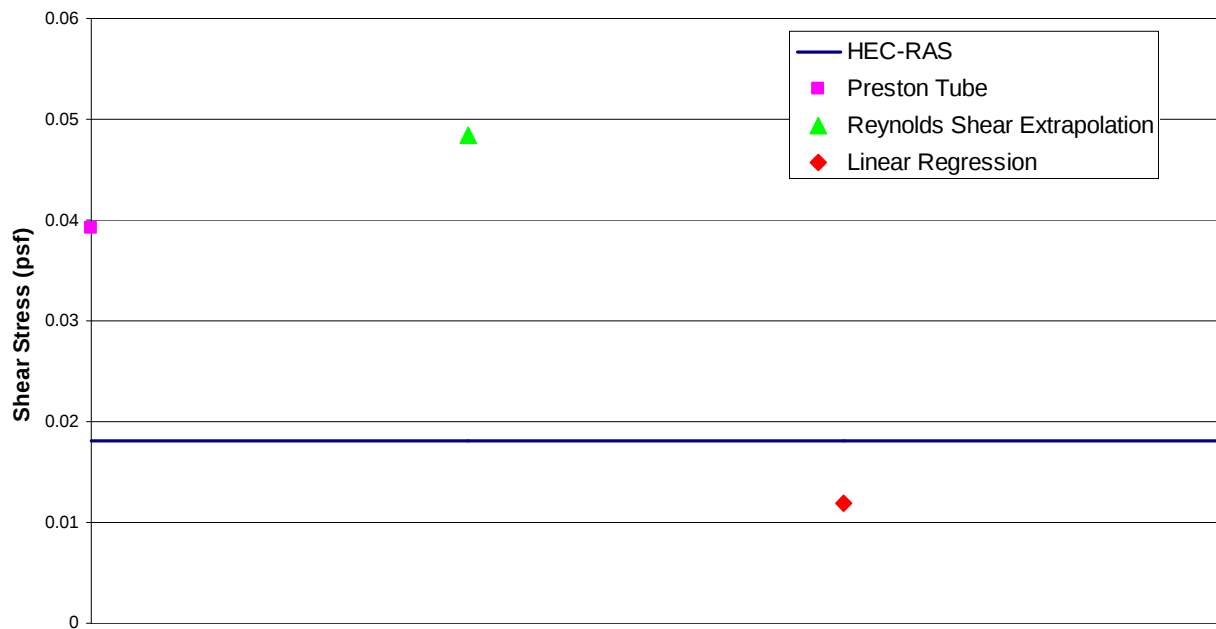


Figure G.7 Comparison of Shear Stress Maximum Values (20 cfs Upstream)

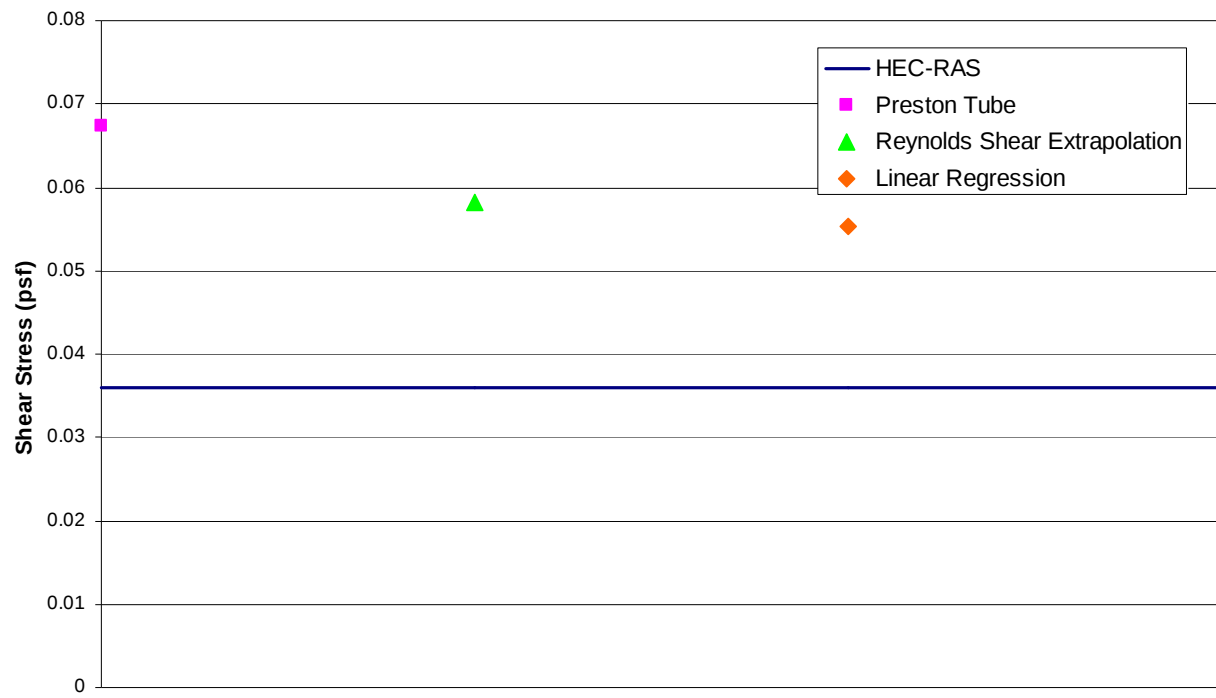


Figure G.8 Comparison of Shear Stress Maximum Values (20 cfs Downstream)